

# Progressive Photon Mapping Extensions

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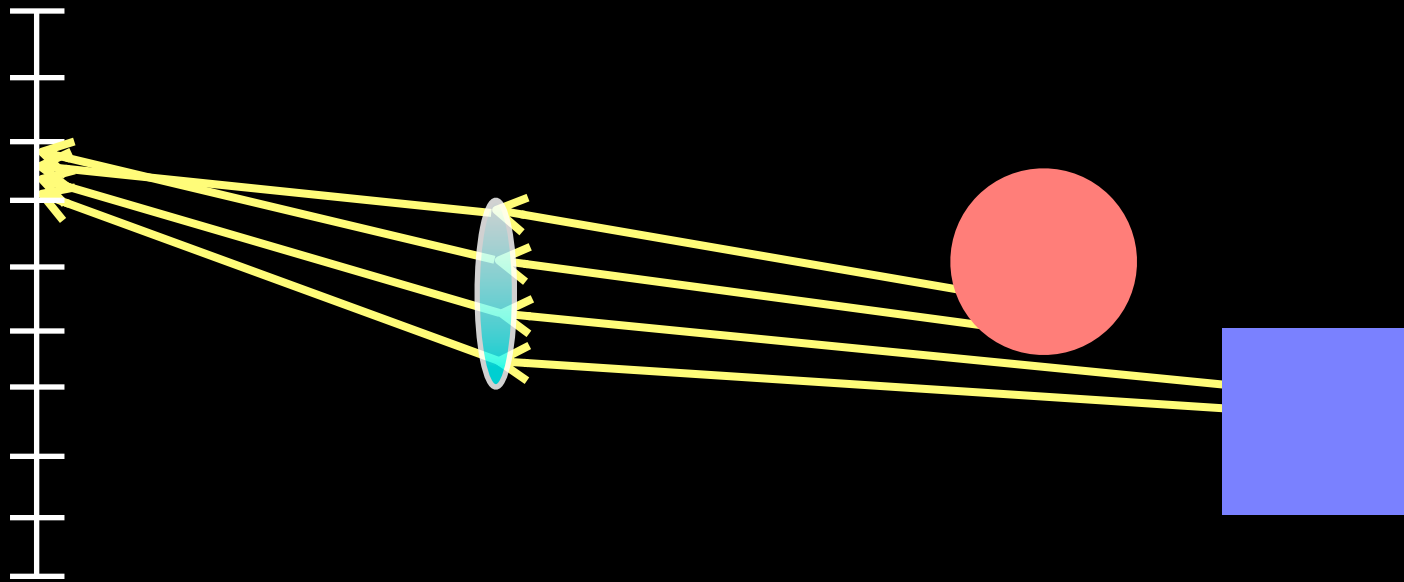
State of the Art in Photon Density Estimation  
SIGGRAPH 2012 Course



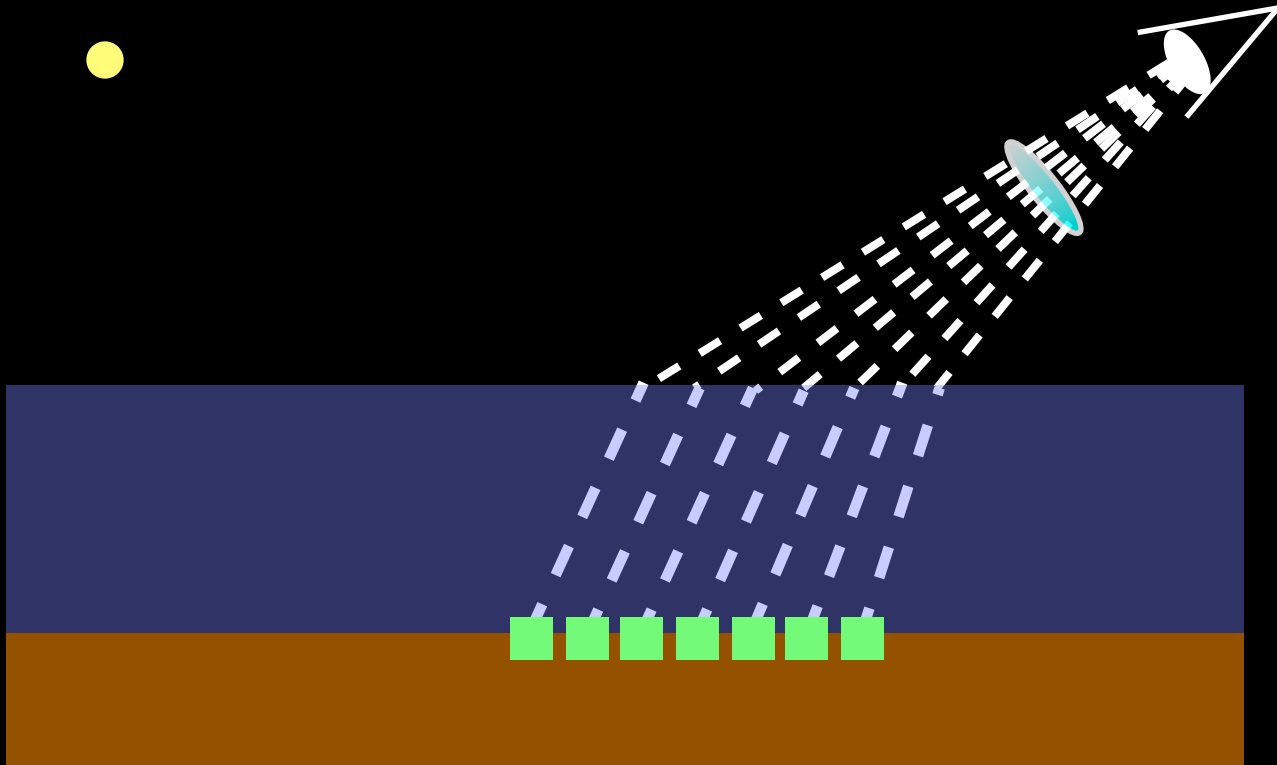


# Distributed Ray Tracing

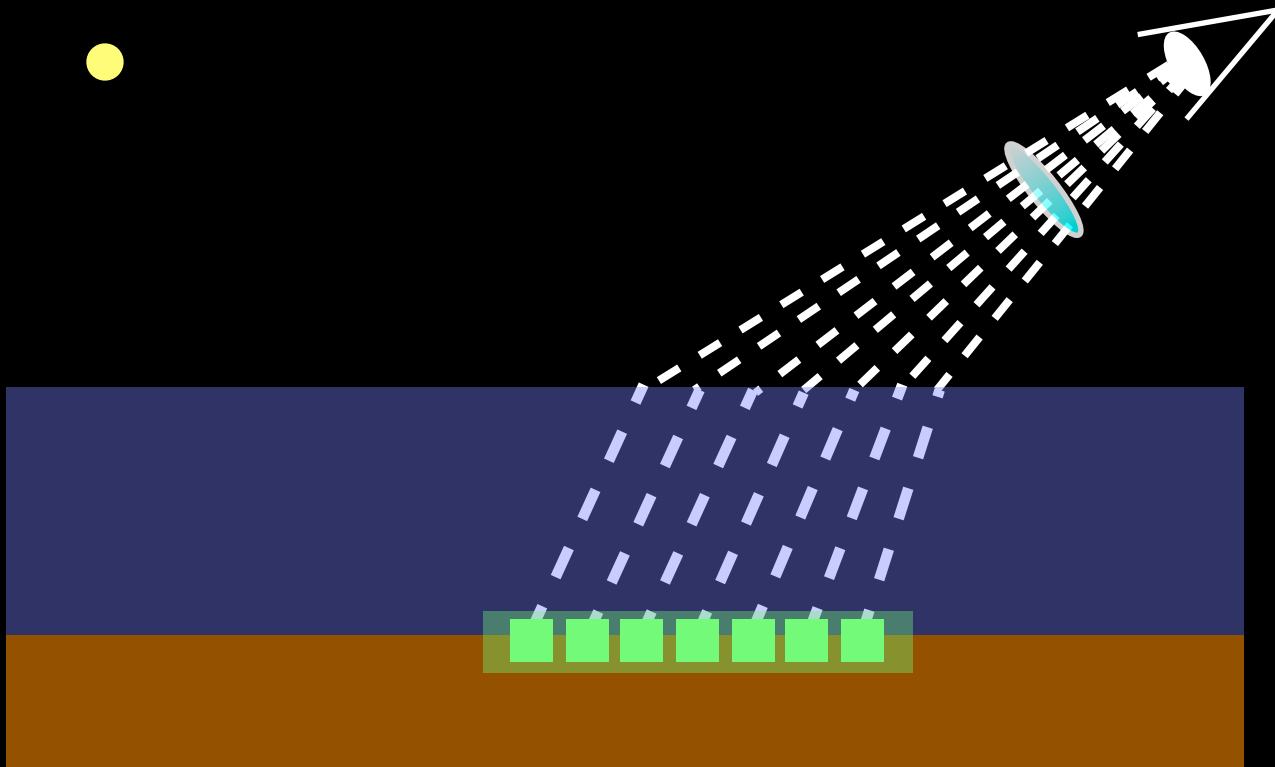
- Computes average illumination [Cook et al. 84]



# Lens Simulation with PPM



# Lens Simulation with PPM



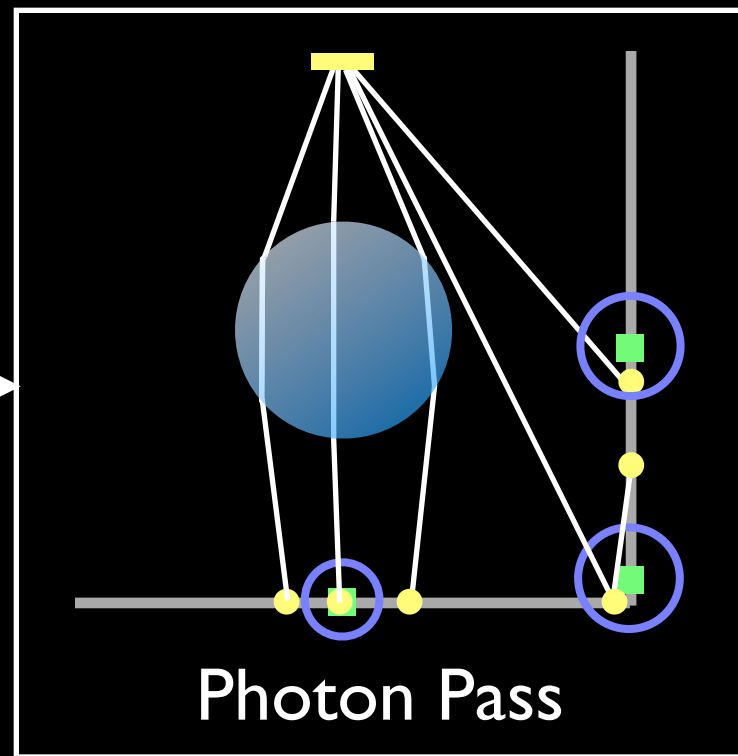
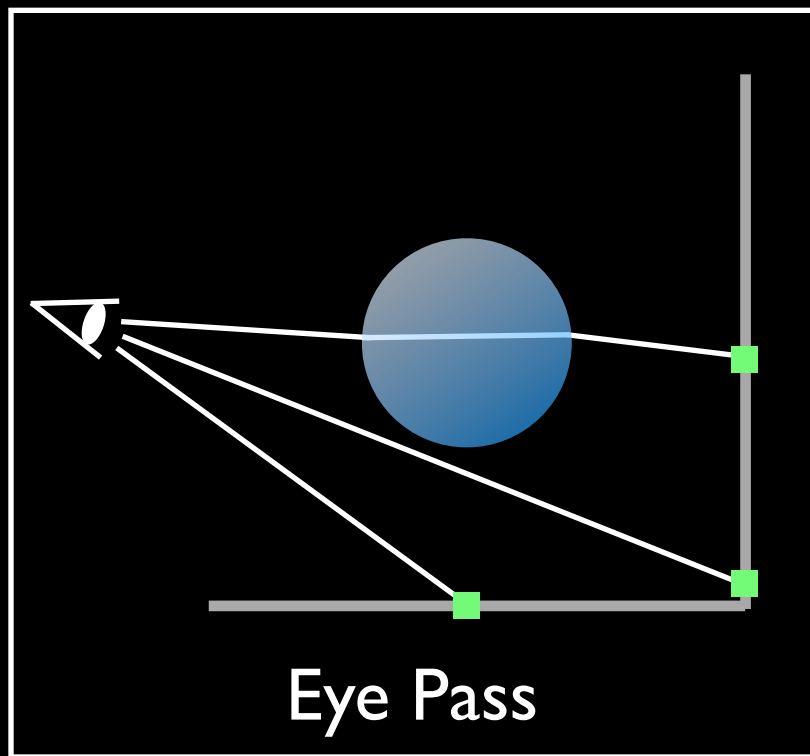
Infinite number of measurement points

