Distributed Database Management Systems

Outline

- Introduction
- Distributed DBMS Architecture
- Distributed Database Design
- Distributed Query Processing
- Distributed Concurrency Control
- Distributed Reliability Protocols
Outline

- Introduction
  - What is a distributed DBMS
  - Problems
  - Current state-of-affairs
- Distributed DBMS Architecture
- Distributed Database Design
- Distributed Query Processing
- Distributed Concurrency Control
- Distributed Reliability Protocols

Motivation

integration ≠ centralization
What is a Distributed Database System?

A distributed database (DDB) is a collection of multiple, *logically interrelated* databases distributed over a *computer network*.

A distributed database management system (D–DBMS) is the software that manages the DDB and provides an access mechanism that makes this distribution *transparent* to the users.

Distributed database system (DDBS) = DDB + D–DBMS

What is not a DDBS?

- A timesharing computer system
- A loosely or tightly coupled multiprocessor system
- A database system which resides at one of the nodes of a network of computers - this is a centralized database on a network node
Centralized DBMS on a Network

Distributed DBMS Environment
Implicit Assumptions

- Data stored at a number of sites ⇒ each site logically consists of a single processor.
- Processors at different sites are interconnected by a computer network ⇒ no multiprocessors ⇒ parallel database systems
- Distributed database is a database, not a collection of files ⇒ data logically related as exhibited in the users’ access patterns ⇒ relational data model
- D-DBMS is a full-fledged DBMS ⇒ not remote file system, not a TP system

Distributed DBMS Promises

1. Transparent management of distributed, fragmented, and replicated data
2. Improved reliability/availability through distributed transactions
3. Improved performance
4. Easier and more economical system expansion
Transparency

- Transparency is the separation of the higher level semantics of a system from the lower level implementation issues.
- Fundamental issue is to provide data independence in the distributed environment
  - Network (distribution) transparency
  - Replication transparency
  - Fragmentation transparency
    - horizontal fragmentation: selection
    - vertical fragmentation: projection
    - hybrid

Example

<table>
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<tr>
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<tr>
<td>E4</td>
<td>Programmer</td>
<td>24000</td>
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</tbody>
</table>
Transparent Access

```
SELECT ENAME, SAL
FROM EMP, ASG, PAY
WHERE DUR > 12
AND EMP.ENO = ASG.ENO
AND PAY.TITLE = EMP.TITLE
```

Distributed Database – User View
Distributed DBMS - Reality

- DBMS Software
- User Query
- User Application
- Communication Subsystem

Potentially Improved Performance

- Proximity of data to its points of use
  - Requires some support for fragmentation and replication
- Parallelism in execution
  - Inter-query parallelism
  - Intra-query parallelism
Parallelism Requirements

- Have as much of the data required by *each* application at the site where the application executes
  - Full replication

- How about updates?
  - Updates to replicated data requires implementation of distributed concurrency control and commit protocols

System Expansion

- Issue is database scaling

- Emergence of microprocessor and workstation technologies
  - Demise of Grosh's law
  - Client-server model of computing

- Data communication cost vs telecommunication cost
Distributed DBMS Issues

- **Distributed Database Design**
  - how to distribute the database
  - replicated & non-replicated database distribution
  - a related problem in directory management

- **Query Processing**
  - convert user transactions to data manipulation instructions
  - optimization problem
  - $\text{min}\{\text{cost} = \text{data transmission} + \text{local processing}\}$
  - general formulation is NP-hard

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Distributed DBMS Issues

- **Concurrency Control**
  - synchronization of concurrent accesses
  - consistency and isolation of transactions' effects
  - deadlock management

- **Reliability**
  - how to make the system resilient to failures
  - atomicity and durability
Relationship Between Issues

Outline

- Introduction
- Distributed DBMS Architecture
  - Distributed Database Design
    - Fragmentation
    - Data Placement
- Distributed Query Processing
- Distributed Concurrency Control
- Distributed Reliability Protocols
Design Problem

- In the general setting:
  - Making decisions about the placement of data and programs across the sites of a computer network as well as possibly designing the network itself.

- In Distributed DBMS, the placement of applications entails
  - placement of the distributed DBMS software; and
  - placement of the applications that run on the database

Distribution Design

- Top-down
  - mostly in designing systems from scratch
  - mostly in homogeneous systems

- Bottom-up
  - when the databases already exist at a number of sites
Top-Down Design

Distribution Design Issues

1. Why fragment at all?
2. How to fragment?
3. How much to fragment?
4. How to test correctness?
5. How to allocate?
6. Information requirements?
Fragmentation

- Can't we just distribute relations?
- What is a reasonable unit of distribution?
  - relation
    - views are subsets of relations ⇒ locality
    - extra communication
  - fragments of relations (sub-relations)
    - concurrent execution of a number of transactions that access different portions of a relation
    - views that cannot be defined on a single fragment will require extra processing
    - semantic data control (especially integrity enforcement) more difficult

Fragmentation Alternatives – Horizontal

**PROJ₁**: projects with budgets less than $200,000

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<td>P2</td>
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<td>135000</td>
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**PROJ₂**: projects with budgets greater than or equal to $200,000

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<td>CAD/CAM</td>
<td>500000</td>
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Fragmentation Alternatives – Vertical

PROJ₁: information about project budgets

PROJ₂: information about project names and locations

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Degree of Fragmentation

finite number of alternatives

finds the suitable level of partitioning within this range
Correctness of Fragmentation

- **Completeness**
  - Decomposition of relation $R$ into fragments $R_1, R_2, ..., R_n$ is complete iff each data item in $R$ can also be found in some $R_i$

- **Reconstruction**
  - If relation $R$ is decomposed into fragments $R_1, R_2, ..., R_n$, then there should exist some relational operator $\nabla$ such that

  $$ R = \nabla_{1 \leq i \leq n} R_i $$

- **Disjointness**
  - If relation $R$ is decomposed into fragments $R_1, R_2, ..., R_n$, and data item $d_i$ is in $R_i$, then $d_i$ should not be in any other fragment $R_k$, ($k \neq j$).

