Query Optimization and Execution Plan Generation in Object-Oriented Data Management Systems*

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Abstract

The generation of execution plans for object-oriented database queries is a new and challenging area of study. Unlike the relational algebra, a common set of object algebra operators has not been defined. Similarly, a standardized object manager interface analogous to storage manager interfaces of relational subsystems does not exist. We define the interface to an object manager whose operations are the executable elements of query execution plans. Parameters to the object manager interface are streams of tuples of object identifiers. The object manager can apply methods and simple predicates to the objects identified in a tuple. Two algorithms for generating such execution plans for queries expressed in an object algebra are presented. The first algorithm runs quickly but may produce inefficient plans. The second algorithm enumerates all possible execution plans and presents them in an efficient, compact representation.

Keywords: object-oriented databases, query processing, query optimization, execution plan generation.

1 Introduction

There is significant interest in object-oriented data management systems (OODMS) as an approach to handle the data management problems of complex application domains such as engineering databases, office information systems and knowledge bases. Unfortunately, the area is plagued by the lack of a formal and universally accepted object-oriented data model. Given the diversity of application domain requirements, there are many alternative design decisions regarding OODMSs. Some of these design decisions are significantly affected by the query model and the language interface. With this understanding, we have initiated a research project investigating query models

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and query processing issues in object-oriented data management systems. This paper describes
the results of one part of this investigation and is an expanded and revised version of [36]. Our
companion papers [34, 35] discuss other related issues.

We have defined a query processing methodology for an OODB (Figure 1) similar to that for
relational systems (see, for example [12, 16]). Queries are expressed in a declarative language
which requires no user knowledge of object implementations, access paths or processing strategies.
The query expression is first reduced to a normalized form and then converted to an equivalent
object algebra expression. This form of the query is a nested expression which can be viewed as
a tree whose nodes are algebra operators and whose leaves represent the extents of classes in the
database. The algebra expression is next checked for type consistency to insure that predicates
and methods are not applied to objects which do not support the requested functions. This is not
as simple as type checking in general programming languages since intermediate results, which are
sets of objects, may be composed of heterogeneous types. The next step in query processing is
the application of equivalence preserving rewrite rules to the type consistent algebra expression.
Lastly, an execution plan which specifies an ordering of primitive low-level operations while still
respecting object encapsulation is generated from the optimized algebra expression.

This paper addresses the last step in the query processing methodology shown in Figure 1,
namely execution plan generation, which is the process of mapping high level representations of
queries (i.e., object algebra expressions) to sequences of data manipulation operators of an object
manager. Details of the data model, full definition of calculus and algebra, including translation
algorithms, and some of the rewrite rules are covered in [34]. The full suite of algebra rewrite rules
is discussed in [33]. The type checking rules are given in [35] and the typechecking algorithm is
presented in [32]. In the case of the relational data model [7], there is a close correspondence between
algebra operations and the low level primitives of the physical system [26]. The mapping between
relations and files, and tuples and records may have contributed to this strong correspondence.
However, there is no analogous, intuitive correspondence between object algebra operators and
physical system primitives. Thus any discussion of execution plan generation must first define the
low level object manipulation primitives which will be the building blocks of execution plans. We call
this low level object manipulation interface the Object Manager (OM) interface. Object managers
have received attention lately in the context of distributed systems [4, 9, 21, 37], programming
environments [10, 17] and databases [6, 8, 11, 15, 20, 39]. These object managers differ in terms of
their support for data abstraction, concurrency, and object distribution. In addition, they are
typically oriented towards “one-at-a-time” object execution which is an inefficient paradigm for query processing.

The fundamental contributions of this paper are the following:

- Definition of a new OM interface which maintains many features of previous object managers but operates on streams of objects. This definition would not have been necessary if there was a standard, widely-accepted OM interface. In the absence of such a standard, we define our own interface and use it in the generation of execution plans.

- Description of algorithms for generating execution plans whose processing steps are calls to the stream-oriented object manager interface.

The rest of the paper is organized as follows. Section 2 reviews the object model and query language for which we generate query execution plans. Section 3 presents the object manager interface. Next, two algorithms for developing query execution plans are developed. The algorithm of Section 4 is simple but may not find best plans. Section 5 presents a more complex algorithm which finds all feasible plans and shows how OM cost functions can be used to select a best plan. In Section 6 we discuss two issues related to query optimization in OODMSs that are not address specifically in this paper: the use of OM cost functions to select an “optimum” execution plan and the optimization of method executions. We conclude in Section 7 with some observations about our methodology and suggestions for future work.

2 Overview of the Data and Query Model

This section presents the fundamental features of the data model as well as the query model that we use to investigate query processing issues in object-oriented database systems. Due to space constraints, the description given here is brief and appeals to intuition. For a rigorous and formal definition of these concepts, the reader is referred to [34] and [32]. As with the OM interface, the definition of the data model, which encompasses many of the features common to other object data models, is necessitated by the lack of a standard model specification.

2.1 Objects

Objects are viewed as instances of abstract data types (ADT) which can only be manipulated via functions defined by the type. Types are organized in an inheritance hierarchy which allows
multiple inheritance. An object \( o \) is a triple \( o = (id, cn, val) \) where \( id \) is a unique, time invariant identity which is independent of the object's state, \( cn \) is the name of the class that the object belongs to, and \( val \) is the value of the object. Relations on object identities such as equality and set inclusion provide the basis for primitive query operations. All other relations among objects are implemented by the ADT interfaces. Object values are either an atomic value provided by the database system (integer, string, uninterpreted byte sequence [6]), a set value which is a collection of object identifiers, or a structural value. Structural values can encompass attributes (tuples), discriminated unions, etc. as in [1].

2.2 Classes and Methods

Our model interprets a class both as a definition of an ADT interface via methods and as a template for all the objects which are instances of the type. Methods are named functions whose arguments and result are objects. Since our primary emphasis is on query models, we donot consider methods with side effects. Each method has a signature of the form \( C_1 \times \ldots \times C_n \rightarrow C_{\text{result}} \) where \( C_1 \ldots C_n \) specify the class of the argument objects and \( C_{\text{result}} \) specifies the class of the result object. All classes in the database form a lattice where the root node represents the most general class of objects and any individual class may have multiple parents. Subclasses inherit behavior from their parents and may define additional methods. Thus, the class lattice provides inclusion polymorphism [5] which allows an object of class \( C \) to be used in any context specifying a superclass of \( C \) [29].

2.3 Primitive Object Operations

Objects encapsulate a state and a behavior. An object’s state is captured by its value which is distinct from its identity [18, 30]. The different types of values that can represent the state of an object is discussed above. Methods defined on the class of which an object is an instance define the object’s behavior. A behavior is obtained by applying a method to an object. The result of a method application is another object. The dot notation \(<o_1 \ldots o_n>_m_1.m_2 \ldots m_m\) is used to denote method application and method composition. Figure 2 illustrates the processing denoted by this operation when we assume that methods \( m_1 \) and \( m_m \) take three arguments each, and method \( m_2 \) takes 2 arguments. Method \( m_1 \) is applied to objects \(<o_1,o_2,o_3>_r_1\) resulting in object \( r_1 \), method \( m_2 \) is applied to objects \(<r_1,o_4>_r_2\) returning object \( r_2 \), and so on until the final result object \( r_m \) is obtained by applying method \( m_m \) to objects \(<r_m-1,o_{n-1},o_n>_r\). The notation \(<o_1 \ldots o_n>_m\text{list}\) will be used when the list of method names is unimportant. This notation is sufficient to specify function
applications of the form \( f(g(h(x))) \), but do not permit applications of the form \( f(g(y), h(x)) \).

The behavioral nature of accessing an object’s state is particularly important for structural valued objects. Structural values are visible only to class implementors. Any aspects of structural values which are required by users of a class should be revealed by the implementor via a method. This is one aspect which differentiates our approach from others which explicitly support tuple values and permit access to their components.

We define four comparison operators which can be used in queries: \( ==, \in, \subseteq \) and \( = \) whose semantics are shown in Tables 1 and 2. The \( == \) operator tests for object identity equality; i.e., \( o_i == o_j \) evaluates to true when \( o_i \) and \( o_j \) denote the same object. The \( \in \) and \( \subseteq \) operators apply to set valued objects and denote set value inclusion and set value equality respectively. As shown in the tables, one of the operands can denote a value if required. When both \( o_i \) and \( o_j \) are sets, \( \in \) denotes the subset relationship \( (o_i \subseteq o_j) \). The last operator, \( = \), can only be used to test the value of an atomic object.

<table>
<thead>
<tr>
<th>( o_i )</th>
<th>( o_j )</th>
<th>( == )</th>
<th>( = )</th>
<th>( \in )</th>
<th>( \subseteq )</th>
</tr>
</thead>
<tbody>
<tr>
<td>atomic</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>structural</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>set</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>structural</td>
<td>T/F</td>
<td>undefined</td>
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<tr>
<td>atomic</td>
<td>T/F</td>
<td>undefined</td>
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<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>structural</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>set</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
</tbody>
</table>

Table 1: Semantics of \( o_i o_j \) as a function of the object value type.

<table>
<thead>
<tr>
<th>( a )</th>
<th>( o_i )</th>
<th>( == )</th>
<th>( = )</th>
<th>( \in )</th>
<th>( \subseteq )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( val_1 )</td>
<td>undefined</td>
<td>T/F</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>structural</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>set</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
</tr>
<tr>
<td>( {val_1, \ldots, val_n} )</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>undefined</td>
<td>T/F</td>
</tr>
</tbody>
</table>

Table 2: Semantics of \( a o_i \) as a function of the object value type.
2.4 Predicate Formation

Atoms\(^1\) are primitive operations of the data model which return a boolean result. Atoms reference lower case, single letter object variables which range over sets of objects when used in a query. The legal atoms are as follows:

- \(o_i \theta o_j\) where:
  - \(o_i\) and \(o_j\) are object variables or denote an operation of the form \(<o_1 \ldots o_n>.mlist\) where \(o_1 \ldots o_n\) are object variables.
  - \(\theta\) is one of the operators \(==, =, \in\) or \(=\).