# Stochastic Progressive Photon Mapping

Toshiya Hachisuka    Henrik Wann Jensen

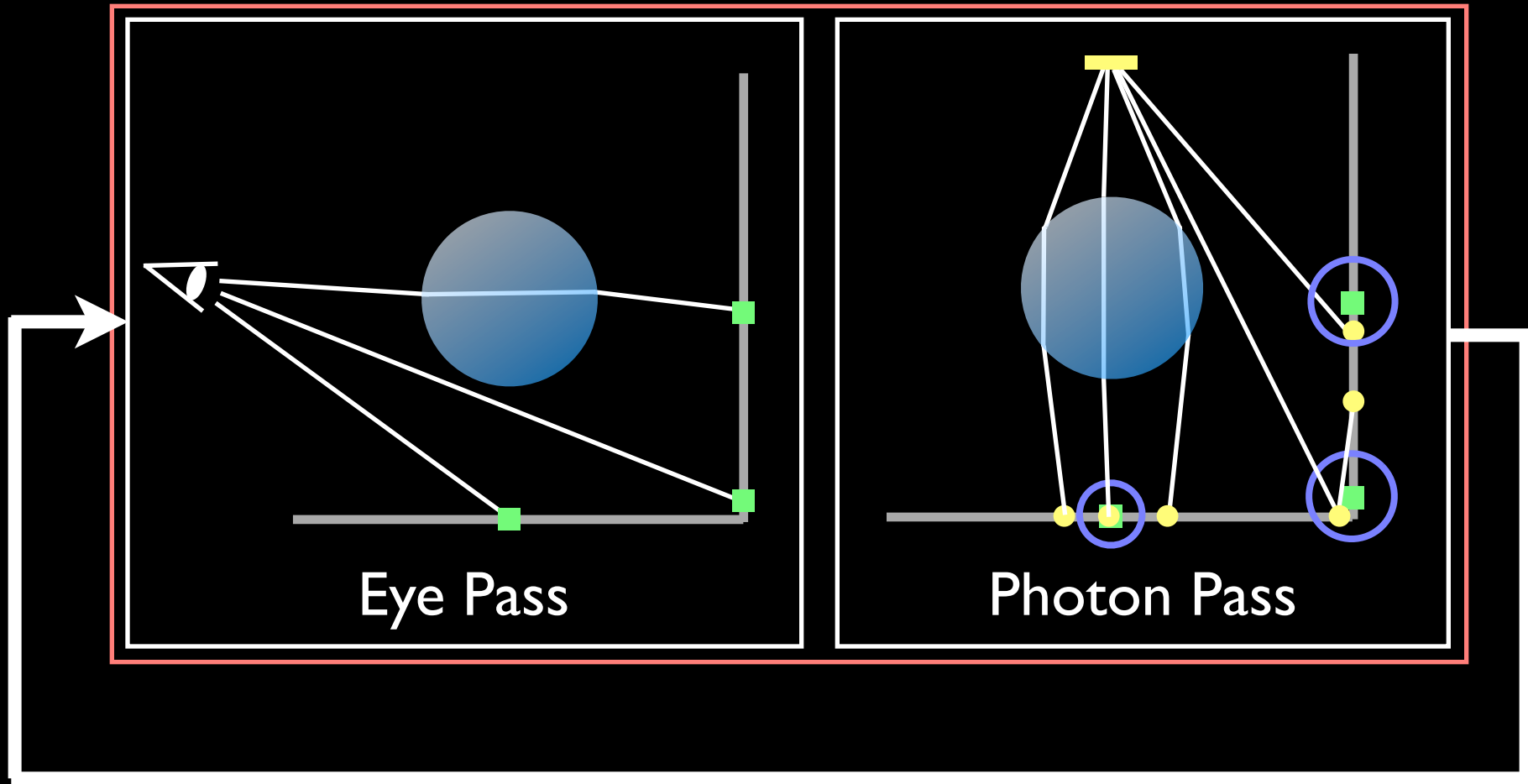
Published at SIGGRAPH Asia 2009

# PPM

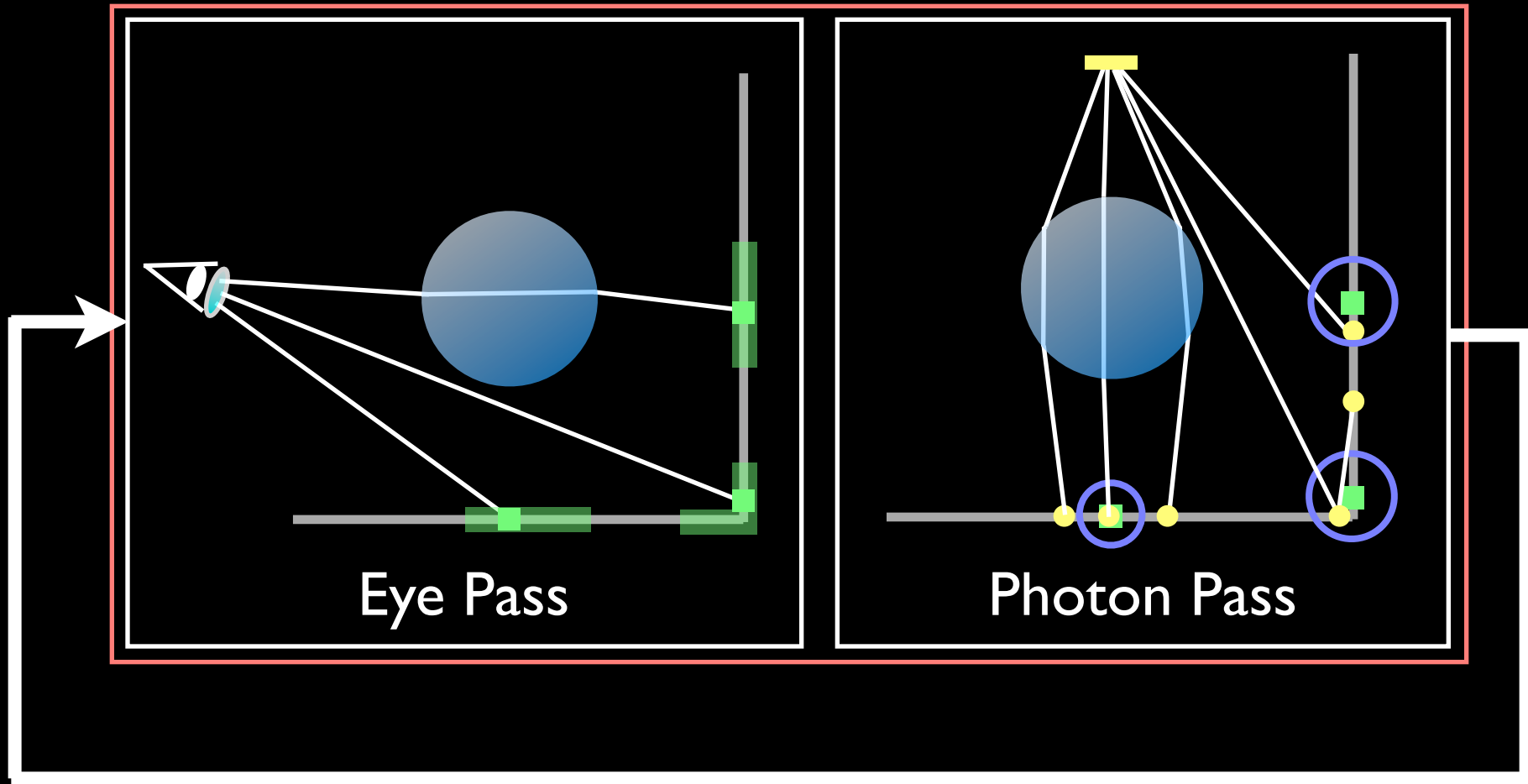




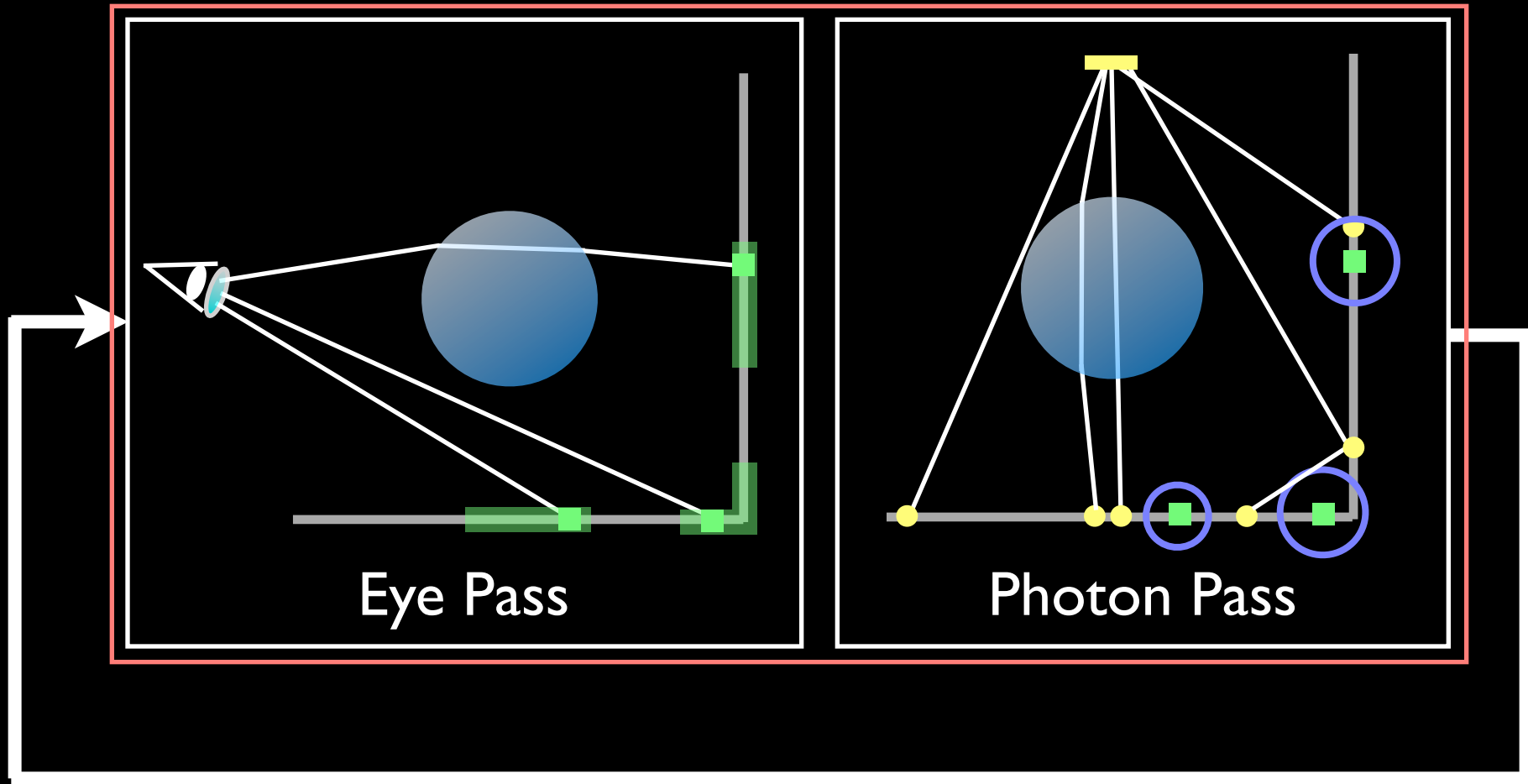
# Stochastic PPM



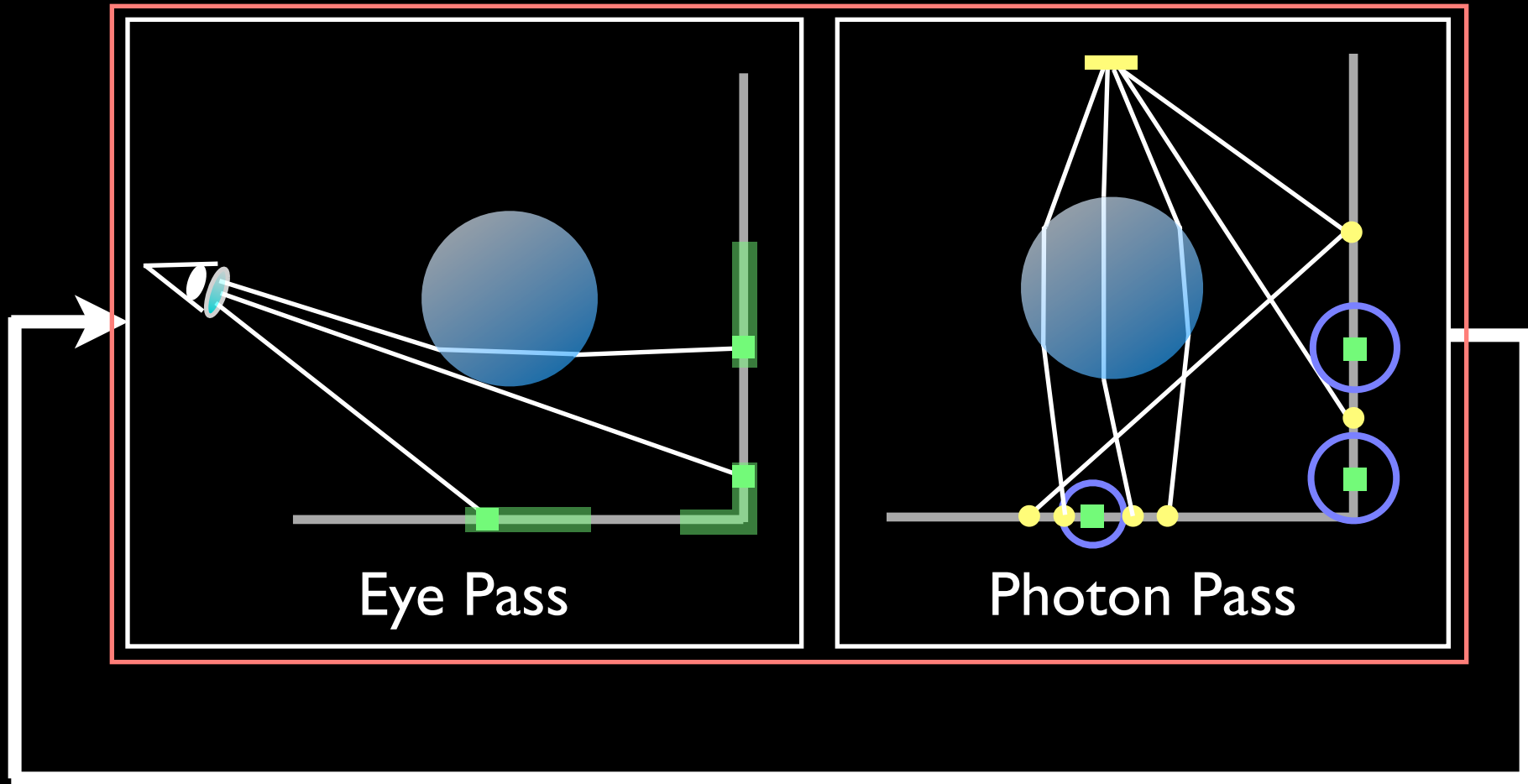
# Stochastic PPM



# Stochastic PPM



# Stochastic PPM



# Stochastic Progressive Density Estimation