Allocation Alternatives

- **Non-replicated**
  - partitioned: each fragment resides at only one site

- **Replicated**
  - fully replicated: each fragment at each site
  - partially replicated: each fragment at some of the sites

- **Rule of thumb:**

  If \( \text{read - only queries} \geq 1 \) replication is advantageous, otherwise replication may cause problems
Fragmentation

- Horizontal Fragmentation (HF)
  - Primary Horizontal Fragmentation (PHF)
  - Derived Horizontal Fragmentation (DHF)
- Vertical Fragmentation (VF)
- Hybrid Fragmentation (HF)

Primary Horizontal Fragmentation

Definition:

\[ R_j = \sigma_{F_j}(R), \ 1 \leq j \leq w \]

where \( F_j \) is a selection formula.

Therefore,

A horizontal fragment \( R_i \) of relation \( R \) consists of all the tuples of \( R \) which satisfy a predicate \( p_i \).

\[ \downarrow \]

Given a set of predicates \( M \), there are as many horizontal fragments of relation \( R \) as there are predicates.
PHF – Example

Two candidate relations: PAY and PROJ

### PAY 

<table>
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<td>Programmer</td>
<td>24000</td>
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### PAY 

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<tr>
<td>Syst. Anal.</td>
<td>34000</td>
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</table>
PHF – Example

\[
\begin{array}{c|c|c|c}
\text{PNO} & \text{PNAME} & \text{BUDGET} & \text{LOC} \\
\hline
\text{P1} & \text{Instrumentation} & 150000 & \text{Montreal} \\
\text{P2} & \text{Database Develop.} & 135000 & \text{New York} \\
\text{P3} & \text{CAD/CAM} & 250000 & \text{New York} \\
\text{P4} & \text{Maintenance} & 310000 & \text{Paris} \\
\end{array}
\]

PHF – Correctness

- **Completeness**
  - Since the set of predicates is complete and minimal, the selection predicates are complete.

- **Reconstruction**
  - If relation \( R \) is fragmented into \( F_R = \{R_1, R_2, \ldots, R_r \} \)
    
    \[
    R = \bigcup_{i \in F_R} R_i
    \]

- **Disjointness**
  - Predicates that form the basis of fragmentation should be mutually exclusive.
Derived Horizontal Fragmentation

- Defined on a member relation of a link according to a selection operation specified on its owner.
  - Each link is an equijoin.
  - Equijoin can be implemented by means of semijoins.

DHF – Definition

Given a link $L$ where $\text{owner}(L) = S$ and $\text{member}(L) = R$, the derived horizontal fragments of $R$ are defined as

$$R_i = R \bowtie_{F_i} S, 1 \leq i \leq w$$

where $w$ is the maximum number of fragments that will be defined on $R$ and

$$S_i = \sigma_{F_i}(S)$$

where $F_i$ is the formula according to which the primary horizontal fragment $S_i$ is defined.
DHF – Example

Given link $L_1$ where owner($L_1$) = SKILL and member($L_1$) = EMP

$\text{EMP}_1 = \text{EMP} \bowtie \text{SKILL}_1$

$\text{EMP}_2 = \text{EMP} \bowtie \text{SKILL}_2$

where

$\text{SKILL}_1 = \sigma_{\text{SAL} \leq 30000} (\text{SKILL})$

$\text{SKILL}_2 = \sigma_{\text{SAL} > 30000} (\text{SKILL})$

<table>
<thead>
<tr>
<th>ENO</th>
<th>ENAME</th>
<th>TITLE</th>
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<tbody>
<tr>
<td>E4</td>
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| E1  | J. Doe    | Elect. Eng.
| E2  | M. Smith  | Syst. Anal.
| E5  | B. Casey  | Syst. Anal.
| E8  | J. Jones  | Syst. Anal.

DHF – Correctness

- **Completeness**
  - Referential integrity
  - Let $R$ be the member relation of a link whose owner is relation $S$ which is fragmented as $F_S = \{S_1, S_2, \ldots, S_n\}$. Furthermore, let $A$ be the join attribute between $R$ and $S$. Then, for each tuple $t$ of $R$, there should be a tuple $t'$ of $S$ such that $t[A] = t'[A]$

- **Reconstruction**
  - Same as primary horizontal fragmentation.

- **Disjointness**
  - Simple join graphs between the owner and the member fragments.
Vertical Fragmentation

- Has been studied within the centralized context
  - design methodology
  - physical clustering
- More difficult than horizontal, because more alternatives exist.
  Two approaches:
  - grouping
    - attributes to fragments
  - splitting
    - relation to fragments

Vertical Fragmentation

- Overlapping fragments
  - grouping
- Non-overlapping fragments
  - splitting
    - We do not consider the replicated key attributes to be overlapping.
- Advantage:
  - Easier to enforce functional dependencies (for integrity checking etc.)
VF – Correctness

A relation $R$, defined over attribute set $A$ and key $K$, generates the vertical partitioning $F_R = \{R_1, R_2, \ldots, R_r\}$.

- **Completeness**
  - The following should be true for $A$:
    \[ A = \bigcup A_{R_i} \]

- **Reconstruction**
  - Reconstruction can be achieved by
    \[ R = \bowtie_K R_i \forall R_i \in F_R \]

- **Disjointness**
  - TID's are not considered to be overlapping since they are maintained by the system
  - Duplicated keys are not considered to be overlapping

Fragment Allocation

- **Problem Statement**
  - Given
    \[ F = \{F_1, F_2, \ldots, F_n\} \quad \text{fragments}\]
    \[ S = \{S_1, S_2, \ldots, S_m\} \quad \text{network sites}\]
    \[ Q = \{q_1, q_2, \ldots, q_q\} \quad \text{applications}\]
  - Find the "optimal" distribution of $F$ to $S$.