- \(a \theta o_i\) where:
  - \(o_i\) is an object variable or denotes an operation of the form \(<o_1 \ldots o_n>.mlist\) where \(o_1 \ldots o_n\) are object variables.
  - \(a\) is the textual representation of an atomic value or a set of atomic values.
  - \(\theta\) is one of the operators \(=, \in\) or \(=\).

Predicates are formed by connecting atoms with \(\land, \lor\) and \(\neg\) as required.

**Example 2.1** Let \(p, q\) and \(r\) be object variables. Then the following are examples of legal atoms and their semantics:

1. \((p == q)\) – Are the objects denoted by \(p\) and \(q\) the same object?

2. \((p \in <q, r>.mlist)\) – Is the identifier of \(p\) contained in the set value of the object obtained by applying the methods in \(mlist\) to the objects \(<q, r>\)?

3. \((<p, q>.mlist = r)\) – Is the set value of the object obtained by applying the methods in \(mlist\) to the objects \(<p, q>\) pairwise equal to the set value of the object denoted by \(r\)?

4. \("59" = p\) – Is “59” the atomic value of the object denoted by \(p\)?

5. \("59" \in p\) – Does the set value of the object denoted by \(p\) include an identifier for the object whose atomic value is “59”?

\(^1\)Note that atom as part of a predicate and atomic objects as part of the model are different concepts. In retrospect, it might have been better to call the former terms, but we use atom in this paper to maintain consistency and continuity with our other papers on this topic [34, 35].
6. \( \{ "59", \text{"61"} \} = \{ q, r \} \) – Does the set value of the object obtained by applying the methods in \( mlist \) to the objects \( \langle p, q, r \rangle \) contain only two identifiers for objects whose atomic values are "59" and "61"? \\

2.5 Query Language – An Object Algebra

The object algebra contains both binary and n-ary operators. It is closed since the inputs and outputs of operators are sets of objects (strictly speaking, object identifiers). Let \( \Theta \) be an operator in the algebra. We use the notation \( P \Theta \langle Q_1 \ldots Q_n \rangle \) for algebra expressions where \( P \) and \( Q_i \) denote sets of objects. These could be classes (since a class in our model represents both the type and its extent) or intermediate sets of objects. In the case of a binary operator we will use \( P \Theta Q \) without loss of generality. Note that \( P \) and \( Q_i \) are sets of objects, not set-valued objects with their own identifiers.

The algebra defines five object preserving operators: union, difference, select, generate and map. These are fundamental operators; others may be defined (e.g., intersection) for convenience in terms of these. Object preservation means that algebra operators return objects which belonging to predefined classes in the database and do not create new objects. We have restricted our consideration to object-preserving algebras for two reasons. First, any OODMS query language must have a complete object-preserving query facility independent of whether it additionally creates new objects. The ability to retrieve any object in the database utilising relationships defined by the type hierarchy or defined by ADT operations on objects is a fundamental requirement. Second, object-creating operations raise a number of issues which were not addressed in this research, such as the type of the created objects and the operations they support, the relationship between object creation and dynamic schema evolution, and so on.

We will use a sample database (Figure 3) similar to that of [19]. Double lines represent subclass relationships and thin lines denote method signatures. For simplicity, only unary methods (e.g., \( \textit{manufacturer: Vehicle \rightarrow Company} \)) are used in the examples although real databases would take advantage of multiple argument methods (e.g., \( \textit{employees*: Company \times City \rightarrow SetOfPerson} \)). Methods marked with an asterisk such as \( \textit{employees}* \) and \( \textit{cars}* \) return objects with set values.

The following are the precise definitions of the algebra operators that are supported in our model, where \( P \) and \( Q_i \) are sets of objects as defined above and \( P(o) \) means \( o \in P \).

**Union** (denoted \( P \cup Q \)): The union is the set of objects which are in \( P \) or \( Q \) or both. An equivalent expression for union is \( \{ o \mid P(o) \lor Q(o) \} \).
Difference (denoted \(P - Q\)): The difference is the set of objects which are in \(P\) and not in \(Q\). An equivalent expression for difference is \(\{o \mid P(o) \land \neg Q(o)\}\). The intersection operator, \(P \cap Q\), can be derived by \(P - (P - Q)\).

Select (denoted \(P \sigma_F \langle Q_1 \ldots Q_k \rangle\)): Select returns the objects denoted by \(p\) in each vector \(<p,q_1 \ldots q_k> \in P \times Q_1 \times \ldots \times Q_k\) which satisfies the predicate \(F\). An equivalent expression for select is \(\{p \mid P(p) \land Q_1(q_1) \land \ldots \land Q_k(q_k) \land F(p,q_1,\ldots,q_k)\}\).

Multiple operands permit explicit joins as described in [19]. An explicit join is a join between arbitrary classes which support (a sequence of) method applications resulting in comparable objects.

**Example 2.2** The query "find all persons who live in a city which has an auto company" is an example of an explicit join. The select expression for this query is \(Person \sigma_F \langle AutoCompany \rangle\) where \(F \equiv (<p>\cdot address \eq <a>\cdot location)\), \(a\) ranges over \(AutoCompany\), and \(p\) ranges over \(Person\).

The result of this expression is a set of \(Person\) objects, rather than sets of \(<Person,AutoCompany>\) objects. This is due to the object-preserving nature of the algebra which disallows creation of new objects. Returning \(<Person,AutoCompany>\) objects would be equivalent to relational join, requiring the creation of new types of objects. In this sense, it can be said that the algebra supports the equivalent of relational semijoin operator, but not the join. As a result, the selection \(P \sigma_F \langle Q_1 \ldots Q_k \rangle\) always returns a subset of \(P\).

Generate (denoted \(Q_1 \gamma^p_F \langle Q_2 \ldots Q_k \rangle\)): \(F\) is a predicate with the condition that it must contain one or more generating atoms for the target variable \(t\), i.e., \(t\) does not range over any of the argument sets. The operation returns the objects denoted by \(t\) in \(F\) for each vector \(<q_1 \ldots q_k> \in Q_1 \times \ldots \times Q_k\) which satisfies the predicate \(F\). An equivalent expression for generate is \(\{t | Q_1(q_1) \land \ldots \land Q_k(q_k) \land F(t,q_1 \ldots q_k)\}\).

Generating atoms are unique in that they generate values for variables which do not range over an input set of the query (Table 3). They are called generating atoms because they generate objects for \(x\) from a constant value (entry 5), from the content of other objects (entries 2,4), or by applying methods to objects (entries 3,4). As an illustration, consider the query \(Q \gamma^p_{(p \in <q,r> \cdot enlist)} \langle R \rangle\). Variables \(q\) and \(r\) in the predicate range over the argument sets.
$Q$ and $R$ respectively and thus can be considered ‘bound’ in the query. However, variable $p$ is not bound to any argument set and the atom $p \in <q, r>, \text{\textit{mlist}}$ will evaluate to true only when $p$ ranges over the objects in the set value of the objects obtained by the method applications. Under these conditions then, the atom generates values for $p$.

<table>
<thead>
<tr>
<th></th>
<th>Table 3: Generating atoms for $x$.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$x == o$</td>
</tr>
<tr>
<td>2</td>
<td>$x \in o$</td>
</tr>
<tr>
<td>3</td>
<td>$x == &lt;a_1, \ldots, a_n&gt;, \text{\textit{mlist}}$</td>
</tr>
<tr>
<td>4</td>
<td>$x \in &lt;a_1, \ldots, a_n&gt;, \text{\textit{mlist}}$</td>
</tr>
<tr>
<td>5</td>
<td>$x = a$</td>
</tr>
</tbody>
</table>

**Example 2.3** An example is the query “return all cars driven by presidents of auto companies” where the $\text{\textit{cars^*}}$ method applied to a company president returns an object whose value is a set of car objects. The generate expression for this query is $\text{\textit{AutoCompany}} \gamma_F^I (\{\})$, where $F \equiv (t \in <a>, \text{\textit{president.cars}})$. The query “find all cities auto company employees live in” combines unnesting of set values with method application. The algebra expression is $\text{\textit{AutoCompany}} \gamma_F^I (\{\})$, where $F \equiv (x \in <a>, \text{\textit{employees}} \land t == <x>, \text{\textit{address}})$. Note that predicate $F$ contains generating atoms for two variables, $x$ and $t$, although only objects for $t$ are included in the result as specified by the $\gamma_F^I$ notation. ◊

**Map** (denoted $Q_1 \mapsto_{\text{\textit{mlist}}} \langle Q_2, \ldots, Q_k \rangle$): Let $\text{\textit{mlist}}$ be a list of method names of the form $m_1 \ldots m_m$. Map applies the sequence of methods in $\text{\textit{mlist}}$ to each object $q_1 \in Q_1$ using objects in $\langle Q_2 \ldots Q_k \rangle$ as parameters to the methods in $\text{\textit{mlist}}$. This returns the set of objects resulting from each sequence application. If no method in $\text{\textit{mlist}}$ requires any parameters, then $\langle Q_2 \ldots Q_k \rangle$ is the empty sequence $\langle \rangle$. Map is a special case of the generate operator whose equivalent is $\{ t \mid Q_1(q_1) \land \ldots \land Q_k(q_k) \land t == <q_1 \ldots q_k>, \text{\textit{mlist}} \}$. This form of the generate operation warrants its own definition as it occurs frequently and supports several useful optimizations. Map is similar to the $\text{\textit{image}}$ operator of [29].
3 The Object Manager

As we indicated in Section 1, relational DBMSs benefit from the close correspondence between the relational algebra operations and low level access primitives of the physical system. Therefore, access plan generation in relational systems basically concerns the choice and implementation of the most efficient algorithms for executing individual algebra operators and their combinations. In OODMSs the issue is more complicated due to the difference in the abstraction levels of behaviorally defined objects and their storage. Encapsulation of objects, which hides their implementation details, and the optimization of queries against these objects pose a challenging design problem which can simply be stated as follows: “At what point in query processing should the query optimizer access information regarding the storage of objects?” We differentiate between two types of object storage information: representation information, which specifies the data structures used to represent objects themselves, and physical storage information regarding the clustering of objects, indexes defined on them, etc. It is commonly accepted that object-oriented systems hide representation information within each object and not make it visible outside object boundaries. However, the visibility of physical storage information during query processing is the topic of some discussion. If object storage is under the control of an object manager, the design question can be posed in terms of the level of OM interface. Physical optimization of query executions requires storage information, arguing for a high-level OM interface that is accessed early in the optimization process. Many systems that are typically called “complex object systems” choose this approach. Encapsulation, on the other hand, hides storage details and, therefore, argues for a low-level OM interface that is accessed late in the process.