$$L_i(S, \vec{\omega}) = \frac{\tau_i(S, \vec{\omega})}{\pi R_i(S)^2 N_e(i)}$$

$$\lim_{i \rightarrow \infty} L_i(S, \vec{\omega}) = L(S, \vec{\omega})$$

Provable convergence to  
average photon density over a region S

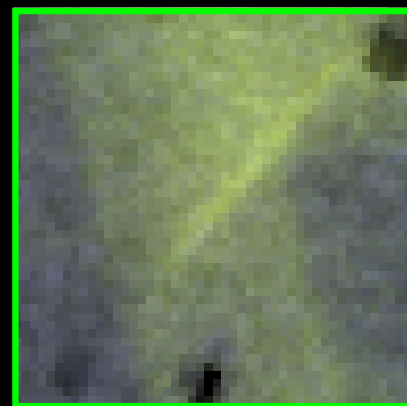
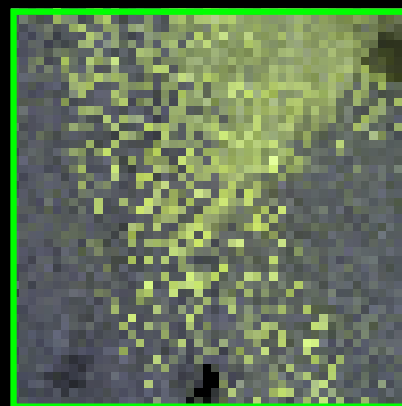
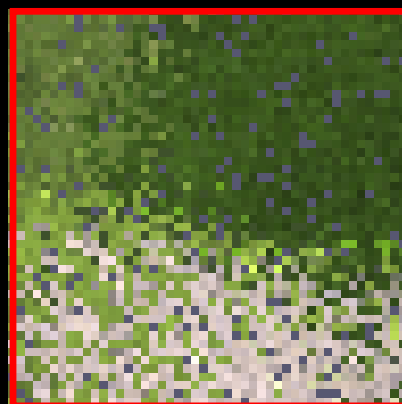
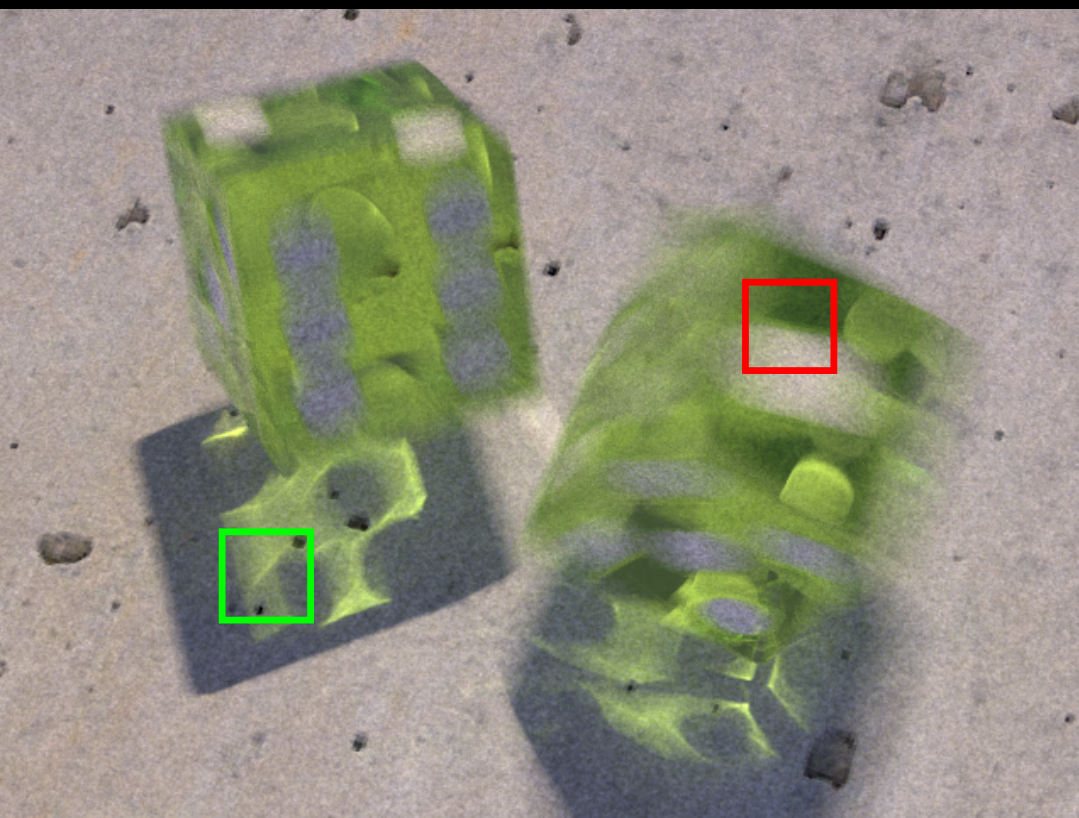
# Bidirectional Path Tracing