- **Optimality**
  - Minimal cost
    - Communication + storage + processing (read & update)
    - Cost in terms of time (usually)
  - Performance
    - Response time and/or throughput
  - Constraints
    - Per site constraints (storage & processing)
Allocation Model

General Form
\[
\min (\text{Total Cost}) \\
\text{subject to} \\
\text{response time constraint} \\
\text{storage constraint} \\
\text{processing constraint}
\]

Decision Variable
\[
x_{ij} = \begin{cases} 
1 & \text{if fragment } F_i \text{ is stored at site } S_j \\
0 & \text{otherwise}
\end{cases}
\]

Total Cost
\[
\sum_{\text{all queries}} \text{query processing cost} + \\
\sum_{\text{all sites}} \sum_{\text{all fragments}} \text{cost of storing a fragment at a site}
\]

Storage Cost (of fragment \( F_j \) at \( S_k \))
\[
(\text{unit storage cost at } S_k) \times (\text{size of } F_j) \times x_{jk}
\]

Query Processing Cost (for one query)
processing component + transmission component
**Allocation Model**

- **Query Processing Cost**
  - **Processing component**
    - access cost + integrity enforcement cost + concurrency control cost
  - **Access cost**
    \[ \sum_{\text{all sites}} \sum_{\text{all fragments}} (\text{no. of update accesses} + \text{no. of read accesses}) \times x_{ij} \times \text{local processing cost at a site} \]
  - **Integrity enforcement and concurrency control costs**
    - Can be similarly calculated

- **Transmission component**
  - cost of processing updates + cost of processing retrievals
  - **Cost of updates**
    \[ \sum_{\text{all sites}} \sum_{\text{all fragments}} \text{update message cost} + \sum_{\text{all sites}} \sum_{\text{all fragments}} \text{acknowledgment cost} \]
  - **Retrieval Cost**
    \[ \sum_{\text{all fragments}} \min_{\text{all sites}} (\text{cost of retrieval command} + \text{cost of sending back the result}) \]
Allocation Model

- Constraints
  - Response Time
    \[ \text{execution time of query} \leq \text{max. allowable response time for that query} \]
  - Storage Constraint (for a site)
    \[ \sum_{\text{all fragments}} \text{storage requirement of a fragment at that site} \leq \text{storage capacity at that site} \]
  - Processing constraint (for a site)
    \[ \sum_{\text{all queries}} \text{processing load of a query at that site} \leq \text{processing capacity of that site} \]

Allocation Model

- Solution Methods
  - FAP is NP-complete
  - DAP also NP-complete

- Heuristics based on
  - single commodity warehouse location (for FAP)
  - knapsack problem
  - branch and bound techniques
  - network flow
Allocation Model

- Attempts to reduce the solution space
  - assume all candidate partitionings known; select the “best” partitioning
  - ignore replication at first
  - sliding window on fragments

Outline

- Introduction
- Distributed DBMS Architecture
- Distributed Database Design
- Distributed Query Processing
  - Query Processing Methodology
  - Distributed Query Optimization
- Distributed Concurrency Control
- Distributed Reliability Protocols
Query Processing

- high level user query
- query processor
- low level data manipulation commands

Query Processing Components

- Query language that is used
  - SQL: “intergalactic dataspeak”
- Query execution methodology
  - The steps that one goes through in executing high-level (declarative) user queries.
- Query optimization
  - How do we determine the “best” execution plan?
Selecting Alternatives

```sql
SELECT ENAME
FROM EMP, ASG
WHERE EMP.ENO = ASG.ENO
AND DUR > 37
```

Strategy 1

\[ \Pi_{\text{ENAME}}(\sigma_{\text{DUR} > 37 \land \text{EMP.ENO} = \text{ASG.ENO}} (\text{EMP} \times \text{ASG})) \]

Strategy 2

\[ \Pi_{\text{ENAME}}(\text{EMP} \bowtie_{\text{ENO}} (\sigma_{\text{DUR} > 37} (\text{ASG}))) \]

Strategy 2 avoids Cartesian product, so is “better”

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What is the Problem?

<table>
<thead>
<tr>
<th>Site 1</th>
<th>Site 2</th>
<th>Site 3</th>
<th>Site 4</th>
<th>Site 5</th>
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</thead>
<tbody>
<tr>
<td>ASG_1 = \sigma_{\text{ENO} \leq \text{E3}(\text{EMP})} (\text{ASG})</td>
<td>ASG_2 = \sigma_{\text{ENO} &gt; \text{E3}(\text{EMP})} (\text{ASG})</td>
<td>EMP_1 = \sigma_{\text{ENO} = \text{E3}(\text{EMP})} (\text{EMP})</td>
<td>EMP_2 = \sigma_{\text{ENO} = \text{E3}(\text{EMP})} (\text{EMP})</td>
<td>Result</td>
</tr>
</tbody>
</table>

Site 5

result = EMP_1 \cup EMP_2

Site 4

result = (EMP_1 \cup EMP_2) \bowtie_{\text{ENO} > \text{DUR} > 37} (\text{ASG} \cup \text{ASG})

Site 1

EMP_1

Site 2

EMP_2

Site 3

ASG_1

Site 4

ASG_2

Site 5

Result

Page 29
Cost of Alternatives

Assume:
- \( \text{size}(\text{EMP}) = 400 \), \( \text{size}(\text{ASG}) = 1000 \)
- tuple access cost = 1 unit; tuple transfer cost = 10 units

