

CS 745 Fall 2017

## Assignment # 2

Due in class on Nov. 2nd

0. Consider the readers/writers problem on a single, shared object. Processes cycle over the following states: Non-trying, trying-to-read, trying-to-write, reading, writing. Processes non-deterministically choose between trying-to-read and trying-to-write. Once the choice is made they stay in that mode until they return to non-trying. There is a shared object to read/write and so several processes may read the object at the same time, but a process that is writing must have exclusive access to the object. Assume that each process can 'see' the internal state of each of the other processes. Processes execute asynchronously.

Write a correctness specification in CTL or LTL that expresses the requirements given above --- for shared or exclusive access to the resource. Describe a program skeleton model of the processes.

Explain why the model satisfies the temporal specification.

1. True or false:  $((GFp) \rightarrow (GFq)) \text{ EQUIV } G(p \rightarrow Fq)$
2. Let  $A_1$  and  $A_2$  be Buchi automata. Give a Buchi automaton  $A$  for the language  $L(A_1) \cup L(A_2)$  and explain your answer.
3. Consider a model  $M$  with states  $\{a, b, c, d, e\}$ . State  $a$  is the initial state. From  $a$  there is a transition to  $b$ . State  $b$  has bidirectional transitions to each of  $c, d$  and  $e$ . There are no other transitions. State  $a$  is labeled with  $\{p\}$ ,  $b$  is labeled with  $\{q\}$ ,  $c$  is labeled with  $\{r\}$ ,  $d$  is labeled with  $\{s\}$  and  $e$  is labeled with  $\{t\}$ .

Consider the sequences of computations encoded in the machine. The sequences of state labels, starting at the initial state define a language of the structure.

Does the language satisfy:

FGq?  
GFq?  
 $G(\sim q \rightarrow Xq)$ ?  
 $G(r \rightarrow XXr)$ ?

Justify your answers.

4. Consider the model in the previous section.

Does the model satisfy:

$AG(p + q + r + s + t)$ ?

$AG(q \rightarrow AXAXq)$ ?

$AG(r \rightarrow AXEXs)$ ?

$AG(r \rightarrow AFs)$ ?

Justify your answers.

5. Give a Buchi automaton that recognizes the same language as the LTL formula  $(GF p1) \wedge (GF p2)$ .

Give a Buchi automaton for the  $\sim((GF p1) \wedge (GF p2))$ .