# Stochastic PPM



# Motion Blur



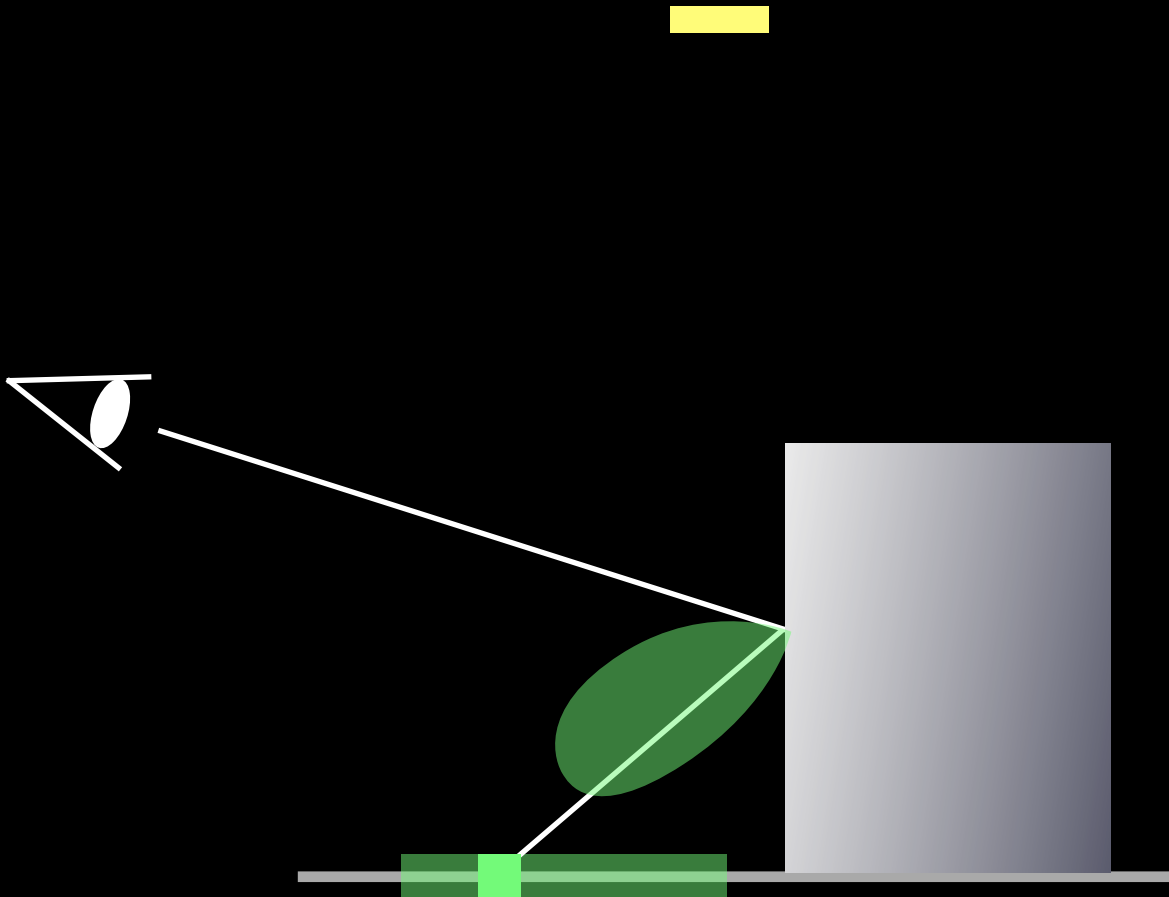
Equal time, Equal memory

PPM

SPPM

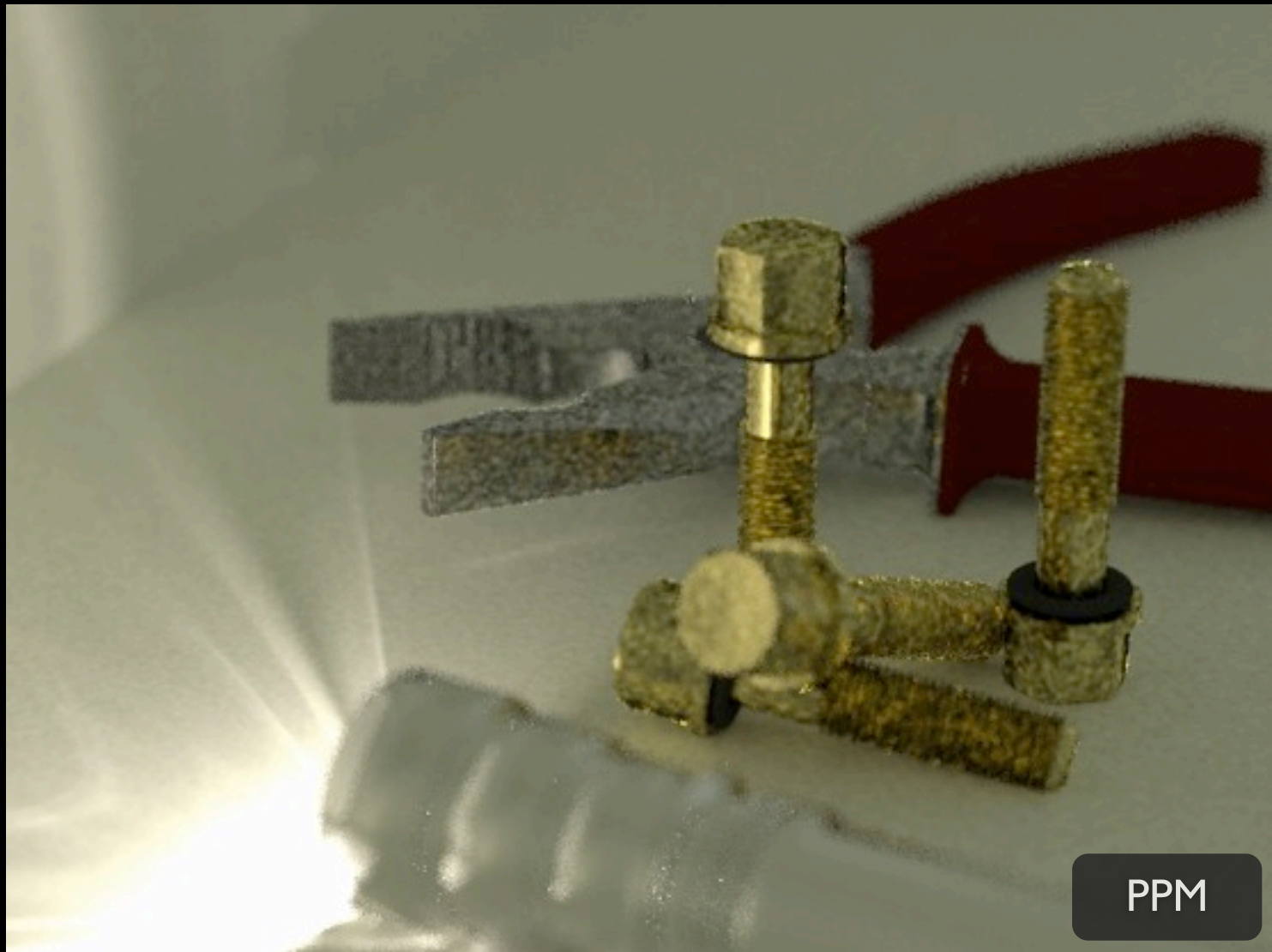


# Glossy Materials with SPPM



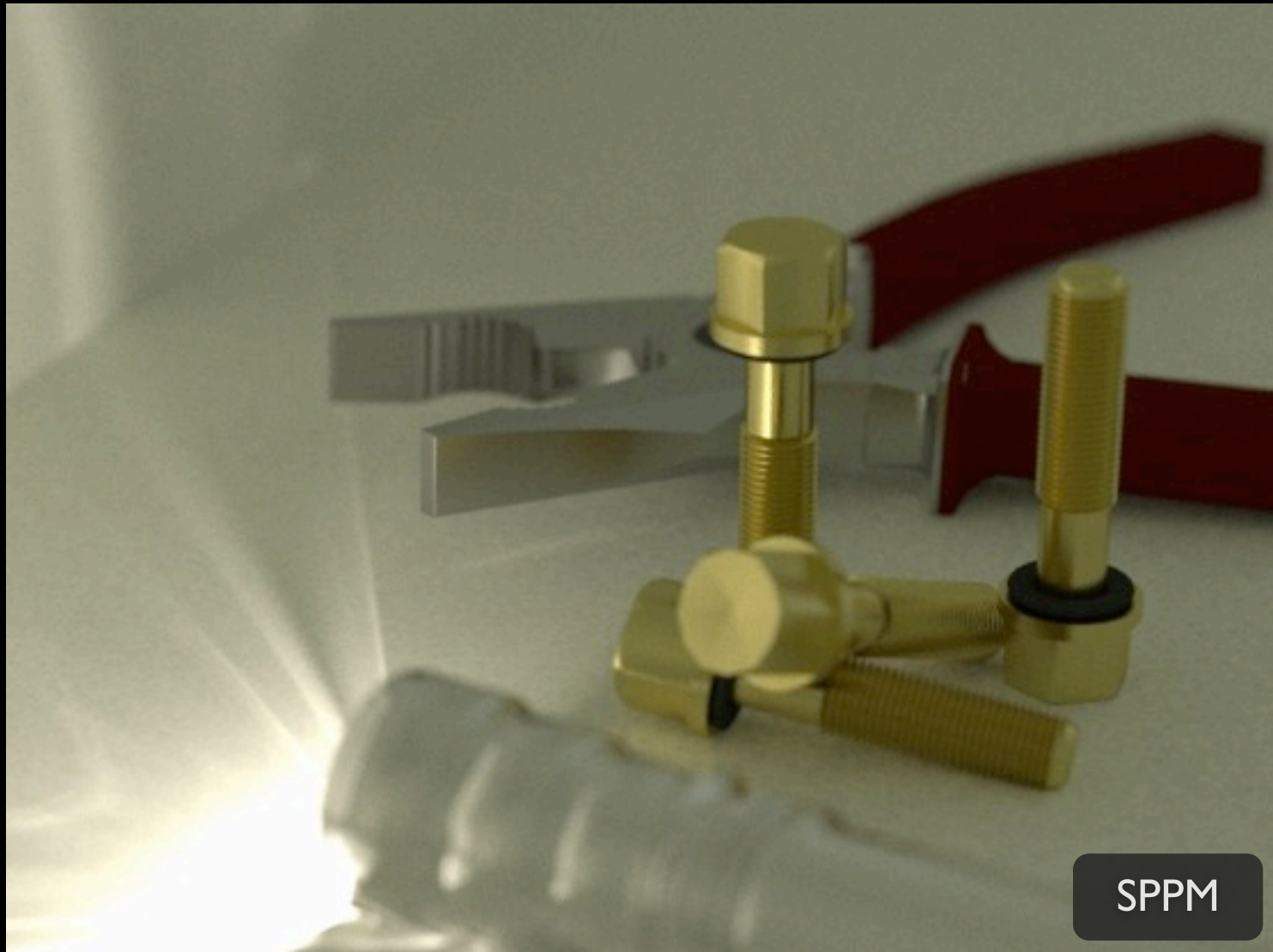
Trace one bounce rays

# DOF + Glossy Reflection + Caustics



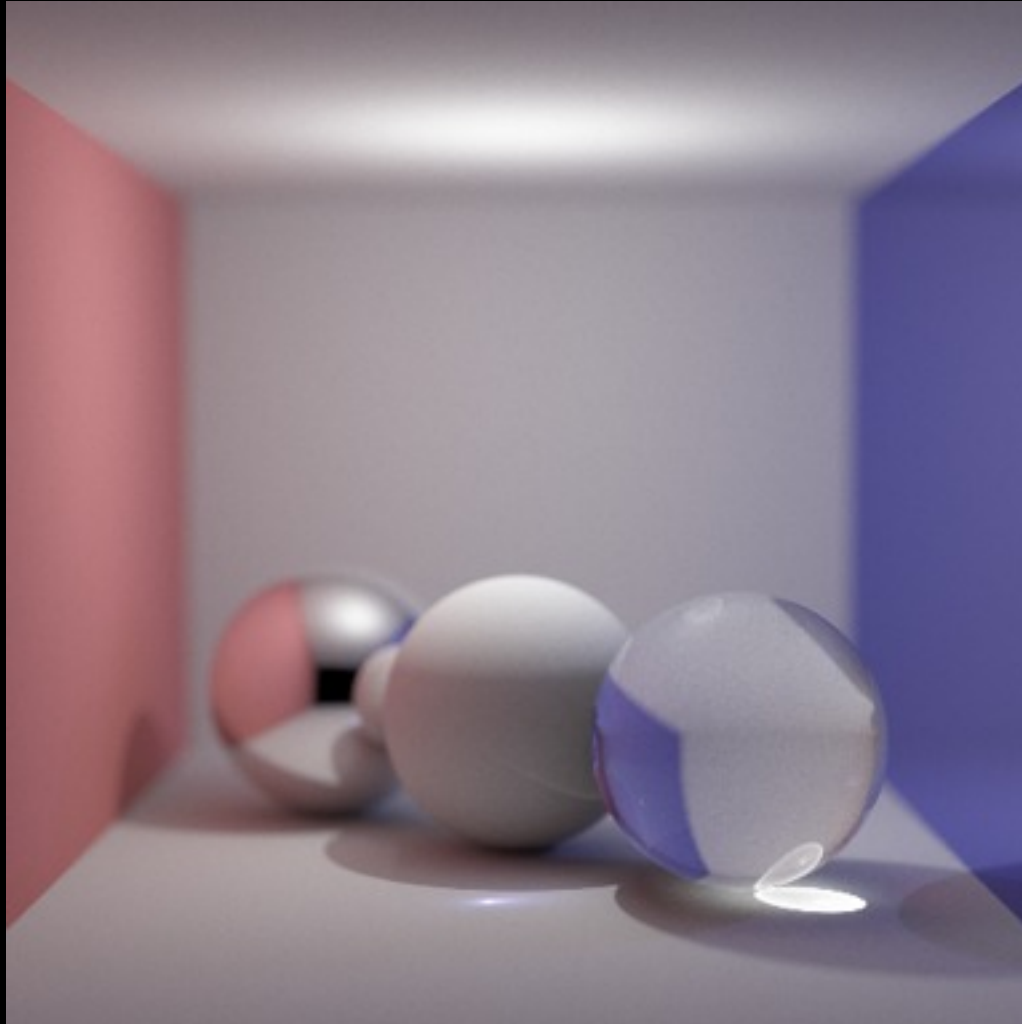
PPM

# DOF + Glossy Reflection + Caustics



SPPM

# GPUSPPM



[cs.au.dk/~toshiya/gpusppm.zip](http://cs.au.dk/~toshiya/gpusppm.zip)

How much computation is enough?