Strategy 1
- produce \( \text{ASG}^\prime \): \((10+10)\) tuple access cost = 20
- transfer \( \text{ASG}^\prime \) to the sites of \( \text{EMP} \): \((10+10)\) tuple transfer cost = 200
- produce \( \text{EMP}^\prime \): \((10+10)\) tuple access cost × 2 = 40
- transfer \( \text{EMP}^\prime \) to result site: \((10+10)\) tuple transfer cost = 200
- Total cost = 460

Strategy 2
- transfer \( \text{EMP} \) to site 5: \((400+400)\) tuple transfer cost = 4,000
- transfer \( \text{ASG} \) to site 5: \((1000+1000)\) tuple transfer cost = 10,000
- produce \( \text{ASG}^\prime \): \(1000\) tuple access cost = 1,000
- join \( \text{EMP} \) and \( \text{ASG}^\prime \): \((400+20)\) tuple access cost = 8,000
- Total cost = 23,000

Query Optimization Objectives

Minimize a cost function
- I/O cost + CPU cost + communication cost

These might have different weights in different distributed environments

Wide area networks
- communication cost will dominate
  - low bandwidth
  - low speed
  - high protocol overhead
- most algorithms ignore all other cost components

Local area networks
- communication cost not that dominant
- total cost function should be considered

Can also maximize throughput
Query Optimization Issues – Types of Optimizers

- Exhaustive search
  - cost-based
  - optimal
  - combinatorial complexity in the number of relations

- Heuristics
  - not optimal
  - regroup common sub-expressions
  - perform selection, projection first
  - replace a join by a series of semijoins
  - reorder operations to reduce intermediate relation size
  - optimize individual operations

Query Optimization Issues – Optimization Granularity

- Single query at a time
  - cannot use common intermediate results

- Multiple queries at a time
  - efficient if many similar queries
  - decision space is much larger
Query Optimization Issues – Optimization Timing

- **Static**
  - compilation ⇒ optimize prior to the execution
  - difficult to estimate the size of the intermediate results ⇒ error propagation
  - can amortize over many executions
  - $R^*$

- **Dynamic**
  - run time optimization
  - exact information on the intermediate relation sizes
  - have to reoptimize for multiple executions
  - Distributed INGRES

- **Hybrid**
  - compile using a static algorithm
  - if the error in estimate sizes > threshold, reoptimize at run time
  - MERMAID

Query Optimization Issues – Statistics

- **Relation**
  - cardinality
  - size of a tuple
  - fraction of tuples participating in a join with another relation

- **Attribute**
  - cardinality of domain
  - actual number of distinct values

- **Common assumptions**
  - independence between different attribute values
  - uniform distribution of attribute values within their domain
Query Optimization Issues – Decision Sites

- Centralized
  - single site determines the "best" schedule
  - simple
  - need knowledge about the entire distributed database

- Distributed
  - cooperation among sites to determine the schedule
  - need only local information
  - cost of cooperation

- Hybrid
  - one site determines the global schedule
  - each site optimizes the local subqueries

Query Optimization Issues – Network Topology

- Wide area networks (WAN) – point-to-point
  - characteristics
    - low bandwidth
    - low speed
    - high protocol overhead
  - communication cost will dominate; ignore all other cost factors
  - global schedule to minimize communication cost
  - local schedules according to centralized query optimization

- Local area networks (LAN)
  - communication cost not that dominant
  - total cost function should be considered
  - broadcasting can be exploited (joins)
  - special algorithms exist for star networks
Distributed Query Processing Methodology

Step 1 – Query Decomposition

**Input:** Calculus query on global relations

- **Normalization**
  - manipulate query quantifiers and qualification

- **Analysis**
  - detect and reject “incorrect” queries
  - possible for only a subset of relational calculus

- **Simplification**
  - eliminate redundant predicates

- **Restructuring**
  - calculus query $\Rightarrow$ algebraic query
  - more than one translation is possible
  - use transformation rules
Normalization

- Lexical and syntactic analysis
  - check validity (similar to compilers)
  - check for attributes and relations
  - type checking on the qualification

- Put into normal form
  - Conjunctive normal form
    \[(p_{11} \lor p_{12} \lor \ldots \lor p_{1n}) \land \ldots \land (p_{mn} \lor p_{m2} \lor \ldots \lor p_{mn})\]
  - Disjunctive normal form
    \[(p_{11} \land p_{12} \land \ldots \land p_{1n}) \lor \ldots \lor (p_{mn} \land p_{m2} \land \ldots \land p_{mn})\]

- OR's mapped into union
- AND's mapped into join or selection

Analysis

- Refute incorrect queries
- Type incorrect
  - If any of its attribute or relation names are not defined in the global schema
  - If operations are applied to attributes of the wrong type
- Semantically incorrect
  - Components do not contribute in any way to the generation of the result
  - Only a subset of relational calculus queries can be tested for correctness
  - Those that do not contain disjunction and negation
  - To detect
    - connection graph (query graph)
    - join graph
Simplification

- Why simplify?
  - Remember the example

- How? Use transformation rules
  - elimination of redundancy
    - idempotency rules
      \[ p_1 \land \neg(p_1) \iff \text{false} \]
      \[ p_1 \land (p_1 \lor p_2) \iff p_1 \]
      \[ p_1 \lor \text{false} \iff p_1 \]
      ...
  - application of transitivity
  - use of integrity rules

Simplification – Example

```sql
SELECT TITLE
FROM EMP
WHERE EMP.ENAME = "J. Doe"
OR
  (NOT(EMP.TITLE = "Programmer")
AND
  (EMP.TITLE = "Programmer"
OR
  EMP.TITLE = "Elect. Eng.")
AND
  NOT(EMP.TITLE = "Elect. Eng."))

\downarrow

SELECT TITLE
FROM EMP
WHERE EMP.ENAME = "J. Doe"
```
Restructuring

- Convert relational calculus to relational algebra
- Make use of query trees
- Example