3.1 OM Design Principles

Since our data model treats objects as instances of abstract data types, encapsulation is a fairly important consideration. Furthermore, in our work, we are interested in investigating how far we could go with query processing without accessing the physical storage information. Therefore, we have elected to define a fairly low-level OM interface that is accessed late in the optimization process. Furthermore, the OM interface does not reveal any physical organization information. In other words, we are defining a lower level of abstraction than that provided by the data model and object algebra. We, therefore, split what is usually called “access path selection” in relational systems into two steps: (1) execution plan generation, which is the mapping of object algebra expressions
to object manager interface expressions; and (2) access plan selection, which involves the selection of the “optimum” execution plan and the efficient implementation of the object manager interface operations. In one sense, this is similar to query processing in distributed database systems [23] which involves both global plan generation and local optimization. In this paper we are mainly concerned with the first step, briefly touching upon the second in Section 6.1.

Object algebra expressions which are the input to the execution plan generation process have several important characteristics:

1. They can be represented as a graph whose nodes are object algebra operators and whose edges represent streams (sets) of objects. Thus intermediate results do not have any structure. In fact, the intermediate results can be thought of as streams of individual object identifiers.

2. Some algebra operators (σF, γF) are qualified by a predicate. Predicates are formed as a conjunction of atoms, each of which may reference several variables. The variable corresponding to the result of the algebra operation is called the target variable.

3. A variable name appearing in multiple atoms of a predicate implies a ‘join’ of some kind; i.e., objects denoted by the variable must satisfy several conditions concurrently.

The last point, namely implied ‘joins’ between object variables within a predicate, is the driving factor behind our query execution and execution plan generation strategy. Consider the predicate F for the select operation P σF (O, R, S, T)

\[ F \equiv o == \langle p, q, r, m_1 \rangle \land (q \in t) \land (q == <s>, m_2) \]  

(1)

where p is the target variable and O, P, R, S, T are inputs to the operation. All values for q are generated by the atoms in the predicate. The result of this select operation can be defined as

\[ \{ p | F(p, o, q, r, s, t) \text{ is true for } \langle p, o, r, s, t \rangle \in P \times O \times R \times S \times T \} \]  

(2)

Table 4 identifies which variables are referenced in each atom (numbered left to right) and reflects the dependencies between the variables.

It should be clear from the table that an object denoted by q must satisfy all three atoms. It might be tempting to have the query processor itself evaluate all of the atoms concurrently. However, if the data abstraction afforded by objects is to be respected, then it is not possible for the query processor to directly evaluate all three atoms concurrently. Instead, it is more likely that we call upon another agent which can perform individual operations on objects that correspond to
Table 4: Dependencies between variables in a predicate.

<table>
<thead>
<tr>
<th>o</th>
<th>p</th>
<th>q</th>
<th>r</th>
<th>s</th>
<th>t</th>
</tr>
</thead>
<tbody>
<tr>
<td>a1</td>
<td>x</td>
<td>x</td>
<td>x</td>
<td></td>
<td>(o ==&lt;p,q,r&gt;,m1)</td>
</tr>
<tr>
<td>a2</td>
<td></td>
<td>x</td>
<td></td>
<td>(q ∈ l)</td>
<td></td>
</tr>
<tr>
<td>a3</td>
<td>x</td>
<td>x</td>
<td></td>
<td>(q ==&lt;s&gt;,m2)</td>
<td></td>
</tr>
</tbody>
</table>

the individual atoms. This is because the evaluation of each atom requires access to the storage information (through the execution of methods) which we assume is not available at this level. This, in turn, requires the ability to keep track of the combinations of variables in $O \times P \times R \times S \times T$ which satisfy $F$. This intuition leads to the following design decisions.

1. The low level operators used to generate an execution plan for an algebra level operator will consume and generate streams (sets) of tuples of object identifiers$^2$. We introduce the notation $[a,b,c,\cdots]$ to denote a stream of tuples of object identifiers of the form $\{<a,b,c,\cdots>\}$. For convenience we will call this an oid-stream in the remainder of the paper. This way relationships among variables and the atoms they satisfy can be maintained over a sequence of operations.

2. The object manager interface performs low level operations comparable to individual atoms in a predicate.

3.2 OM Interface Specification

The object manager interface specifies a calling sequence and semantics for performing operations on oid-streams. Four operation types are defined:

$\text{OM}_u([i_1],[i_2],[\alpha])$ — stream union

$\text{OM}_d([i_1],[i_2],[\alpha])$ — stream difference

$\text{OM}_{eval}([i_1],\ldots,[i_n],[\alpha],[\alpha],meth,pred)$ — atom evaluation

$\text{OM}_{red}([i_1],\ldots,[i_n],[\alpha])$ — stream reduction

where $[i_n]$ and $[\alpha]$ denote input and output oid-streams respectively. The semantics of the OM calls are described next.

(1) **Stream Union**: This operator generates the union of the two input oid-streams. Streams $[i_1]$ and $[i_2]$ must reference the same variable names though not necessarily in the same order.

$^2$Note that our reference to tuples here is not to the structural values; these are tuples of oids.
The operation is analogous to the relational union operator. The output oid-stream contains those tuples which are present in \([i_1]\) or \([i_2]\) projected onto the variables identified by the output specifier \([o]\).

**Example 3.1** Consider the stream union operation

\[
\text{OM}_U([a, b, c, d], [c, d, b, a], [c, b])
\]

This operation generates the union of the two streams and outputs a stream consisting of tuples \(<c, b>\).

(2) **Stream Difference:** This operator generates the difference of the two input oid-streams. Streams \([i_1]\) and \([i_2]\) must reference the same variable names though not necessarily in the same order. The operation is analogous to the relational difference operator. The output oid-stream contains those tuples which are in \([i_1]\) but not in \([i_2]\) projected onto the variables identified by the output specifier \([o]\).

(3) **Atom Evaluation:** This operator applies the (optional) method given by \texttt{meth} to each member of \([i_1] \times \ldots \times [i_n]\) creating the intermediate oid-stream \([i_1] \times \ldots \times [i_n] \times [res]\) where \texttt{res} is the result of the method application for each \(i_1, \ldots, i_n\) combination. Next, the predicate \texttt{pred} is applied to the intermediate oid-stream and the result is projected onto those variables given in the output stream identifier \([o]\). More specifically:

- \([i_1], \ldots, [i_n]\) denote a set of oid-streams which represent the input to the object manager call. A variable name may appear in only one input stream.

- \([o]\) denotes the oid-stream which will be returned as output of the object manager call. A variable name may appear only once in the output stream. Variables referenced in the oid-stream \([o]\) are a subset of those in the input streams or the special identifier \texttt{res}.

- \texttt{meth} is an optional method application specifier of the form \(<a, b, \ldots >.mname\), where \(a, b, \ldots\) correspond either to variables in the input streams or are the textual representation of an atomic value. The special identifier \texttt{res} denotes the result of the method application and can be referenced in the output stream and predicate.

- \texttt{pred} is an optional predicate on objects in the input streams and/or result of the \texttt{meth} field. The full set of permissible predicates is given in Table 5. Variables in the predicate
correspond either to variables in the input streams, the special identifier res or are the
textual representation of an atomic value (denoted by const in the table).

<table>
<thead>
<tr>
<th>$o_i \equiv o_j$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$o_i \in o_j$</td>
</tr>
<tr>
<td>$o_i \equiv_0 o_j$</td>
</tr>
<tr>
<td>$\text{const} = o$</td>
</tr>
<tr>
<td>$\text{const} \in o$</td>
</tr>
<tr>
<td>$o \in \text{const}$</td>
</tr>
<tr>
<td>$\text{const} \equiv_0 o$</td>
</tr>
</tbody>
</table>

Table 5: Predicates allowed in $\text{OM}_{\text{eval}}$ calls.

An $\text{OM}_{\text{eval}}$ call must have either a method or a predicate specified, and can have both if required. If specified, the method is always applied before the predicate is evaluated. The special identifier res denotes the result of the method application and can be referenced in the output stream or predicate only if a method is specified.

The input streams may contain variables which are not referenced in the output stream, the method or the predicate. In this case the respective oids in the input streams are ignored. Variables referenced in the input streams and output stream but not in the method or predicate are carried through without modification. In this case, the unreferenced oid in each input tuple which satisfies the predicate after the optional method has been applied is copied unchanged to the corresponding output tuple. There is no relationship or restrictions on the ordering of variables in the input streams and output stream.