# A Progressive Error Estimation Framework for Photon Density Estimation

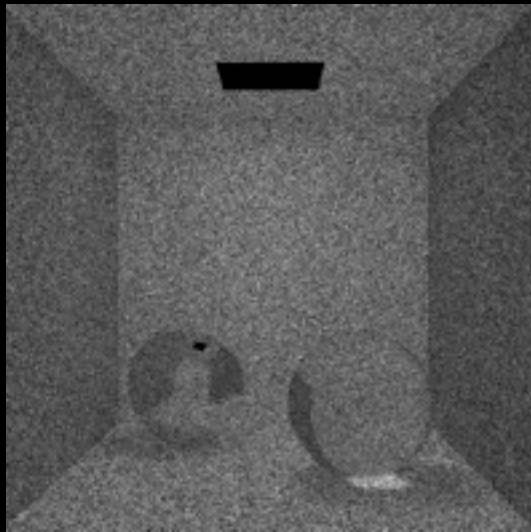
Toshiya Hachisuka   Wojciech Jarosz   Henrik Wann Jensen

Presented & Published at SIGGRAPH/SIGGRAPH Asia 2010

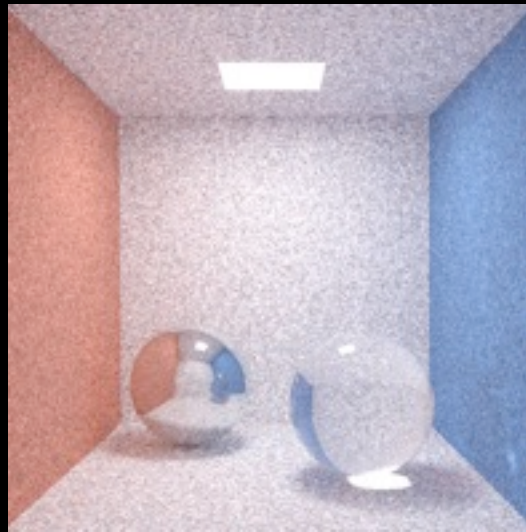
# Definition of Error

- Difference between computed and exact

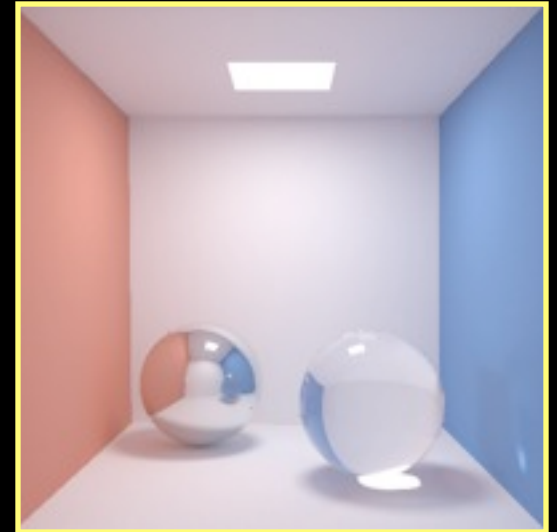
$$E_i = L_i - \boxed{L} \text{ Unknown}$$



=



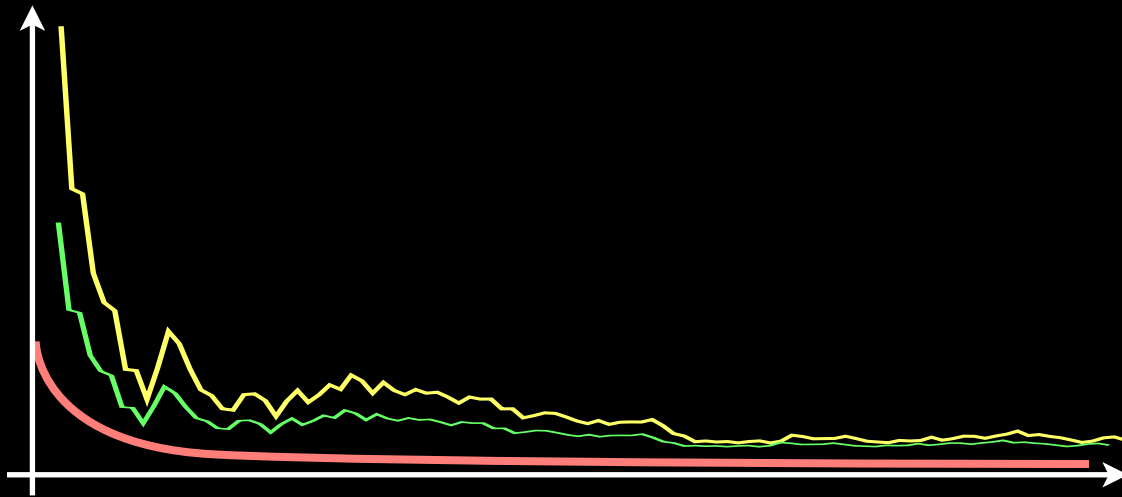
-



# Decomposition of Error

- Bias-Noise decomposition

$$E_i = L_i - L = B_i + N_i$$





# Stochastic Error Bound Derivation

$$E_i = L_i - L = B_i + N_i$$

Stochastic error bound

User-defined  
Probability

$$P(|E_i| \leq E_{b,i}) \leq 1 - \beta$$

$$E_{b,i} = C_{i,1-\frac{\beta}{2}} \sqrt{\frac{\text{Variance}}{i}} + |B_i|$$

# Stochastic Error Bound Derivation

$$E_i = L_i - L = B_i + N_i$$

$$P(|E_i| \leq E_{b,i}) \leq 1 - \beta$$

$$E_{b,i} = \boxed{C_{i,1-\frac{\beta}{2}} \sqrt{\frac{\text{Variance}}{i}}} + |B_i|$$

Error due to Noise

# Stochastic Error Bound Derivation

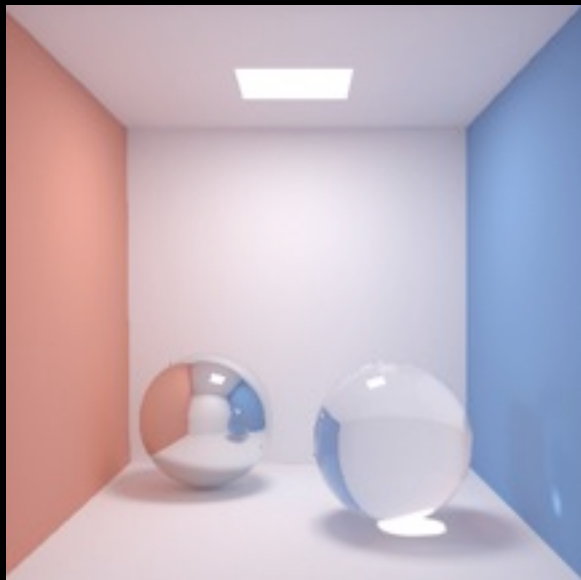
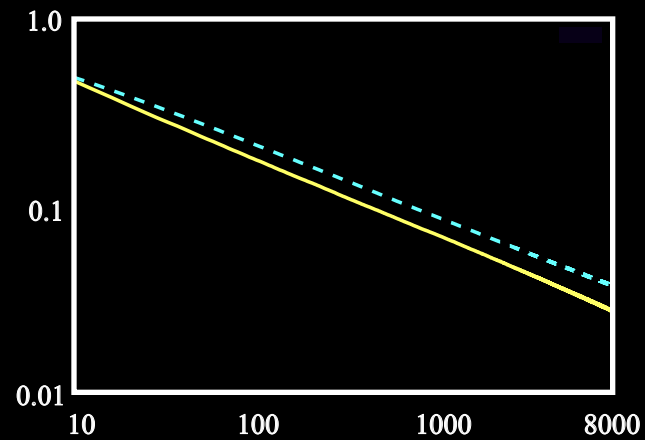
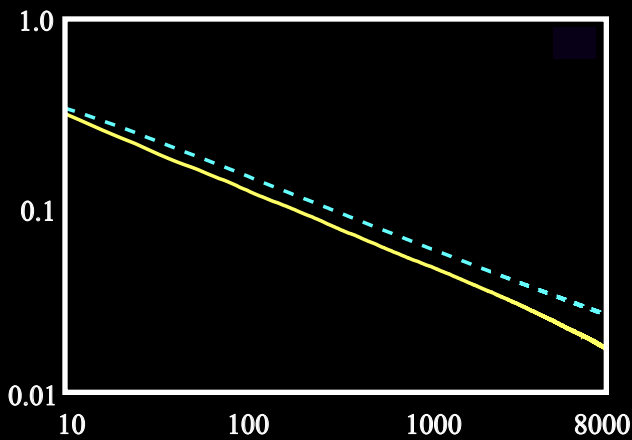
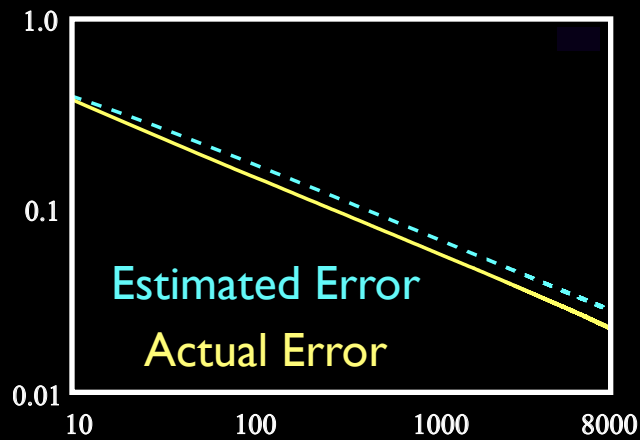
$$E_i = L_i - L = B_i + N_i$$

$$P(|E_i| \leq E_{b,i}) \leq 1 - \beta$$

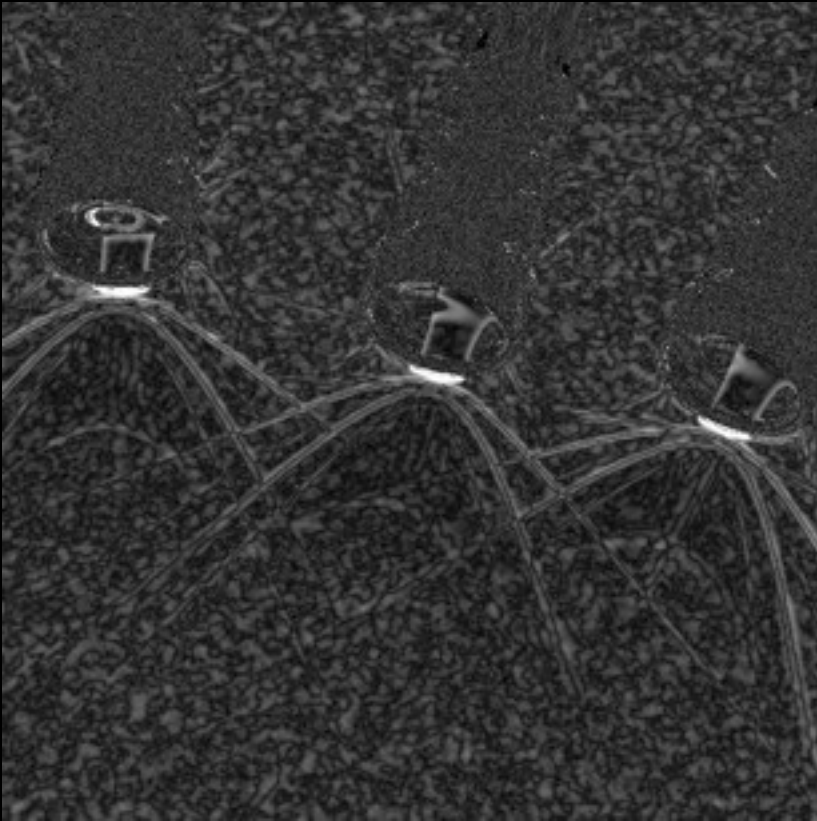
$$E_{b,i} = C_{i,1-\frac{\beta}{2}} \sqrt{\frac{\text{Variance}}{i}} + \boxed{|B_i|}$$