Find the names of employees other than J. Doe who worked on the CAD/CAM project for either 1 or 2 years.

```
SELECT ENAME
FROM EMP, ASG, PROJ
WHERE EMP.ENO = ASG.ENO
AND ASG.PNO = PROJ.PNO
AND ENAME ≠ "J. Doe"
AND PNAME = "CAD/CAM"
AND (DUR = 12 OR DUR = 24)
```

Restructuring – Transformation Rules

- Commutativity of binary operations
  - \( R \times S \Leftrightarrow S \times R \)
  - \( R \bowtie S \Leftrightarrow S \bowtie R \)
  - \( R \cup S \Leftrightarrow S \cup R \)

- Associativity of binary operations
  - \(( R \times S ) \times T \Leftrightarrow R \times ( S \times T ) \)
  - \(( R \bowtie S ) \bowtie T \Leftrightarrow R \bowtie ( S \bowtie T ) \)

- Idempotence of unary operations
  - \( \Pi_{A'}(\Pi_{A}(R)) \Leftrightarrow \Pi_{A}(R) \)
  - \( \sigma_{P_{1}(A_1)}(\sigma_{P_{2}(A_2)}(R)) = \sigma_{P_{1}(A_1) \land P_{2}(A_2)}(R) \)
  - where \( R[A] \) and \( A' \subseteq A \), \( A'' \subseteq A \) and \( A' \subseteq A'' \)

- Commuting selection with projection
Restructuring – Transformation Rules

- Commuting selection with binary operations
  \[ σ_{p(A)}(R \times S) \Leftrightarrow (σ_{p(A)}(R)) \times S \]
  \[ σ_{p(A)}(R \bowtie_{\{A_i,B_k\}} S) \Leftrightarrow (σ_{p(A)}(R)) \bowtie_{\{A_i,B_k\}} S \]
  \[ σ_{p(A)}(R \cup T) \Leftrightarrow σ_{p(A)}(R) \cup σ_{p(A)}(T) \]
  where \( A_i \) belongs to \( R \) and \( T \)

- Commuting projection with binary operations
  \[ π_C(R \times S) \Leftrightarrow π_A(R) \times π_B(S) \]
  \[ π_C(R \bowtie_{\{A_i,B_k\}} S) \Leftrightarrow π_A(R) \bowtie_{\{A_i,B_k\}} π_B(S) \]
  \[ π_C(R \cup S) \Leftrightarrow π_C(R) \cup π_C(S) \]
  where \( R[A] \) and \( S[B] \)

Example

Recall the previous example:
Find the names of employees other than J. Doe who worked on the CAD/CAM project for either one or two years.

```sql
SELECT ENAME
FROM PROJ, ASG, EMP
WHERE ASG.ENO=EMP.ENO
AND ASG.PNO=PROJ.PNO
AND ENAME#“J. Doe”
AND PROJ.PNAME=“CAD/CAM”
AND (DUR=12 OR DUR=24)
```
Equivalent Query

\[ \Pi_{\text{ENAME}} \sigma_{\text{PNAME}=\text{"CAD/CAM"} \land (\text{DUR}=12 \lor \text{DUR}=24) \land \text{ENAME} \neq \text{"J. DOE"}} \]

Restructuring

\[ \Pi_{\text{ENAME}} \]

\[ \sigma_{\text{PNAME}=\text{"CAD/CAM"}} \]

\[ \Pi_{\text{PNO}} \]

\[ \sigma_{\text{DUR} = 12 \land \text{DUR}=24} \]

\[ \Pi_{\text{PNO,ENAME}} \]

\[ \sigma_{\text{ENAME} \neq \text{"J. Doe"}} \]

\[ \Pi_{\text{PNO,ENO}} \]

\[ \Pi_{\text{PNO}} \]

\[ \Pi_{\text{PNO,ENO}} \]

\[ \Pi_{\text{ENO}} \]

\[ \Pi_{\text{PNO}} \]

\[ \Pi_{\text{PNO,ENO}} \]

\[ \Pi_{\text{PNO,ENAME}} \]

\[ \Pi_{\text{EN}} \]

\[ \Pi_{\text{PNO}} \]

\[ \Pi_{\text{PNO,ENO}} \]

\[ \Pi_{\text{PNO,ENAME}} \]

\[ \Pi_{\text{ASG}} \]

\[ \Pi_{\text{EMP}} \]

\[ \Pi_{\text{PROJ}} \]
Step 2 – Data Localization

Input: Algebraic query on distributed relations

- Determine which fragments are involved
- Localization program
  - substitute for each global query its materialization program
  - optimize

Example

Assume

- EMP is fragmented into EMP1, EMP2, EMP3 as follows:
  - EMP1 = σENO ≤ "E3"(EMP)
  - EMP2 = σ"E3"<ENO ≤ "E6"(EMP)
  - EMP3 = σENO ≥ "E6"(EMP)
- ASG fragmented into ASG1 and ASG2 as follows:
  - ASG1 = σENO ≤ "E3"(ASG)
  - ASG2 = σENO > "E3"(ASG)

Replace EMP by (EMP1 ∪ EMP2 ∪ EMP3) and ASG by (ASG1 ∪ ASG2) in any query

\[\Pi_{ENAME} \sigma_{DUR=12 \ OR \ DUR=24} \sigma_{PNAME="CAD/CAM"} \sigma_{ENAME \neq "J. DOE"} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} \sigma_{ENO} 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Provides Parallellism

Eliminates Unnecessary Work
Reduction for PHF

Reduction with selection

- Relation $R$ and $F_R = \{R_1, R_2, \ldots, R_w\}$ where $R_j = \sigma_{p_j}(R)$

$$\sigma_{p_j}(R) = \phi \text{ if } \forall x \in R: (p_j(x) \lor \neg p_j(x))$$