**Example 3.2** Consider the atom evaluation operation

$$\text{OM}_{\text{eval}}([a,b],[c],[res,c],<c,a>.m,b \in res)$$

The semantics of this operation are given by the following algorithm.

```
for (each tuple $t : <a,b,c> \in [a,b] \times [c]$) begin
  let $res$ be the object returned by $<t,c,t.a>.m^3$
  if ($t,b \in res$) then
    add the tuple $<res,t,c>$ to the output stream
```

14
(4) **Stream Reduction:** This operator combines and reduces the number of input streams by performing an equijoin on those variables which are common to all input streams. This requires that all input streams have at least one variable name in common. The semantics of the operation is best described using an example.

**Example 3.3** Consider the stream reduction

\[
\text{OM}_{\circ}( [a, b, c], [b, d, c], [e, c, b], [a, b, c])
\]

The variables common to all input streams are \(b\) and \(c\). We can rewrite the operation as

\[
\text{OM}_{\circ}( [a, b_1, c_1], [b_2, d, c_2], [e, c_3, b_3], [a, b, c])
\]

in order to differentiate the different sources for variables \(b\) and \(c\). The input streams are first combined by taking their cross product which results in the oid-stream \([a, b_1, c_1, b_2, d, c_2, e, c_3, b_3]\). The final result stream is of the form \([a, b, c]\) and contains only those tuples from the previous intermediate result where \((b_1 = b_2 = b_3) \land (c_1 = c_2 = c_3)\). Note that the equality (\(=\)) here is among oids; therefore, this check is not part of the algebra.

We note that many object algebra and object query optimization studies (e.g., [2, 13, 28, 38]) assume the existence of an object manager interface. However, few, if any, of them have defined it explicitly. It could be argued that the interface defined in this paper is not sufficient to serve as a standard, but this is difficult to judge at this stage of development of object-oriented systems. At least, the interface meets the goals specified in Section 3.1 and in the remainder of the paper we develop mechanisms for using this interface effectively.

The reasons for choosing this interface will become clearer in Sections 4 and 5 when we discuss execution plan generation. The primary consideration is to define a stream-oriented interface that matches the algebra operations defined earlier. Union and difference operations map directly to their object manager counterparts. Map operation maps to (a sequence of) atom evaluations. The mapping of select and generate operations involve both atom evaluation and stream reduction.

---

3We use the notation \(t.c\) to denote component \(c\) of tuple \(t\).
As indicated earlier, this is a low-level interface that is crossed quite late in query processing (but not necessarily as late as method invocation). There are obvious advantages and disadvantages to this approach. The fundamental advantage follows from fully obeying the encapsulation of objects. Physical storage decisions (e.g., dynamic clustering) can be clearly separated from logical aspects of query optimization, yet the effects of these decisions can be incorporated into the optimization process without major hardship. One disadvantage is delaying the use of cost models and, therefore, potentially losing out on some possible optimizations. We discuss this further in Section 6.1. A second potential problem is the individual optimization of each operator. It is well-known from work on relational systems that there may be optimization opportunities when operations are considered together (e.g., a join followed by a selection) which may not be available when each operation is considered in isolation. This may also prove to be a problem in our case. Since work on object-oriented query optimization is relatively immature, we do not yet know all of the trade-offs involved. As more experimentation is carried out, it may be necessary to define a higher level interface.

4 Execution Plan Generation

Execution plan generation can be thought of as creating a mapping from object algebra expression trees to trees of object manager operations. A query is initially represented as a tree of object algebra operators as shown in Figure 4(a). Edges in the figure have been annotated with oid-stream labels to indicate that a set of objects, e.g., \( P \), can be considered a stream of individual objects, e.g., \([p]\) as well. One unique feature of object algebra expression trees is that all edges represent streams of single objects, never streams of multiple objects. This is due to the closed nature of the algebra which insures that the output of any operation can be used as input to another.

The graph in Figure 4(b) represents an execution plan corresponding to the algebra tree on the left. An execution plan graph is a graph whose nodes are OM operators and whose edges are oid-streams. It is evaluated from the leaves to the root. The subtrees within dotted rectangles are sequences of object manager operations corresponding to individual algebra operators of the original query. Edges which do not cross subtree boundaries may represent streams of tuples of objects (e.g., \([p, q]\) and \([s, o]\)). In addition, streams may be used as input to multiple object manager operations within a subtree, e.g., \([q]\).

The following sections show how the mapping to object manager operators is performed for
each of the object algebra operators ($\cup$, $\cap$, $\sigma_F$, $\tau_{m\text{list}}$ and $\gamma_F$). For ease of presentation, we will first intuitively discuss how these operations can be mapped to execution plan graphs and then develop formal algorithms.

### 4.1 Union and Difference Operations

The union and difference operators map directly to their object manager counterparts. Inputs and output of these two algebra operations are always unary streams of objects even though $\text{OM}_\cup$ and $\text{OM}_\text{diff}$ accept streams of tuples of object identifiers.

### 4.2 Map Operation

Reviewing briefly, the map operator $Q_1 \mapsto_{m_1 \ldots m_n} (Q_2, \ldots, Q_k)$ denotes a sequence of method applications (called a multi-operation) $\langle q_1, \ldots, q_k \rangle . m_1 \ldots m_n$ where $\langle q_1, \ldots, q_k \rangle$ are drawn from $Q_1 \times \ldots \times Q_k$. Since the object manager interface can only apply one method per call, the multi-operation must be decomposed into individual method applications. Determining which $q_i$ are a parameter for a given $m_j$ has been treated previously in [35] and is not repeated here. Figure 5 depicts how the map operation $Q_1 \mapsto_{m_1, m_2, m_3, m_4} (Q_2, Q_3, Q_4, Q_5, Q_6, Q_7)$ is represented as a sequence of OM operations. The formal algorithm to perform this transformation is given in Algorithm 4.1.

**Algorithm 4.1** *Create execution plan graph for the map operator*

**Input:** Object algebra map operation of the form $Q_1 \mapsto_{m_1 \ldots m_n} (Q_2, \ldots, Q_k)$

**Output:** Execution plan graph $G$

1. let $G := \phi$ \hspace{1cm} \text{initialization}
2. use the type inference rules of [35] to create mappings $m_i \rightarrow q_2, \ldots, q_y$ where:
   - $i$ denotes the $i^{th}$ method in $m_1 \ldots m_n$
   - $x$ denotes the subscript in $Q_1, \ldots, Q_k$ of the second argument to $m_i$
   - $y$ denotes the subscript in $Q_1, \ldots, Q_k$ of the last argument to $m_i$
3. let $r_0 := q_1$
4. for ($i := 1$ to $n$) begin
5.   add node $\text{OM}_{\text{end}}([r_{i-1}], [q_2], \ldots, [q_y], [r_i], \langle r_{i-1}, q_2, \ldots, q_y \rangle . m_i, r_i \Rightarrow r \text{es})$ to $G$
6.   if (this is not the first node to be placed) then
7.     add an edge to $G$ connecting the output of the node placed on the previous pass to the first input ($[r_{i-1}]$) of the node placed on this pass
8.   endif
9. endfor
10. end.
4.3 Select and Generate

The select and generate operators introduce complexity into execution plan generation due to their use of predicates. At first it may appear that the two should be treated separately as select returns a subset of an input set while the generate generates objects from those in the input sets. But from the perspective of low level execution plan creation, they are quite similar. Consider again the selection predicate of Equation 1 in Section 3.1. Even though the operation is a selection, the predicate generates values for \( q \). There is no inherent difference in complexity between predicates for selections and those for generate operations. The only real distinction between the two is that the target variable of a generate operation does not correspond to one of the input sets.

Figures 6 and 7 illustrate several possible execution plans, specified as execution plan graphs, for the select example whose predicate is given in Equation 1. Nodes in these execution plan graphs are either \( \text{OM}_{\text{eval}} \) operations corresponding to individual atoms of the predicate or \( \text{OM}_{\text{M}} \) operations for reducing intermediate oid-streams. \( \text{OM}_{\text{eval}} \) nodes are labeled with the atom they represent (\( a_1 \), \( a_2 \) or \( a_3 \)) while \( \text{OM}_{\text{M}} \) nodes are labeled with the \( \& \) symbol.

The first requirement in creating these execution plans is to rewrite the predicate such that each atom does indeed correspond to just a single object manager call. This is done by applying the following rewrite rules.

1. Given an atom of the form \( const = var \) where \( const \) is the textual representation of an atomic value and \( var \) is some object variable, remove the atom from the predicate and replace each occurrence of \( var \) with the text of \( const \).

2. Replace all occurrences of atoms of the form

\[
(\text{multi-op}_1 \ \theta \ \text{multi-op}_2)
\]

with

\[
(\text{multi-op}_1 \ \theta \ new_{var}) \ \land \ (new_{var} \ \theta \ \text{multi-op}_2)
\]

where \( new_{var} \) is a newly introduced object variable currently unused in the predicate and \( \theta \in \{=,==,\epsilon,\neq\} \). This insures there is only one multi-operation per atom.

3. Expand each multi-operation into a sequence of single method applications. This is identical to the steps performed for the map operator in Section 4.2. Using the map operation of
Figure 5 as an example, the following equivalence would be used:

\[
\langle q_1, q_2, q_3, q_4, q_5, q_6, q_7 \rangle.m_1.m_2.m_3.m_4 \equiv \begin{align*}
\ r_1 = & <q_1, q_2 >. m_1 \land \\
\ r_2 = & <r_1, q_3, q_4 >. m_2 \land \\
\ r_3 = & <r_2, q_5, q_6 >. m_3 \land \\
\ res = & <r_3, q_7 >. m_4
\end{align*}
\]

where \( r_i \) and \( res \) are previously unused object variables.