Error due to Bias

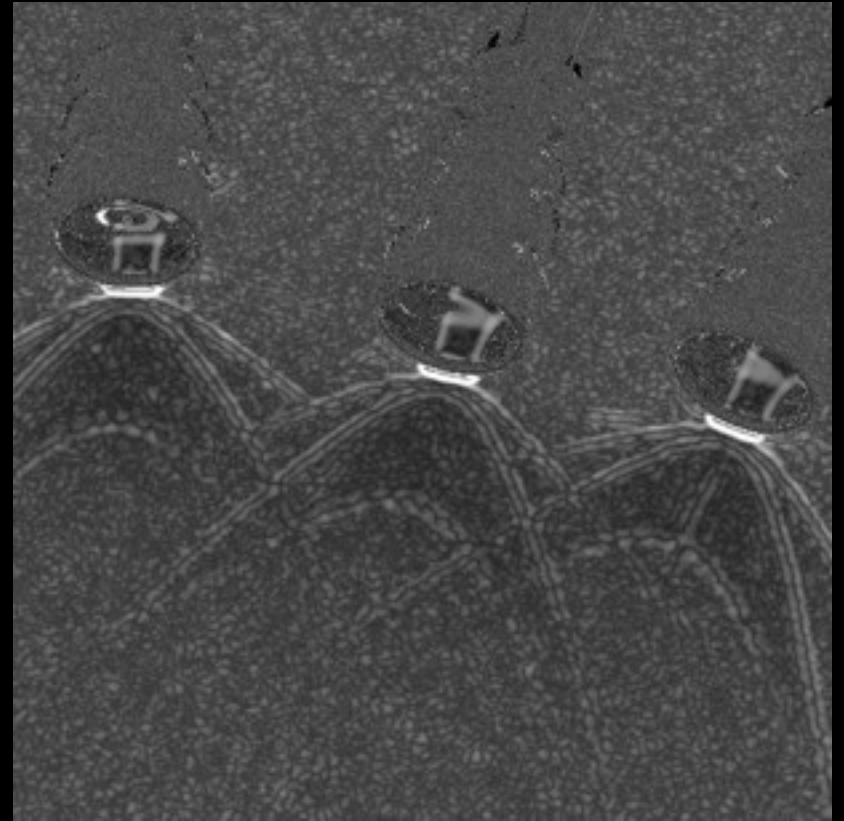
# Error Estimation



# Error Estimation

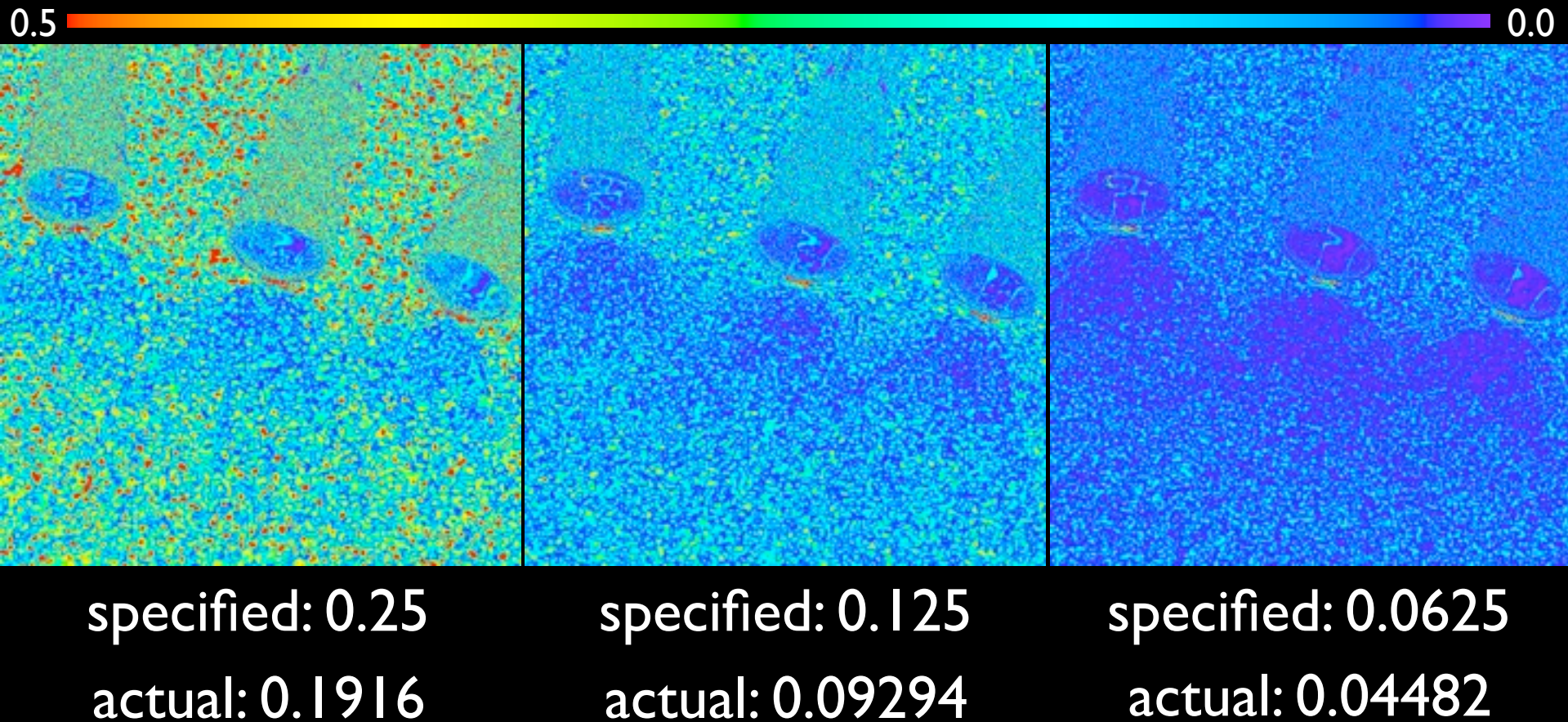


Actual Error



Estimated Error Bound

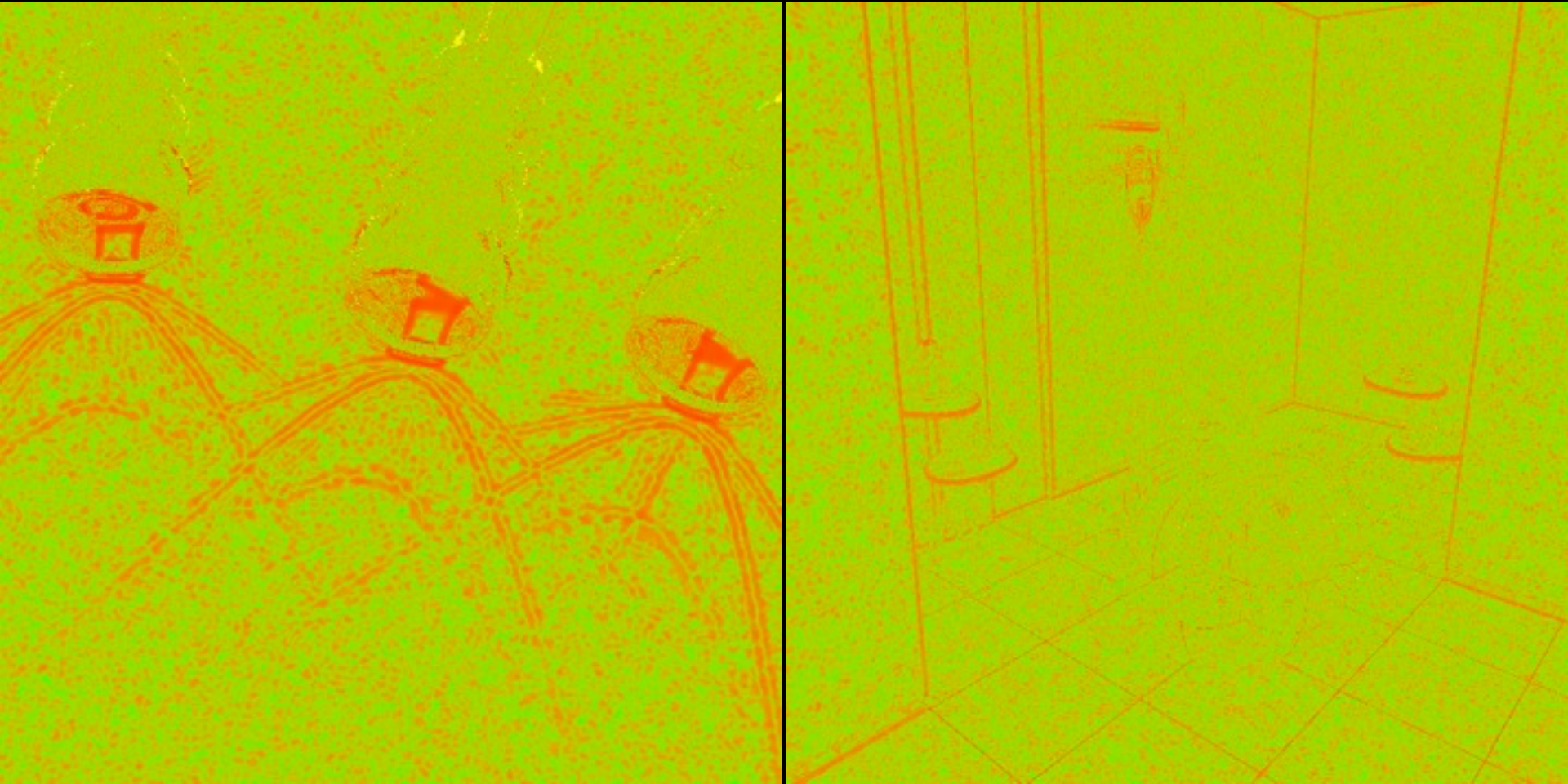
# Automatic Rendering Termination



1.3 times overestimation on average



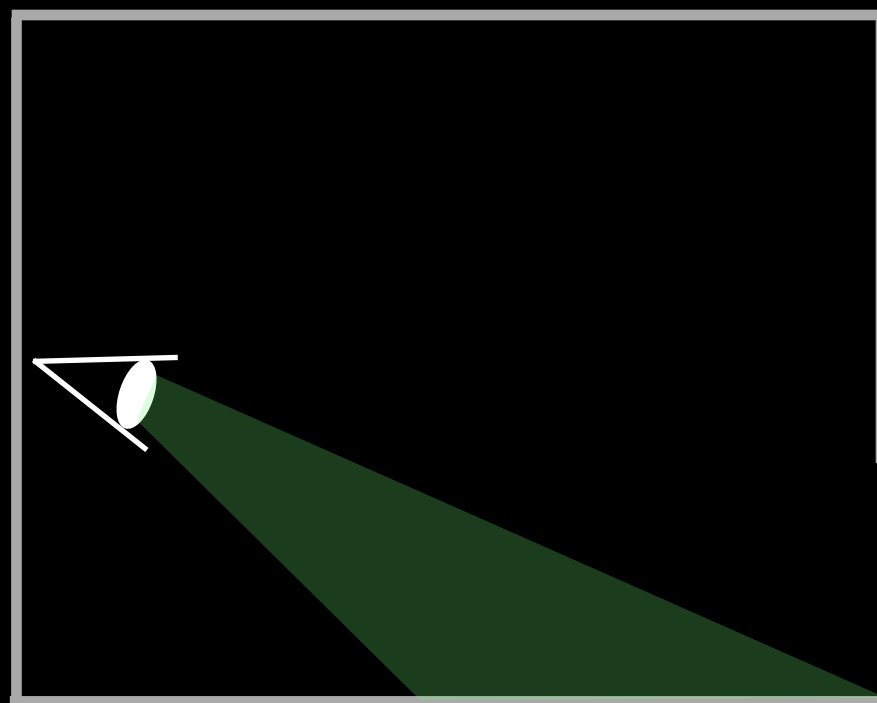