- Example

```
SELECT * FROM EMP WHERE ENO='E5'
```

Reduction for PHF

Reduction with join

- Possible if fragmentation is done on join attribute
- Distribute join over union

$$(R_1 \cup R_2) \bowtie S \iff (R_1 \bowtie S) \cup (R_2 \bowtie S)$$

- Given $R_i = \sigma_{p_i}(R)$ and $R_j = \sigma_{p_j}(R)$

$$R_i \bowtie R_j = \phi \text{ if } \forall x \in R_i \forall y \in R_j: (p_i(x) \lor p_j(y))$$
Reduction for PHF

- Reduction with join - Example
  - Assume EMP is fragmented as before and
    \[ \text{ASG}_1: \sigma_{\text{ENO} \leq "E3"(\text{ASG})} \]
    \[ \text{ASG}_2: \sigma_{\text{ENO} > "E3"(\text{ASG})} \]
  - Consider the query
    \[
    \text{SELECT}^* \\
    \text{FROM} \quad \text{EMP, ASG} \\
    \text{WHERE} \quad \text{EMP.ENO=ASG.ENO}
    \]

Reduction for PHF

- Reduction with join - Example
  - Distribute join over unions
  - Apply the reduction rule
**Reduction for VF**

- Find useless (not empty) intermediate relations

Relation $R$ defined over attributes $A = \{A_1, ..., A_n\}$ vertically fragmented as $R_i = \Pi_{A'}(R)$ where $A' \subseteq A$:

$\Pi_{D,K}(R_i)$ is useless if the set of projection attributes $D$ is not in $A'$

Example: $EMP_1 = \Pi_{ENO,ENAME}(EMP)$; $EMP_2 = \Pi_{ENO,TITLE}(EMP)$

```
SELECT ENAME
FROM EMP
```

**Step 3 – Global Query Optimization**

**Input:** Fragment query

- Find the **best** (not necessarily optimal) global schedule
  
  - Minimize a cost function
  
  - Distributed join processing
    - Bushy vs. linear trees
    - Which relation to ship where?
    - Ship-whole vs ship-as-needed
  
  - Decide on the use of semijoins
    - Semijoin saves on communication at the expense of more local processing.
  
  - Join methods
    - nested loop vs ordered joins (merge join or hash join)
## Cost-Based Optimization

- **Solution space**
  - The set of equivalent algebra expressions (query trees).

- **Cost function (in terms of time)**
  - I/O cost + CPU cost + communication cost
  - These might have different weights in different distributed environments (LAN vs WAN).
  - Can also maximize throughput

- **Search algorithm**
  - How do we move inside the solution space?
  - Exhaustive search, heuristic algorithms (iterative improvement, simulated annealing, genetic, …)

---

### Query Optimization Process

```
Input Query → Search Space Generation → Equivalent QEP → Search Strategy → Best QEP
```

- **Search Space Generation**
- **Equivalent QEP**
- **Search Strategy**
- **Best QEP**

- **Transformation Rules**
- **Cost Model**
Search Space

- Search space characterized by alternative execution plans
- Focus on join trees
- For $N$ relations, there are $O(N!)$ equivalent join trees that can be obtained by applying commutativity and associativity rules

```sql
SELECT ENAME, RESP
FROM EMP, ASG, PROJ
WHERE EMP.ENO=ASG.ENO
AND ASG.PNO=PROJ.PNO
```

- Restrict by means of heuristics
  - Perform unary operations before binary operations
  - ...
- Restrict the shape of the join tree
  - Consider only linear trees, ignore bushy ones
Search Strategy

- How to “move” in the search space.
- Deterministic
  - Start from base relations and build plans by adding one relation at each step
  - Dynamic programming: breadth-first
  - Greedy: depth-first
- Randomized
  - Search for optimalities around a particular starting point
  - Trade optimization time for execution time
  - Better when > 5-6 relations
  - Simulated annealing
  - Iterative improvement

Search Strategies

- Deterministic

```
R_1  R_2  R_3  R_4
```

- Randomized

```
R_1  R_2  R_3  R_2
```

```
R_1  R_3  R_1  R_3
```
Cost Functions

- **Total Time (or Total Cost)**
  - Reduce each cost (in terms of time) component individually
  - Do as little of each cost component as possible
  - Optimizes the utilization of the resources
  
    \[ \text{Increases system throughput} \]

- **Response Time**
  - Do as many things as possible in parallel
  - May increase total time because of increased total activity

---

Total Cost

Summation of all cost factors

\[
\text{Total cost} = \text{CPU cost} + \text{I/O cost} + \text{communication cost}
\]

- CPU cost = unit instruction cost \(\times\) no. of instructions
- I/O cost = unit disk I/O cost \(\times\) no. of disk I/Os
- communication cost = message initiation + transmission
Total Cost Factors

- Wide area network
  - message initiation and transmission costs high
  - local processing cost is low (fast mainframes or minicomputers)
  - ratio of communication to I/O costs = 20:1

- Local area networks
  - communication and local processing costs are more or less equal
  - ratio = 1:1.6

Response Time

Elapsed time between the initiation and the completion of a query

\[
\text{Response time} = \text{CPU time} + \text{I/O time} + \text{communication time}
\]

CPU time = unit instruction time \* no. of sequential instructions

I/O time = unit I/O time \* no. of sequential I/Os

Communication time = \( \frac{\text{unit msg initiation time} \times \text{no. of sequential msg}}{\text{unit transmission time} \times \text{no. of sequential bytes}} \)
Example

Assume that only the communication cost is considered

Total time = 2 * message initialization time + unit transmission time * (x+y)

Response time = max {time to send x from 1 to 3, time to send y from 2 to 3}

time to send x from 1 to 3 = message initialization time + unit transmission time * x

time to send y from 2 to 3 = message initialization time + unit transmission time * y