Table 6 illustrates how each of the simplified atoms is mapped to an object manager call. The table shows all variables from the input streams being carried through to the output stream merely to illustrate the full extent of possibilities. Typically the output stream would be a subset of the input stream variables. Note that some atoms may be mapped to more than one OM call. The “comment” column in the table indicates the condition under which that particular mapping would be valid. In this context, \( res(a) \) means that variable \( a \) is restricted\(^4\) in the predicate in which that atom exists, and \( gen(a) \) indicates that the atom is a generating atom for variable \( a \).

We are now ready to consider, in some detail, the alternative execution plans in Figures 6 and 7 for the sample select operation. Each execution plan assumes that atoms in the predicate are sorted into a dependency order where values for non-input variables are generated before they are used; i.e., an atom which generates \( q \) comes before an atom which uses \( q \). In the predicate of Equation 1 variable \( q \) is ‘generated’ twice, once by \( a2 : q = t \) and again by \( a3 : q = <s>. m_2 \), and only ‘referenced’ in \( a2 : o = <p, q, r >. m_1 \). Thus one of either \( a2 \) or \( a3 \) must be performed before \( a1 \). However, once values for \( q \) have been generated by one of these atoms, the semantics of conjunction allow us to think of the remaining atom as restricting \( q \) as opposed to generating new values for \( q \). As long as oid-streams for all variables referenced by the remaining two atoms are present, their ordering is irrelevant. The execution plans of Figures 6 and 7 express some of the variations which are possible within this framework.

**Plan 1:** (Figure 6) In this plan, the first OM operation\(^5\) consumes atom \( a2 \) and creates an output oid-stream which contains those variables required by the remaining unconsumed atoms \((a1, a3)\). Since \( t \) is not referenced by either \( a1 \) or \( a3 \) it can be omitted from the output oid-stream. It is important to realize, though, that the OM operation to do this (designated by

\(^4\)The restriction of variables is defined formally in [34]. It is necessary for the safety of query expressions such that the query terminates in finite time and produces finite output.

\(^5\)Recall that OM operator trees are evaluated bottom up.
Table 6: Mapping simplified atoms to \( \text{OM}_{\text{eval}} \) calls.

| \( a \) == \( b \) | \( \text{OM}_{\text{eval}}([a, b], [\cdot], \phi, a == b) \) | \( \text{res}(a, b) \) |
| \( o == <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, \phi) \) | \( \text{gen}(o) \) |
| \( a \in b \) | \( \text{OM}_{\text{eval}}([b], [\cdot], \phi, a \in b) \) | \( \text{gen}(a) \) |
| \( \phi, a \in b \) | \( \text{OM}_{\text{eval}}([a, b], [\cdot], \phi, a \in b) \) | \( \text{res}(a, b) \) |
| \( o \in <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, o \in \text{res}) \) | \( \text{gen}(o) \) |
| \( <a, b, \cdots > \cdot m \in o \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, o \in \text{res}) \) | \( \text{res}(\cdot) \) |
| \( a =_{(\cdot)} b \) | \( \text{OM}_{\text{eval}}([a, b], [\cdot], \phi, a =_{(\cdot)} b) \) | \( \text{res}(a, b) \) |
| \( o =_{(\cdot)} <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, o =_{(\cdot)} \text{res}) \) | \( \text{res}(\cdot) \) |
| \( \text{const} =_{(\cdot)} <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], \phi, \text{const} =_{(\cdot)} \text{res}) \) | \( \text{res}(a, b, \cdots) \) |
| \( \text{const} \in o \) | \( \text{OM}_{\text{eval}}([o], [\cdot], \phi, \text{const} \in o) \) | \( \text{res}(o) \) |
| \( \text{const} \in <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, \text{const} \in \text{res}) \) | \( \text{res}(a, b, \cdots) \) |
| \( <a, b, \cdots > \cdot m \in \text{const} \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, \text{res} \in \text{const}) \) | \( \text{res}(a, b, \cdots) \) |
| \( \text{const} =_{(\cdot)} o \) | \( \text{OM}_{\text{eval}}([o], [\cdot], \phi, \text{const} =_{(\cdot)} \text{res}) \) | \( \text{res}(o) \) |
| \( \text{const} =_{(\cdot)} <a, b, \cdots > \cdot m \) | \( \text{OM}_{\text{eval}}([a, b, \cdots], [\cdot], <a, b, \cdots > \cdot m, \text{const} =_{(\cdot)} \text{res}) \) | \( \text{res}(a, b, \cdots) \) |

\( a2 \) in the diagram) requires taking the cross product \( O \times P \times R \times S \times T \). In other words, an \( \text{OM} \) operation always takes the cross product of all its input oid-streams prior to applying a method and evaluating a predicate. The next object manager call consumes atom \( a3 \) and drops variable \( s \) from its output since it is not required by the remaining unconsumed atom \( (a1) \). The last object manager call consumes the remaining atom and includes only the target variable in its output stream.

In summary, variables which represent generated objects are added to the intermediate oid-stream upon generation (e.g., \( q \)). Variables in the intermediate oid-stream are dropped by the last object manager call which references them, e.g., \( t \). The final object manager call includes only the target variable in its output.

**Plans 2.3:** (Figure 6) These two plans are similar to the first except that cross products of some variables are delayed until just before the object manager call which requires them. Since
\( a1 \) is the only atom which references variables \( a, p \) and \( r \), prior OM calls for atoms \( a2 \) and \( a3 \) need not carry through these variables without using them. Plans 2 and 3 differ only in which atom is chosen to generate values for \( q \) first.

**Plan 4:** (Figure 7) This plan exercises another interpretation of the semantics of conjunction: if two atoms generate values for the same variable, then the final set of values is the equijoin of the separately generated values. This parallelization technique has been combined with delayed cross products to minimize the size of parameters to object manager calls. For example, if we had performed an early cross product as in plan 1, then the input to \( q \in t \) (\( a2 \)) would be \([a, p, r, s, t]\) which has many more tuples than there are unique values of \( t \).

**Plans 5,6:** (Figure 7) These two plans utilize the same semantic principles as in plan 4, only in a different fashion. As before, cross products are delayed as long as possible. The two atoms which generate values for \( q \) are performed in parallel. The output of only one of these atoms is combined with \( a, p \) and \( r \) to restrict values of \( p \) and to generate the oid-stream \([p, q]\). However, unlike earlier restrictions, both \( p \) and \( q \) are retained in the output stream of this object manager call. We now have two oid-streams containing values for \( q \), \([q]\) and \([p, q]\). The final oid-stream representing the target variable \( p \) is created by performing an OM operation on the two streams and projecting over the \( p \) component.

Let us attempt to generalize the relative merits and drawbacks of these execution plans. It would seem that ‘just in time’ cross product generation is beneficial as it reduces intermediate oid-stream sizes, both in cardinality and in arity. Cardinality is reduced since restrictions are performed on the oid-stream prior to subsequent cross products. Arity is reduced as new variables are introduced only when needed rather than at the start of the subquery. The argument for delayed cross product generation would be even stronger if the complexity of the cross product operator grew non-linearly with respect to either the number of fields or the stream length. The parallelization performed in plans 5 and 6 looks beneficial initially, but has several drawbacks. One is that values for \( q \) are not restricted as much as they are in all the other plans prior to being used in later operations, e.g., to restrict \( p \). Second, the intermediate oid-streams are larger since \( q \) must be carried through until the final OM operation. Plans 2 and 3 are similar to 4 in that they perform all restrictions on \( q \) as early as possible. Their relative merits would depend on the efficiency of parallel operations combined with OM versus the sequential implementation.

Based on these observations, it is possible to develop an algorithm for generating type 2 and 3
plans: i.e., delayed cross products combined with early restriction. The algorithm takes three inputs:
(1) a set of atoms corresponding to a predicate which has been rewritten using the simplification
rules presented earlier, (2) a set of variable names identifying inputs to the object algebra level
operation, and (3) the name of the target variable. Output is an execution plan graph. The
algorithm uses a hypergraph [3] representation of the predicate. The hypergraph contains one
node for each unique variable name referenced in the atoms of the predicate and is initialized with
an edge for each atom which covers all nodes corresponding to variables referenced in the atom.
(Note that edges in a hypergraph define subsets of its nodes.) The nodes are marked as either red
or green. A green node indicates that values for this variable exist, either because the variable
is a member of the second input parameter or because an object manager call has generated the
values. A red marking indicates that values do not exist, i.e., the variable may not be used yet.
The node markings are initialized to reflect the variables which represent inputs to the object
algebra operation. The initial hypergraph corresponding to Equation 1 is shown in Figure 8-A.
The algorithm proceeds by successively placing into the execution plan graph $\text{OM}_{\text{eval}}$ operations
for atoms (hypergraph edges) until all atoms have been placed. An atom is eligible for placement
in the execution plan graph if all the nodes in its corresponding edge are green, or only one node is
red but it represents a variable whose values are generated by the atom. The complete algorithm
is given in Algorithm 4.2, which will be improved further in Section 5.