# Noise-Bias Ratio

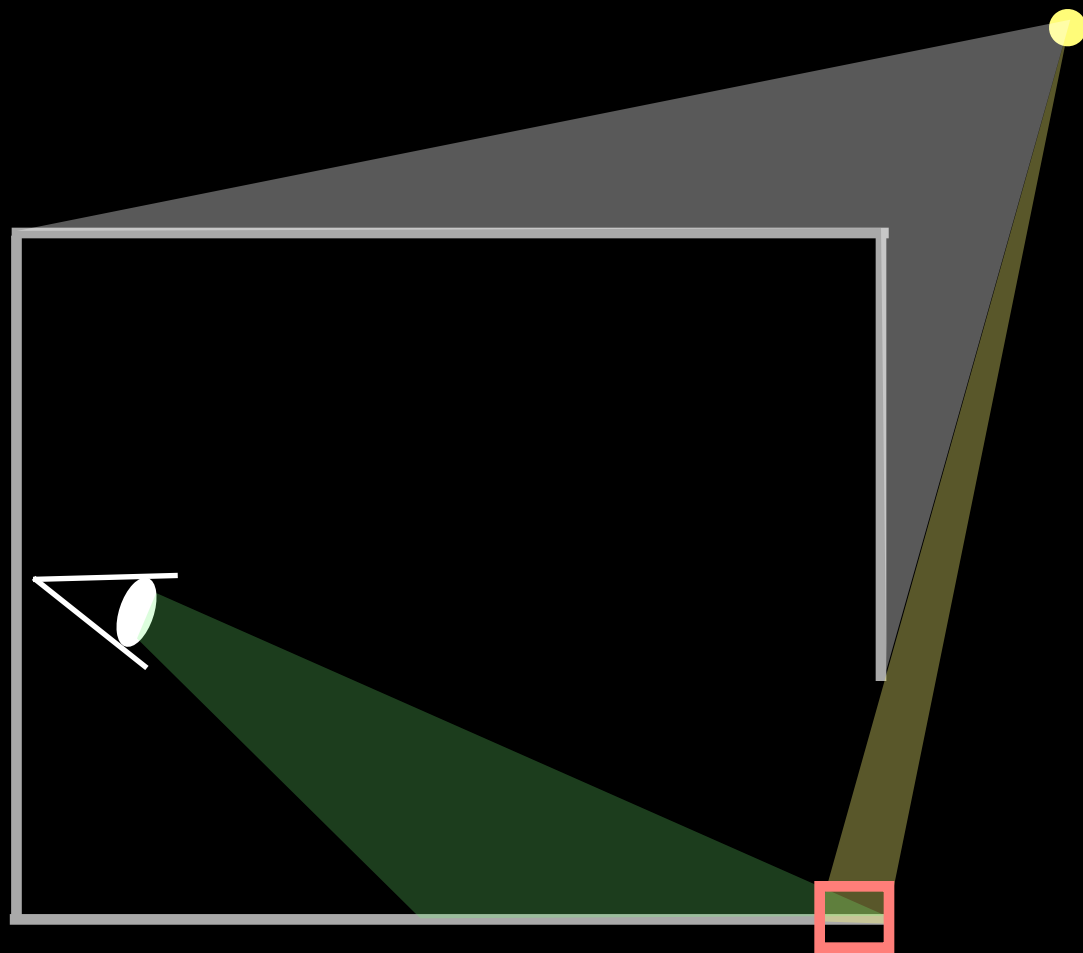


# Inefficient Case







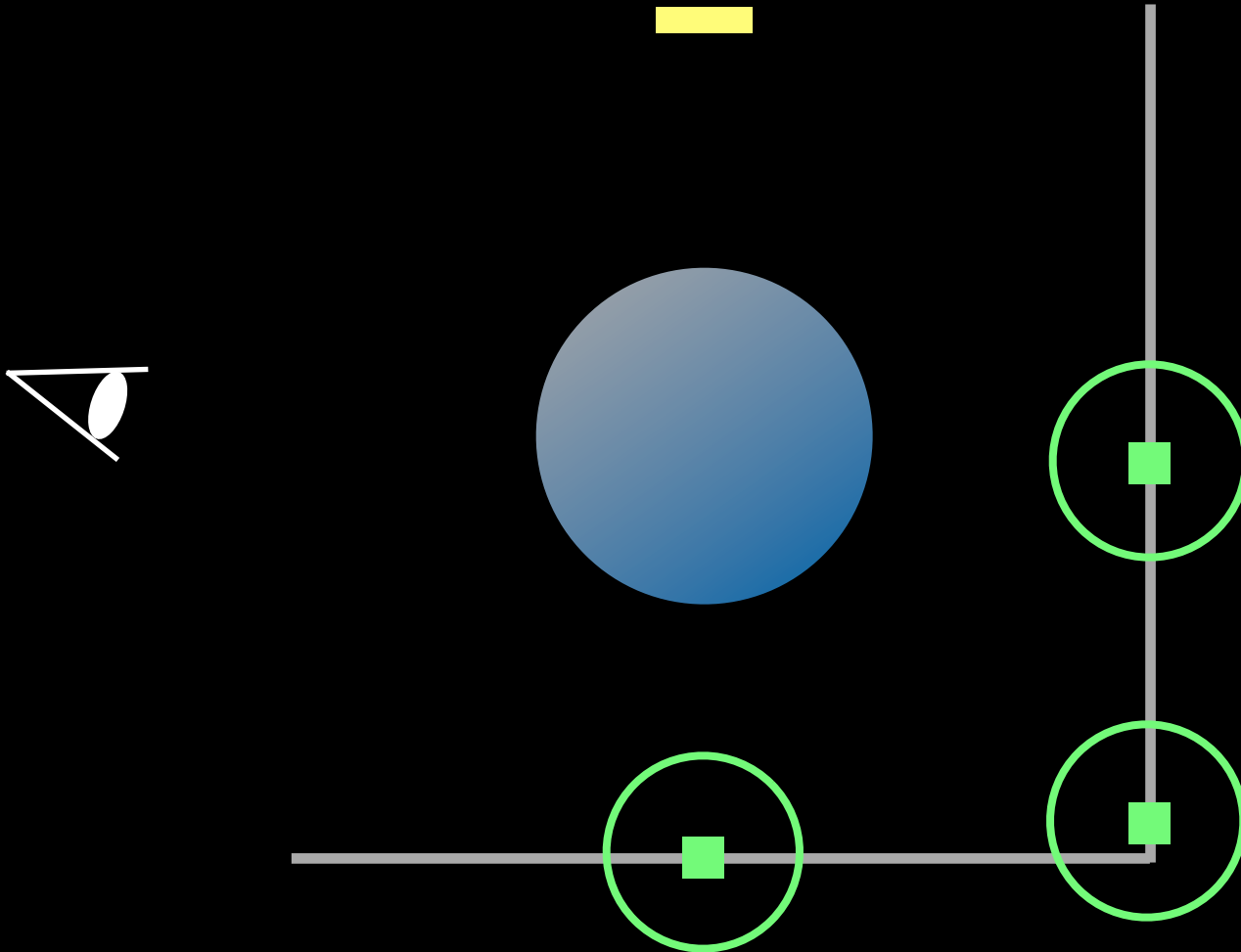


# Robust Adaptive Photon Tracing using Photon Path Visibility

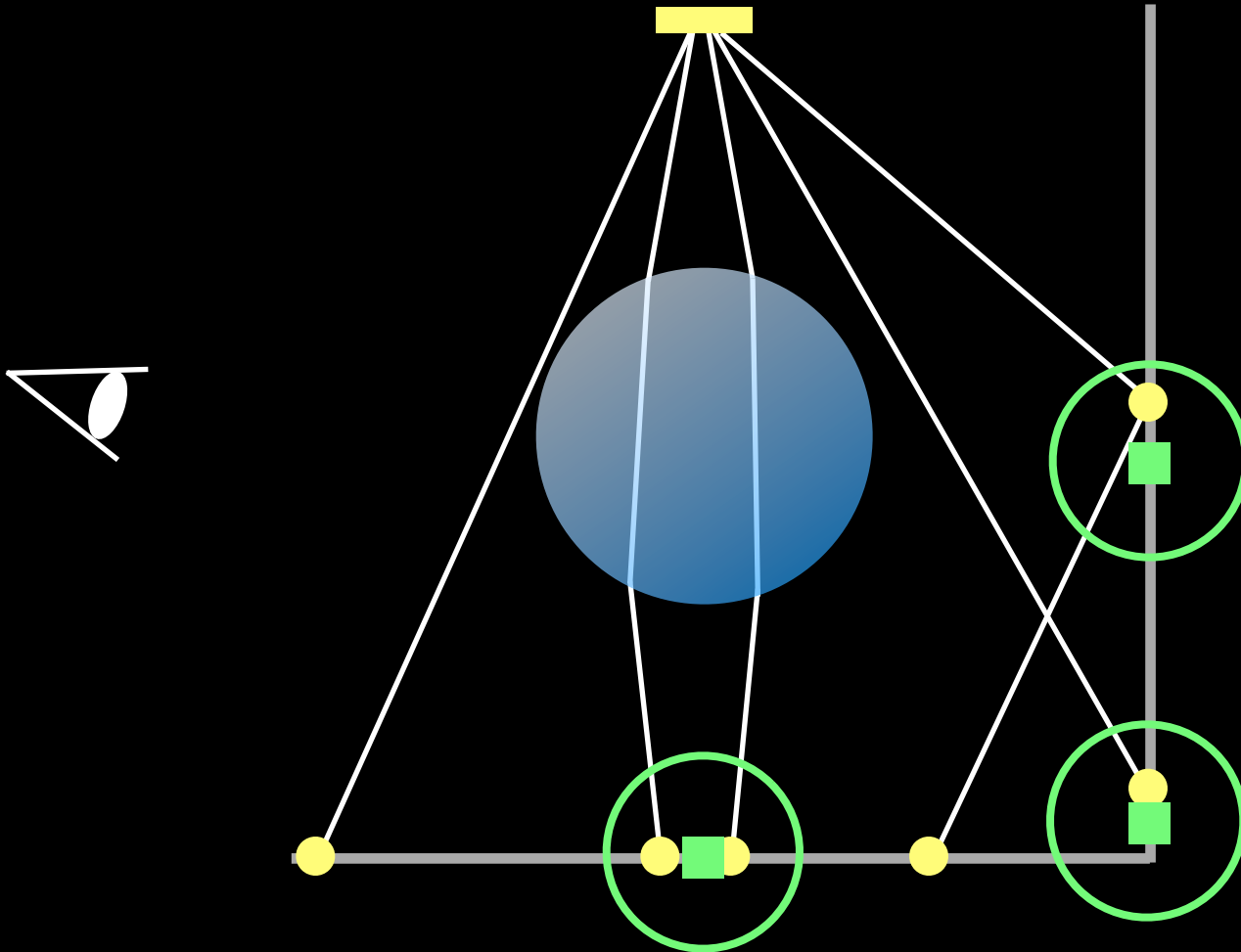
Toshiya Hachisuka    Henrik Wann Jensen

Published in ACM Transaction of Graphics  
(to be presented at SIGGRAPH 2013)