Optimization Statistics

- Primary cost factor: size of intermediate relations
- Make them precise ⇒ more costly to maintain
  - For each relation $R[A_1, A_2, ..., A_n]$ fragmented as $R_1, ..., R_r$
    - length of each attribute: $\text{length}(A_i)$
    - the number of distinct values for each attribute in each fragment: $\text{card}(\Pi_{A_i} R_j)$
    - maximum and minimum values in the domain of each attribute: $\text{min}(A_i), \text{max}(A_i)$
    - the cardinalities of each domain: $\text{card}(\text{dom}[A_i])$
    - the cardinalities of each fragment: $\text{card}(R_j)$
  - Selectivity factor of each operation for relations
    - For joins

$$SF_\bowtie(R, S) = \frac{\text{card}(R \bowtie S)}{\text{card}(R) \cdot \text{card}(S)}$$
Intermediate Relation Sizes

Selection

\[ size(R) = \text{card}(R) \times \text{length}(R) \]
\[ \text{card}(\sigma_F(R)) = SF_{\sigma}(F) \times \text{card}(R) \]

where

\[ SF_{\sigma}(A = \text{value}) = \frac{1}{\text{card}(\prod A(R))} \]
\[ SF_{\sigma}(A > \text{value}) = \frac{\text{max}(A) - \text{value}}{\text{max}(A) - \text{min}(A)} \]
\[ SF_{\sigma}(A < \text{value}) = \frac{\text{value} - \text{max}(A)}{\text{max}(A) - \text{min}(A)} \]

\[ SF_{\sigma}(p(A_i) \land p(A_j)) = SF_{\sigma}(p(A_i)) \times SF_{\sigma}(p(A_j)) \]
\[ SF_{\sigma}(p(A_i) \lor p(A_j)) = SF_{\sigma}(p(A_i)) + SF_{\sigma}(p(A_j)) - (SF_{\sigma}(p(A_i)) \times SF_{\sigma}(p(A_j))) \]
\[ SF_{\sigma}(A \in \text{value}) = SF_{\sigma}(A = \text{value}) \times \text{card}\{\text{values}\} \]

Intermediate Relation Sizes

Projection

\[ \text{card}(\Pi_A(R)) = \text{card}(R) \]

Cartesian Product

\[ \text{card}(R \times S) = \text{card}(R) \times \text{card}(S) \]

Union

upper bound: \[ \text{card}(R \cup S) = \text{card}(R) + \text{card}(S) \]
lower bound: \[ \text{card}(R \cup S) = \max\{\text{card}(R), \text{card}(S)\} \]

Set Difference

upper bound: \[ \text{card}(R - S) = \text{card}(R) \]
lower bound: 0
Intermediate Relation Size

Join

- Special case: $A$ is a key of $R$ and $B$ is a foreign key of $S$;
  \[ \text{card}(R \bowtie_{A=B} S) = \text{card}(S) \]

- More general:
  \[ \text{card}(R \bowtie S) = SF_{R} \circ \text{card}(R) \circ \text{card}(S) \]

Semijoin

\[ \text{card}(R \bowtie_{A} S) = SF_{R} (S.A) \circ \text{card}(R) \]

where
\[ SF_{R} (R \bowtie_{A} S) = SF_{R} (S.A) = \frac{\text{card}(\prod_{A}(S))}{\text{card(dom}[A])] \]

System R Algorithm

1. Simple (i.e., mono-relation) queries are executed according to the best access path

2. Execute joins
   2.1 Determine the possible ordering of joins
   2.2 Determine the cost of each ordering
   2.3 Choose the join ordering with minimal cost
System R Algorithm

For joins, two alternative algorithms:

- Nested loops
  
  for each tuple of external relation (cardinality $n_1$)
  
  for each tuple of internal relation (cardinality $n_2$)
  
  join two tuples if the join predicate is true
  
  end
  
  end
  
  Complexity: $n_1 \cdot n_2$

- Merge join

  sort relations
  
  merge relations
  
  Complexity: $n_1 + n_2$ if relations are previously sorted and equijoin

System R Algorithm – Example

Names of employees working on the CAD/CAM project

Assume

- EMP has an index on ENO,
- ASG has an index on PNO,
- PROJ has an index on PNO and an index on PNAME
System R Example (cont’d)

1. Choose the best access paths to each relation
   - EMP: sequential scan (no selection on EMP)
   - ASG: sequential scan (no selection on ASG)
   - PROJ: index on PNAME (there is a selection on PROJ based on PNAME)

2. Determine the best join ordering
   - EMP △ ASG △ PROJ
   - ASG △ PROJ △ EMP
   - PROJ △ ASG △ EMP
   - ASG △ EMP △ PROJ
   - EMP × PROJ △ ASG
   - PROJ × EMP △ ASG
   - Select the best ordering based on the join costs evaluated according to the two methods

System R Algorithm

Alternatives

Best total join order is one of
- ((ASG △ EMP) △ PROJ)
- ((PROJ △ ASG) △ EMP)
System R Algorithm

- \(((\text{PROJ} \bowtie \text{ASG}) \bowtie \text{EMP})\) has a useful index on the select attribute and direct access to the join attributes of ASG and EMP.