Algorithm 4.2 Create execution plan for Select/Generate operators

Inputs:
1. set of simplified atoms $a_1, \ldots, a_n$
2. set of input variable names $V$
3. target variable name $t$

Output: Graph of object manager operations $G$

let $H$ be the initialized hypergraph for $a_1, \ldots, a_n$ \hspace{1cm} (1)
let $G$ be the output execution plan graph – initially empty \hspace{1cm} (2)
let $\text{stream}\_\text{vars}$ represent variables in the intermediate oid-stream – initialized to $\phi$ \hspace{1cm} (3)

while (there are edges in $H$) begin \hspace{1cm} (4)
  let $a \in H$ be an edge (atom) eligible for placement \hspace{1cm} (5)
  – all variables are green or one is red and generated by the atom, and
  – if $\text{stream}\_\text{vars}$ is non-empty $a$ references all variables in $\text{stream}\_\text{vars}$
  let $i := 1$ \hspace{1cm} (6)
  let $\text{in}\_\text{stream}_i := \text{stream}\_\text{vars}$ \hspace{1cm} (7)
  for (all nodes $n_j \in a \mid n_j \in V \land n_j \not\in \text{stream}\_\text{vars})$ begin \hspace{1cm} (8)
    let $\text{in}\_\text{stream}_{(+i)} := n_j$ \hspace{1cm} (9)
  end \hspace{1cm} (10)
let out_stream contain any variables which edge \( a \) shares with other
edges in \( H \) and \( t \) iff \( t \) is a member of any in_stream

add OM\textsubscript{eval}([in_stream\textsubscript{1}], \ldots, [in_stream\textsubscript{i}], [out_stream], meth, pred) to \( G \) where:
method meth and predicate pred reflect atom \( a \) as per Table 6

if (this is not the first atom to be placed) then

connect in_stream\textsubscript{1} to the out_stream of the node placed on the previous pass

endif

let stream_vars := out_stream

color all nodes \( n_j \in a \) green

remove edge \( a \) from \( H \)

dend

Example 4.1 We will apply Algorithm 4.2 to the predicate of Equation 1. Figure 8-A shows the initialized hypergraph with an edge for each atom in the predicate. Note that the node for \( q \) is red while all others are green indicating that \( q \) does not range over an input set. During the first pass through the while loop both atoms \( a2 \) and \( a3 \) are eligible for placement because all but one node in their respective hypergraph edges are green and each atom generates values for the single red node. Atom \( a1 \) is ineligible at this point as it does not generate values for the red node. Let us assume atom \( a3 \) is chosen at random leading to the placement of its corresponding object manager call (labelled \( a3 \) in Figure 8-B). After placing \( a3 \), \( q \) is colored green, since values now exist for it, and the edge for atom \( a3 \) is removed from the hypergraph. In the second pass, both of the remaining atoms are eligible for placement and we assume atom \( a1 \) is randomly chosen. The output oid-stream of the corresponding OM call is \([p, q]\) because (1) atom \( a1 \) overlaps with \( a2 \) on \( q \), and (2) \( p \) is the target variable. The result of the second pass is shown in Figure 8-C. The algorithm terminates after placing the remaining atom \( a2 \) (Figure 8-D). ◦.

5 Select/Generate Execution Plans Revisited

The previous section introduced the notion of an execution plan as a tree of object manager operations. Queries expressed as trees of object algebra operators are converted to execution plans by mapping each operator in the algebra tree to a corresponding subgraph of object manager operations. Algorithms were developed to perform this mapping for union and difference (Section 4.1), map (Section 4.2), and the select and generate operators (Section 4.3).

This section examines the mapping process for select and generate operators in more detail. The algorithm presented in Figure 4.2 is quite limited in that it can only generate execution plans which are a linear sequence of OM\textsubscript{eval} operations. Specifically:
• only one execution plan is generated,

• the ordering of multiple eligible OM operations is determined by random choice and does not allow a cost based analysis of different orderings,

• object manager operations are never performed in parallel, and

• OM\textsubscript{om} is not used to reduce intermediate oid-streams.

Ideally we would like to generate a family of execution plans from which a best plan can be chosen based on some cost criteria. With respect to the select predicate of Equation 1, this would imply that the algorithm generate all feasible plans including those of Figures 6,7 and Example 4.1.

To assist us in an exhaustive generation of execution plans, we extend the notion of a join template [24] to define a processing template. A processing template represents a family of logically equivalent execution plans. They are used as an intermediate formalism in mapping object algebra query trees to execution plan graphs. Processing templates have been incorporated into various query optimizers such as System R [27] and Starburst [14]. A processing template for the predicate of Equation 1 is given in Figure 9.

A processing template consists of two types of nodes: stream nodes and operator nodes. Stream nodes (drawn as rectangles in Figure 9) represent intermediate results in a tree of object manager operations, i.e., execution plan graph. In other words, stream nodes reflect the variables present in an intermediate oid-stream and the atoms which were evaluated to produce them. Since there are conceivably many ways to produce equivalent oid-streams, each stream node in the processing template represents an equivalence class of oid-streams.

Each stream node has two fields. The top field denotes the object variables present in the oid-stream. The bottom field denotes which atoms of the predicate have been evaluated in order to create the oid-stream, but does not indicate the order in which the atoms were evaluated. We will refer to these atoms as being consumed by the stream node.

Operator nodes (drawn as circles in Figure 9) denote the OM\textsubscript{eval} or OM\textsubscript{om} operations in a select or generate execution plan graph. As in the execution plans of Section 4, an operator node is labeled with an atom number ($a1$, $a2$, etc.) if it corresponds to a OM\textsubscript{eval} operation and with \textsuperscript{1}\textsubscript{om} if it is a stream reduction operation.

Stream nodes with no consumed atoms, i.e., the leaf nodes, represent the original input streams of an object algebra select or generate operator. We define the final node as the stream node in
the processing template whose variables field contains just the target variable of the object algebra operator and whose atoms consumed field contains all the atoms in the object algebra operator’s simplified predicate. The final node is always node 0.

Edges represent the flow of tuples from one node to the next. Individual execution plans are represented by connected subgraphs of the processing template which cover all leaf nodes and the final node.

Referring to Figure 9, nodes 1 through 5 represent the original input streams to the algebra operation of Equation 1 and node 0 represents the final result. Node 6 is the result of the object manager operation \( OM_{eval}([s],[q],<s>,m_2,q == res) \) and node 7 is the result of \( OM_{eval}([l],[q],p,q \in t) \). Each of these nodes represents an equivalence class of size one as they each only have one input. Node 8 represents an equivalence class with three members. Using oid-streams subscripted with their processing template node numbers to indicate their source, the following OM calls all create the equivalent output denoted by stream node 8.

\[
\begin{align*}
OM_{eval}([q], [l], [q], p, q \in t) & \quad \text{ (atom a2)} \\
OM_{eval}([q], [s], [q], <s>, m_2, q == res) & \quad \text{ (atom a3)} \\
OM_{eval}([q], [q], [q]) & \quad \text{ (reduction on q)}
\end{align*}
\]

Each connected subtree of edges in the processing template which includes all initial nodes and the final node is a valid execution plan. As an example, the dashed edges in Figure 10 correspond to the execution plan shown in the top right of the diagram. Careful examination of the diagram will reveal that it includes all of the execution plans of Figure 6 and 7.

Our goal is to develop an algorithm which, given a select or generate operation in the object algebra, returns a processing template which enumerates all possible execution plan graphs for that operation. In the remainder, we first describe the algorithm using an extended example and then provide a more formal definition.

This example shows how the processing template is developed for the object algebra operation of Equation 1. An initial processing template is created by identifying the input streams of the algebra operation and placing nodes for each of them. In our example the input streams are \([o], [p], [r], [s]\) and \([l]\) corresponding to nodes 1, 2, 3, 4 and 5 respectively. The final node, node 0, is also placed in the processing template. Its variables field contains either the variable being restricted in the case of a select operation or the target variable in the case of a generate operation. The example operation is a selection on the input set \( P \), thus \( p \) is placed in the final node. Similarly, all atoms of the reduced predicate \((a1,a2,a3)\) are placed in the final node’s consumed atoms field.

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Once the initial processing template is created, the following steps are repeated until it is no longer possible to create any new stream nodes. We will refer to each iteration of the following steps as a pass through the algorithm.

5.1 Pass 1

Recall that processing template stream nodes represent oid-streams which can be combined to evaluate atoms or to remove duplicates. The first step of each pass then, is to enumerate all possible ways of combining stream nodes. We use the algorithm given in [22] for join enumeration but modify it slightly such that it does not produce combinations where a stream node is combined with itself (self-join). The final node is not included in the enumeration. Enumeration of the initial processing template results in the following permutations of stream nodes. Each permutation is shown as a set of node numbers and the sets are organized by size.

1: \{1\} \{2\} \{3\} \{4\} \{5\}
2: \{1,2\} \{1,3\} \{2,3\} \{1,4\} \{2,4\} \{3,4\} \{1,5\} \{2,5\} \{3,5\} \{4,5\}
3: \{1,2,3\} \{1,2,4\} \{1,3,4\} \{2,3,4\} \{1,2,5\} \{1,3,5\} \{2,3,5\} \{1,4,5\} \{2,4,5\} \{3,4,5\}
4: \{1,2,3,4\} \{1,2,3,5\} \{1,2,4,5\} \{1,3,4,5\} \{2,3,4,5\}
5: \{1,2,3,4,5\}

Similar to the filtering process described in [22], each permutation is tested to determine whether it is a useful combination of stream nodes. Each permutation of stream nodes defines mappings to sets of variables and sets of consumed atoms. For example the permutation \{1,2,5\} defines the mapping shown in Figure 11.

We define two interesting types of mappings:

1. The variable sets are disjoint and, together, all the variables exactly match those required by an atom which has not been consumed by any of the nodes in the permutation. In other words, an unused atom can be consumed using exactly those streams represented by the nodes in the permutation. We can now create a third mapping from the permutation under consideration to a set of atoms which can be consumed by the combination of streams in the permutation. The set of atoms which can be consumed by the combination of streams in the permutation (i.e., eligible for placement) is shown in Figure 12.

The first permutation in Figure 12, \{1,2,5\}, does not meet our criteria while the other permutations do. Although the variables which \{1,2,5\} maps to are disjoint, they do not exactly match the variables required by an unconsumed atom.
For each permutation with a non-empty set of eligible atoms, we consume each atom in the set by adding a stream node and operator node with appropriate connections to the processing template. In Pass 1, permutation \{4\} leads to the placement of stream node 6 and the operator node labeled a3 while permutation \{5\} leads to placement of stream node 7 and the operator node labeled a2. No other placements are possible. Since each stream node in the processing template represents an equivalence class of oid-streams, we do not always place a new stream node. If a stream node already exists with the appropriate set of variables and consumed atoms, only the operator node is added and the appropriate connections made.

2. One or more variables are replicated in each of the variable sets. Discussion of this case is deferred to Pass 2 since the condition does not occur during Pass 1 in this example.

At the end of the first pass the processing template consists of stream nodes 0–7 and the OM operations which connect them.

5.2 Pass 2

Pass 2 begins by again enumerating all possible combinations of stream nodes. However, since the contents of a stream node are not modified after it is initially added to the processing template (only new connections are made), we only need to enumerate all new permutations of stream nodes which were not considered in any of the previous passes. This results in the following new permutations.

1: \{6\} \{7\}
2: \{1,6\} \{2,6\} \{3,6\} \{4,6\} \{5,6\} \{1,7\} \{2,7\} \{3,7\} \{4,7\} \{5,7\} \{6,7\}
3: \{1,2,6\} \{1,3,6\} \{2,3,6\} \{1,4,6\} \{2,4,6\} \{3,4,6\} \{1,5,6\} \{2,5,6\} \{3,5,6\} \{4,5,6\} \{1,2,7\} \{1,3,7\} \{2,3,7\} \{1,4,7\} \{2,4,7\} \{3,4,7\} \{1,5,7\} \{2,5,7\} \{3,5,7\} \{4,5,7\} \{1,6,7\} \{2,6,7\} \{3,6,7\} \{4,6,7\} \{5,6,7\}
4: \{1,2,3,6\} \{1,2,4,6\} \{1,3,4,6\} \{2,3,4,6\} \{1,2,5,6\} \{1,3,5,6\} \{2,3,5,6\} \{1,4,5,6\} \{2,4,5,6\} \{3,4,5,6\} \{1,2,3,7\} \{1,2,4,7\} \{1,3,4,7\} \{2,3,4,7\} \{1,2,5,7\} \{1,3,5,7\} \{2,3,5,7\} \{1,4,5,7\} \{2,4,5,7\} \{3,4,5,7\} \{1,2,6,7\} \{1,3,6,7\} \{2,3,6,7\} \{1,4,6,7\} \{2,4,6,7\} \{3,4,6,7\} \{1,5,6,7\} \{2,5,6,7\} \{3,5,6,7\} \{4,5,6,7\}
5: \{1,2,3,4,6\} \{1,2,3,5,6\} \{1,2,4,5,6\} \{1,3,4,5,6\} \{2,3,4,5,6\} \{1,2,3,4,7\} \{1,2,3,5,7\} \{1,2,4,5,7\} \{1,3,4,5,7\} \{2,3,4,5,7\} \{1,2,3,6,7\} \{1,2,4,6,7\} \{1,3,4,6,7\} \{2,3,4,6,7\} \{1,2,5,6,7\} \{1,3,5,6,7\} \{2,3,5,6,7\} \{1,4,5,6,7\} \{2,4,5,6,7\} \{3,4,5,6,7\}
6: \{1,2,3,4,5,6\} \{1,2,3,4,5,7\} \{1,2,3,4,6,7\} \{1,2,3,5,6,7\} \{1,2,4,5,6,7\} \{1,3,4,5,6,7\} \{2,3,4,5,6,7\}
7: \{1,2,3,4,5,6,7\}
As before, we build the mappings of stream node permutation to variables and consumed atoms and apply the filtering criteria. In this pass, both types of mappings which we consider interesting occur.

1. Mapping type 1 – The variable sets are disjoint and together, all variables exactly match those required by an atom which has not been consumed by any of the stream nodes in the permutation. These criteria are met by permutations \(\{4,7\}, \{5,6\}, \{1,2,3,6\}\) and \(\{1,2,3,7\}\). The mapping to variables and consumed atoms for two of these permutations (randomly chosen for illustrative purposes) are shown in Figure 13. Permutation \(\{4,7\}\), which can be used to consume atom \(a_3\), would result in a stream node whose consumed atoms are \(a_2\) and \(a_3\) and whose variables field includes only \(q\). Since this is identical to stream node 8, we just make the connections to node 8 rather than create a new stream node. This maintains the notion of a stream node representing an equivalence class of oid-streams. The same is true for permutation \(\{5,6\}\) which can be used to consume atom \(a_2\).

Permutations \(\{1,2,3,6\}\) and \(\{1,2,3,7\}\) also meet our criteria and result in the creation of nodes 9 and 10 respectively.

2. Mapping type 2 – One or more variables are replicated in each of the variable sets. This condition means that several stream nodes exist with values for the same variable(s) and that an OM14 operation can be used to combine and reduce the oid-streams. Permutation \(\{6,7\}\) meets this criteria for variable \(q\) as shown in Figure 14.

Each stream node in the permutation represents values for variable \(q\) generated by a different set of atoms. In other words, node 6 represents values for \(q\) generated by atom \(a_3\) while node 7 represents values for \(q\) generated by atom \(a_2\). The nodes are joined by an OM14 operation and all variables required by unconsumed atoms are carried through to the output oid-stream. In this case, the output oid-stream would contain only the variable \(q\) and would have consumed atoms \(a_2\) and \(a_3\). Since this is equivalent to node 8, we only add the OM14 operator node and make connections to node 8 rather than create an entirely new stream node.

5.3 Pass 3

Enumeration of all stream nodes results in the following interesting permutations: \(\{1,2,3,8\}\), \(\{7,9\}\), \(\{8,9\}\), \(\{6,10\}\), \(\{8,10\}\) and \(\{9,10\}\). All of these permutations cause insertion of operator
nodes only and do not cause any new stream nodes to be added to the processing template. The first permutation consumes an atom resulting in the placement of a $OM_{eval}$ operation while all others result in $OM_{M}$ operations. A further criteria is applied to the $OM_{M}$ creating permutations which was not mentioned earlier.

Each of the stream nodes in the permutation must add to the consumed atoms field of the result. For example, permutation $\{6,9\}$ is not acceptable as all of node 6's consumed atoms (\{a3\}), are already represented in those of node 9 (\{a1,a3\}).

The algorithm terminates after Pass 3 because no new stream nodes were created in this pass. In other words, enumerating all stream node combinations again will not result in any permutations which were not evaluated previously.

The full algorithm for exhaustive execution plan enumeration is given in Algorithm 5.1.

Algorithm 5.1 Create Execution Plan for Select/Generate Operators

Inputs:
1. set of simplified atoms $a_1, \ldots, a_n$
2. set of input variable names $V$
3. target variable name $t$

Output: Processing template, $Pt(V,E)$, enumerating multiple access plans
- Names denoting a set of items begin with an upper case letter, e.g., $Pt$ is a set of processing template nodes.
- Names denoting a set of sets are completely upper case.
- All other names are lower case.

define $ENUM(i)$ to return the set of all permutations of numbers in $[1, \ldots, i]$. For example, $ENUM(3)$ returns the set $\{\{1\},\{2\},\{3\},\{1,2\},\{1,3\},\{2,3\},\{1,2,3\}\}$.

define $max\_node()$ to return the highest numbered node in $Pt$.

define $exists\_node(Var\_set,Atom\_set)$ to return the number of the node in $Pt$ with $Var\_set$ and $Atom\_set$ in its ‘variables’ and ‘atoms consumed’ fields respectively, or $-1$ if such a node is not found.

define $add\_node(Var\_set,Atom\_set)$ to add a node with the given parameters to $Pt$. Nodes will be numbered consecutively starting at 0.

define $connect(From\_nodes,to\_node,using)$ to connect the nodes in $From\_nodes$ to $to\_node$ in $Pt$ via the $OM$ operation defined by $using$.

define $Retained\_vars(Var\_set,Atom\_set)$ to return the set of variable names which should be retained in the output stream after the variables in $Var\_set$ are used to consume or join the atoms in $Atom\_set$. This is identical to the technique used to determine which variables to retain in the intermediate stream used in Algorithm 4.2.
define \texttt{FindConsumableAtoms(Var.set, Atom.set)} to return a set of atoms which can be consumed using the variables in \texttt{Var.set} and assuming the atoms in \texttt{Atom.set} have already been consumed. This is similar to the technique used in Algorithm 4.2 to pick an eligible atom only here all eligible atoms are returned rather than selecting just one atom at random.

\begin{align*}
\text{begin} \\
- \text{initialization} \\
\text{let } Pt := \emptyset \\
\text{add.node}(\{t\}, \{a_1, \ldots, a_n\}) \quad - \text{final node of } Pt \text{ is node } 0 \quad (1) \\
\text{for (each } v \in V \text{) begin} \\
\quad \text{add.node}(\{v\}, \{} \) \quad - \text{one node for each input stream} \quad (2) \\
\text{endfor} \\
\text{let } USED := \{ \} \quad - \text{set of node permutation sets which have been evaluated} \quad (3) \\
\text{let } continue := \text{true} \quad - \text{insure one pass through while loop} \quad (4)
\end{align*}