- Therefore, chose it with the following access methods:
  - select PROJ using index on PNAME
  - then join with ASG using index on PNO
  - then join with EMP using index on ENO

Join Ordering in Fragment Queries

- Ordering joins
  - Distributed INGRES
  - System R*

- Semijoin ordering
  - SDD-1
Join Ordering

Consider two relations only

If \( \text{size}(R) < \text{size}(S) \),
\[ R \rightarrow S \]

If \( \text{size}(R) > \text{size}(S) \),
\[ S \rightarrow R \]

Multiple relations more difficult because too many alternatives.
- Compute the cost of all alternatives and select the best one.
- Necessary to compute the size of intermediate relations which is difficult.
- Use heuristics

Join Ordering – Example

Consider
\[ \text{PROJ} \Join_{\text{PNO}} \text{ASG} \Join_{\text{ENO}} \text{EMP} \]
Join Ordering – Example

Execution alternatives:

1. EMP → Site 2
   Site 2 computes EMP'=EMP><ASG
   EMP' → Site 3
   Site 3 computes EMP><d PROJ

2. ASG → Site 1
   Site 1 computes EMP=EMP><ASG
   EMP' → Site 3
   Site 3 computes EMP><<PROJ

3. ASG → Site 3
   Site 3 computes ASG'=ASG>=d PROJ
   ASG' → Site 1
   Site 1 computes ASG><<EMP

4. PROJ → Site 2
   Site 2 computes PROJ'=PROJ><ASG
   PROJ' → Site 1
   Site 1 computes PROJ><<EMP

5. EMP → Site 2
   PROJ → Site 2
   Site 2 computes EMP><d PROJ >><ASG

Semijoin Algorithms

- Consider the join of two relations:
  - R[A] (located at site 1)
  - S[A] (located at site 2)

- Alternatives:
  1. Do the join R▷< A S
  2. Perform one of the semijoin equivalents
     \[ R▷< A S \leftrightarrow (R▷< A S)▷< A S \]
     \[ \leftrightarrow R▷< A (S▷< A R) \]
     \[ \leftrightarrow (R▷< A S)▷< A (S▷< A R) \]
Semijoin Algorithms

- Perform the join
  - send $R$ to Site 2
  - Site 2 computes $R \bowtie_A S$

- Consider semijoin $(R \bowtie_A S) \bowtie_A S$
  - $S' \leftarrow \Pi_A(S)$
  - $S' \rightarrow$ Site 1
  - Site 1 computes $R' = R \bowtie_A S'$
  - $R' \rightarrow$ Site 2
  - Site 2 computes $R' \bowtie_A S$

Semijoin is better if
\[
\text{size}(\Pi_A(S)) + \text{size}(R \bowtie_A S) < \text{size}(R)
\]

Distributed Query Processing

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<td>Dist. INGRES</td>
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<td>Msg. Size, Proc. Cost</td>
<td>General or Broadcast</td>
<td>No</td>
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<td>Horizontal</td>
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<tr>
<td>R*</td>
<td>Static Total time</td>
<td>No, Msg., Msg. Size, IO, CPU</td>
<td>General or Local</td>
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<td>1, 2</td>
<td>No</td>
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<tr>
<td>SDD-1</td>
<td>Static Total time</td>
<td>Msg. Size</td>
<td>General</td>
<td>Yes</td>
<td>1, 3, 4, 5</td>
<td>No</td>
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</tr>
</tbody>
</table>

1: relation cardinality; 2: number of unique values per attribute; 3: join selectivity factor; 4: size of projection on each join attribute; 5: attribute size and tuple size
R* Algorithm

- Cost function includes local processing as well as transmission
- Considers only joins
- Exhaustive search
- Compilation
- Published papers provide solutions to handling horizontal and vertical fragmentations but the implemented prototype does not

R* Algorithm

Performing joins
- Ship whole
  - larger data transfer
  - smaller number of messages
  - better if relations are small
- Fetch as needed
  - number of messages = \( O(\text{cardinality of external relation}) \)
  - data transfer per message is minimal
  - better if relations are large and the selectivity is good
**R* Algorithm – Vertical Partitioning & Joins**

1. Move outer relation tuples to the site of the inner relation
   
   (a) Retrieve outer tuples
   (b) Send them to the inner relation site
   (c) Join them as they arrive

   \[
   \text{Total Cost} = \text{cost}(\text{retrieving qualified outer tuples}) + \text{no. of outer tuples fetched} \times \text{cost}(\text{retrieving qualified inner tuples}) + \text{msg. cost} \times \left(\text{no. outer tuples fetched} \times \frac{\text{avg. outer tuple size}}{\text{msg. size}}\right)
   \]

2. Move inner relation to the site of outer relation

   cannot join as they arrive; they need to be stored

   \[
   \text{Total Cost} = \text{cost}(\text{retrieving qualified outer tuples}) + \text{no. of outer tuples fetched} \times \text{cost}(\text{retrieving matching inner tuples from temporary storage}) + \text{cost}(\text{retrieving qualified inner tuples}) + \text{cost}(\text{storing all qualified inner tuples in temporary storage}) + \text{msg. cost} \times \left(\text{no. inner tuples fetched} \times \frac{\text{avg. inner tuple size}}{\text{msg. size}}\right)
   \]
3. Move both inner and outer relations to another site

Total cost = cost(retrieving qualified outer tuples) + cost(retrieving qualified inner tuples) + cost(storing inner tuples in storage) + msg. cost \( \times \) (no. of outer tuples fetched \( \times \) avg. outer tuple size) / msg. size + msg. cost \( \times \) (no. of inner tuples fetched \( \times \) avg. inner tuple size) / msg. size + no. of outer tuples fetched \times\) cost(retrieving inner tuples from temporary storage)

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4. Fetch inner tuples as needed

(a) Retrieve qualified tuples at outer relation site
(b) Send request containing join column value(s) for outer tuples to inner relation site
(c) Retrieve matching inner tuples at inner relation site
(d) Send the matching inner tuples to outer relation site
(e) Join as they arrive

Total Cost = cost(retrieving qualified outer tuples) + msg. cost \( \times \) (no. of outer tuples fetched) + no. of outer tuples fetched \times\) (no. of inner tuples fetched \( \times\) avg. inner tuple size \( \times \) msg. cost / msg. size) + no. of outer tuples fetched \times\) cost(retrieving matching inner tuples for one outer value)
Step 4 – Local Optimization

**Input:** Best global execution schedule

- Select the best *access path*
- Use the centralized optimization techniques