- main algorithm

\begin{align*}
\text{while (continue) begin} \\
\text{continue := false} \\
- \text{Node.set denotes a set of node numbers such as } \{1, 3, 5\}, \text{i.e., a permutation} \\
\text{for (each Node.set } \in \text{ (ENUM(max.node()) } \setminus \text{ USED)) begin} \\
\quad \text{let } USED := USED \cup \text{Node.set} \\
\quad - n \text{ denotes a node number in Node.set} \\
\quad - n.\text{Vars denotes the variables field of } Pt \text{ node } n \\
\quad - n.\text{Atoms denotes the atoms field of } Pt \text{ node } n \\
\quad \text{let } U.\text{atoms} := \{ a \mid \exists n \in \text{Node.set} \land a \in n.\text{Atoms} \} \quad - \text{atom union} \quad (5) \\
\quad \text{let } U.\text{vars} := \{ v \mid \exists n \in \text{Node.set} \land v \in n.\text{Vars} \} \quad - \text{variable union} \quad (6) \\
\quad \text{let } L.\text{vars} := \{ v \mid \forall n \in \text{Node.set} \Rightarrow v \in n.\text{Vars} \} \quad - \text{var intersection} \quad (7)
\end{align*}

\begin{align*}
\text{if ( } \forall n_1, n_2 \in \text{Node.set}, (n_1.\text{Vars }\cap \text{n}_2.\text{Vars} = \emptyset) \text{ then} \\
- \text{no two nodes in Node.set have any variables in common} \\
\quad \text{let } \text{Atoms.to.consume} := \text{FindConsumableAtoms(U.vars, U.atoms)} \quad (8) \\
\text{for (each } a \in \text{Atoms.to.consume) begin} \\
\quad \text{let } R.\text{vars} := \text{Retained.vars(U.vars, U.atoms } \cup \text{ a)} \quad (9) \\
\quad \text{if } (\text{to.node := exists.node(R.\text{vars}, (U.\text{atoms } \cup \text{ a}))} = -1) \text{ then} \\
\quad \quad \text{let } \text{to.node} := \text{add.node(R.\text{vars}, (U.\text{atoms } \cup \text{ a)}))} \quad (10) \\
\quad \quad \text{let } continue := \text{true} \quad (11) \\
\quad \text{endif} \\
\quad \text{connect(Node.set, to.node, OMextend : a)} \quad (12) \\
\quad \text{endfor} \\
\text{endif} \\
\text{if (L.\text{vars} } \neq \emptyset \text{ then} \\
- \text{there are variables common to all input streams} \\
\text{if ( } \forall a \in U.\text{atoms}(\exists n \in \text{Node.set} \mid a \in n) \text{ then} \\
- \text{each node contributes at least one new element to U.atoms} \\
\quad \text{let } R.\text{vars} := \text{Retained.vars(U.vars, U.atoms)} \quad (13) \\
\text{endif}
\end{align*}

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\[
\text{if } ((\text{to\_node} := \text{exists\_node}(R_{\text{vars}}, U_{\text{atoms}})) = -1) \text{ then} \\
\text{let } \text{to\_node} := \text{add\_node}(R_{\text{vars}}, U_{\text{atoms}}) \\
\text{let } \text{continue} := \text{true} \\
\text{endif} \\
\text{connect(Node\_set, to\_node, OM_0)} \\
\text{endif} \\
\text{endfor} \\
\text{endwhile} \\
\text{end Algorithm 5.1}
\]

6 Discussion

There are a number of issues related to the approach that we have taken and related to the scope of our investigation that we would briefly like to touch upon. These issues involve the selection of the “optimum” execution plan and the optimization of the method executions.

6.1 Choosing the “Optimum” Plan

Output of the enumeration algorithm described above is a processing template which identifies a family of logically equivalent query execution plans. Each connected subtree of edges in the processing template which includes all initial nodes and the final node is a valid plan. But which is the best plan?

Section 3 defined an object manager interface but our research does not address its implementation. An implementation design would be highly dependent on the object representation, the technique used to bind method code to objects and other system parameters. Thus, although we do not propose a specific cost function, we assume that the object manager is capable of using oid-stream statistics to derive a cost for calls to its interface.

Appropriate oid-stream statistics might be stream cardinality and information about the classes represented in the stream. For a given call, the object manager could derive a processing cost and statistics for the resulting output oid-stream. A processing template could then be annotated with cost information as follows.

Initially only leaf nodes (which are stream nodes) of the processing template would have stream statistics associated with them. If the leaf nodes correspond to the leaf nodes of the original object algebra query, then they represent the extent or deep extent of classes in the database and their statistics are readily available. Otherwise the leaf nodes represent the output of a previous subtree
of object manager calls and the output old-stream statistics of the appropriate subtree are attached.

Working from leaf to root in the processing template, the object manager cost function is used to assign a processing cost to each operator node as well as a set of stream statistics for the stream node the operator feeds into. All operator nodes and stream nodes in the processing template can be annotated with cost and statistical information in this fashion. The total cost of any specific execution plan within the processing template is the sum of the operator costs which are included in the execution plan’s subgraph. If time information is included in the cost function, then when operator nodes execute in parallel, only the longest running operator should be included in the sum.

Note that cost information can not be used to prune the search space of the processing template generation algorithm. The search space of the algorithm is defined by the number of stream nodes present in the processing template at the start of each pass. This value can only be affected by the criteria used to define the “interesting permutations” which cause new operator and stream nodes to be created.

6.2 Optimization of method executions.

Our research concentrates primarily on the optimization of query primitives. Ideally, query optimization should be possible for queries which utilize user defined methods. But this is highly dependent on the language used to define those methods. In the worst case, the only optimizations possible are those provided by the compiler of the method implementation language. Examples of such optimizations are inline subroutine expansion, removal of loop invariants and efficient pipeline and register usage.

One approach assumes that behavioral abstraction is maintained at the logical level, while a structural object-oriented system exists at the lowest implementation level [13]. Objects and classes involved in a query are requested to reveal structural information by the query processor. Revealed expressions which still contain encapsulated behavior are recursively requested to reveal their equivalent (sequence of) structural expressions. When the revealing process bottoms out, the structural manipulation primitives are optimized by an extended relational query optimizer.

Another approach would be to use a purely functional language for user defined methods. Expressions in such languages can be recursively decomposed to sequences of primitive data manipulation operations. These decomposed sequences can then be optimized using the techniques described earlier. Finally, if methods are written in the query language supported by the system
(as in Postgres [31]) then their optimization can be handled within the same framework as the user queries.

Clearly, optimization of user defined methods is closely tied to the ability to reason about expressions in the method implementation language and is a significant area for future research.

7 Conclusion

This paper investigates the problem of generating execution plans for queries against object-oriented data management systems. Two primary topics were developed: (1) what interface should an object subsystem provide for efficient execution of queries, and (2) how to translate object algebra expressions into execution plans which consist of calls to the object subsystem interface.

Most of the object subsystems proposed to date provide the ability to apply methods and extract subcomponents for single objects only. However, processing queries efficiently requires that similar operations be applied to streams of objects. The object manager interface proposed in this paper does just this. Execution plans are represented as trees of object manager operations whose edges denote the flow of oid-streams.

The overall strategy for generating an execution plan consists of mapping each individual algebra operator in a tree of algebra operators to a subtree of functionally equivalent object manager calls. Algorithms are developed to perform this mapping for each of the five primary object algebra operators: union, difference, select, map, and generate.

While the mapping process for the union, difference, and map operators is primarily one-to-one, the mapping for the select and generate operations is one-to-many. A variant of the join template [24], which we term the *processing template*, is developed and used to represent the many subtrees of object manager calls which are logically equivalent to a single select or generate operation. An algorithm to derive the processing template is presented along with a discussion of how to use object manager cost functions to pick the best plan.

The execution plan generation method proposed in this paper introduces some interesting questions related to query optimization. Equivalence preserving transformation rules for logical optimization of object algebra expressions are derived in [34]. The execution plan generation scheme proposed here assumes that these rules have been used to ameliorate the original object algebra query prior to plan generation. Plan generation then replaces each individual algebra operator with a "best" subtree of object manager calls. In other words, the overall shape of the query tree
remains the same as that which was arrived at during logical optimization. One area of future research indicated by this methodology is the development of equivalence preserving rewrite rules for trees of object manager operations. Such rules would allow global optimization of the entire execution plan as opposed to merely picking “best” subtrees. Another interesting topic would be to develop an execution plan generation strategy which cycles back and forth between the logical algebra optimization phase and the execution plan generation phase. This would allow interleaving transformations which change the shape of the query with the introduction of execution plan subtrees possibly resulting in more efficient plans.

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References


Figure 1: Query processing methodology
Figure 2: Composition of method applications.
Figure 3: Sample database schema.
Figure 4: Mapping object algebra expression trees to object manager operation trees.
Figure 5: Execution plan generation for a sample map operation.
Plan 1

OM_{eval}([o, p, q, r], [p], <p, q, r>, m_1, o == res)

OM_{eval}([o, p, q, r, s], [o, p, q, r], <s>, m_2, q == res)

OM_{eval}([o, p, q, r, s, t], [o, p, q, r, s], φ, q ∈ t)

Plan 2

OM_{eval}([q], [o], [p], [r], [p], <p, q, r>, m_1, o == res)

OM_{eval}([q], [t], [q], φ, q ∈ t)

OM_{eval}([s], [q], <s>, m_2, q == res)

Plan 3

OM_{eval}([q], [o], [p], [r], [p], <p, q, r>, m_1, o == res)

OM_{eval}([q], [s], [q], <s>, m_2, q == res)

OM_{eval}([t], [q], φ, q ∈ t)

Figure 6: Execution plans for the sample select operation.
Figure 7: More execution plans for the sample select operation.
Figure 8: Building an execution plan using the naïve algorithm.
Figure 9: Processing template for the predicate of Equation 1.
Figure 10: Relationship between a processing template and an execution plan.
Figure 11: Mappings from stream node numbers to variables and atoms.
Figure 12: Extended mappings from stream node numbers to consumable atoms.
Figure 13: Node permutations to eligible atom mappings for pass 2.
Figure 14: Node permutation with replicated variables.