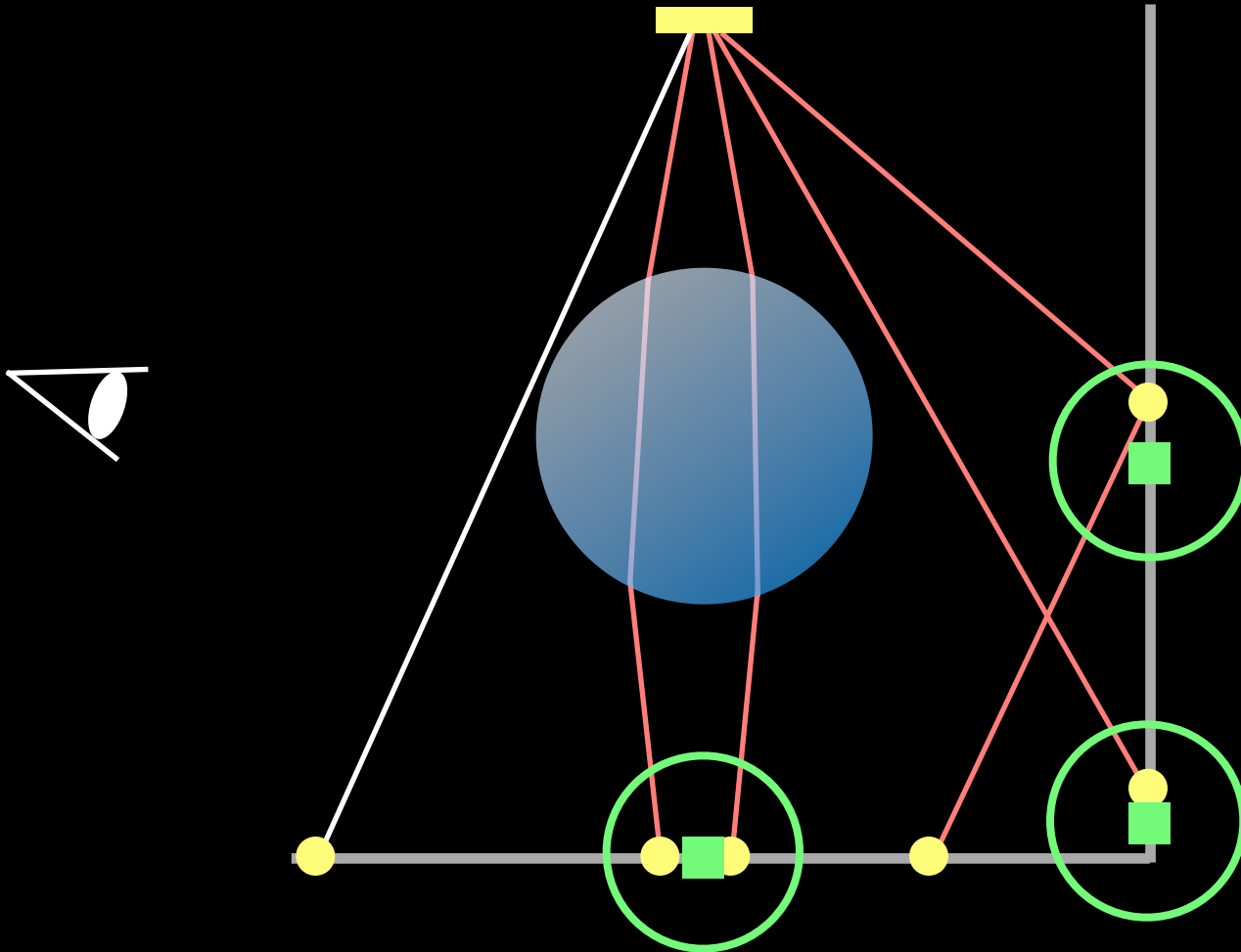
# Photon Tracing using Visibility



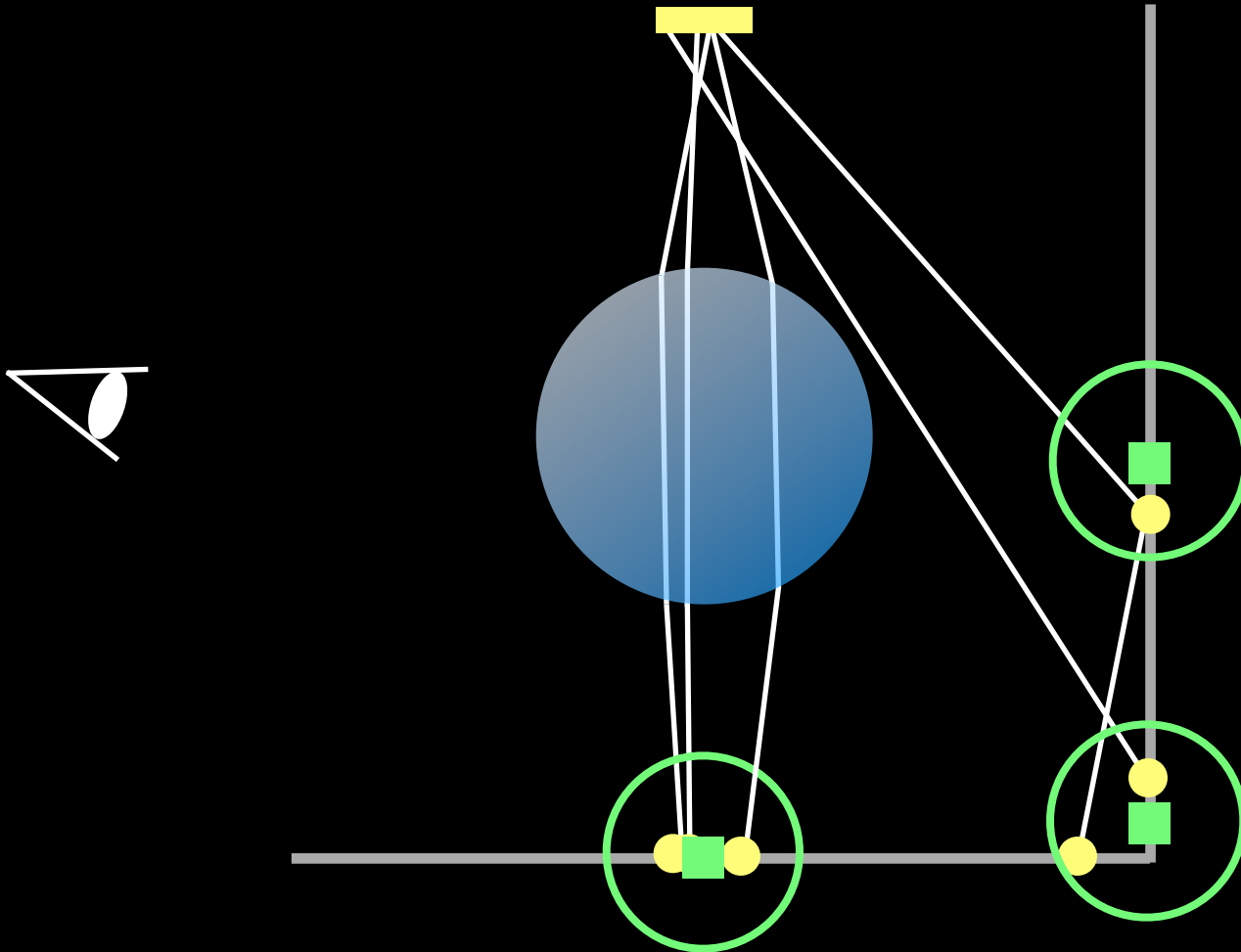
# Photon Tracing using Visibility



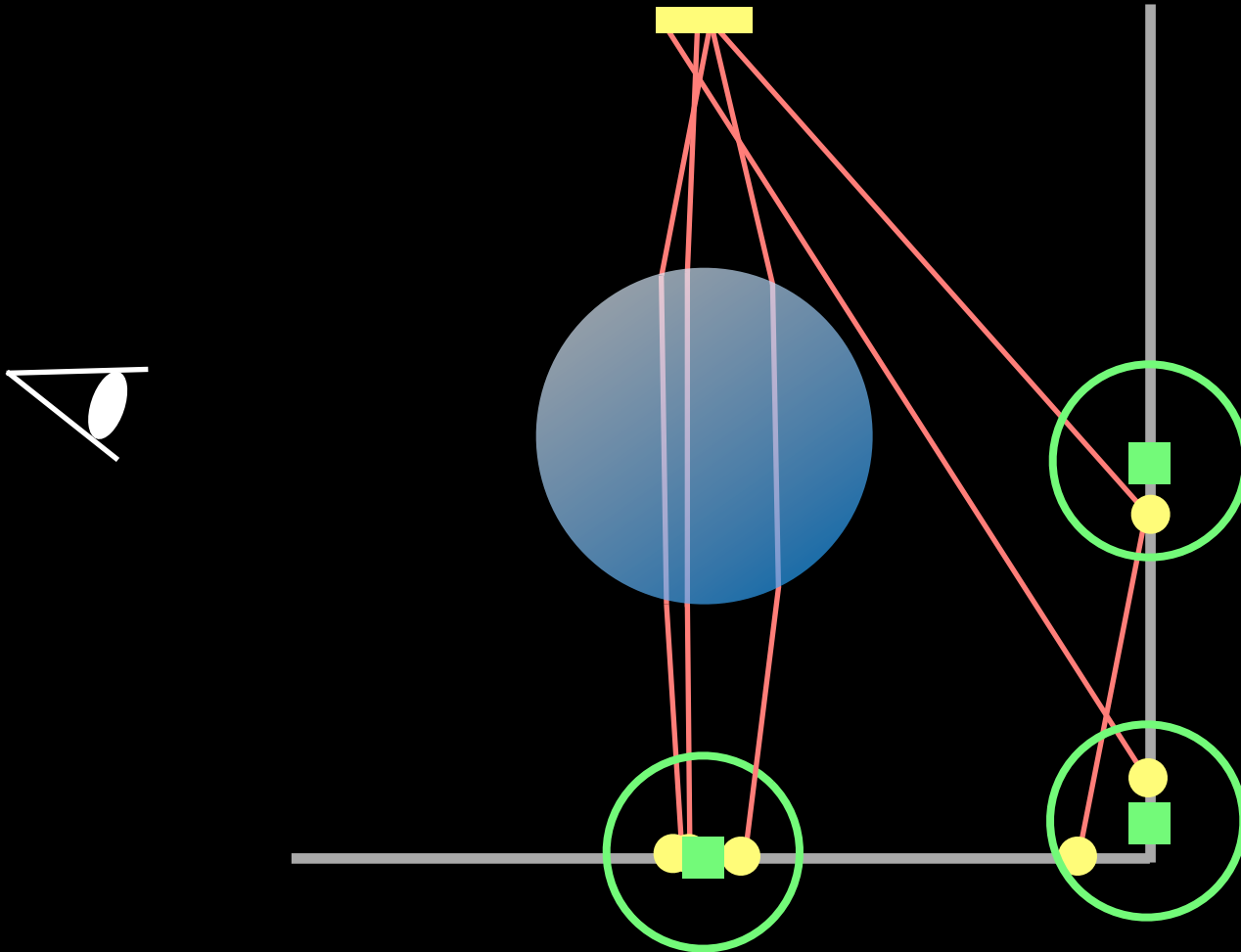
# Photon Tracing using Visibility



# Photon Tracing using Visibility



# Photon Tracing using Visibility





# Approach

- Consider space of random numbers  $\vec{u} \in (0, 1)^N$
- Photon path visibility function

If the photon is not visible:

$$V(\vec{u}) = 0$$

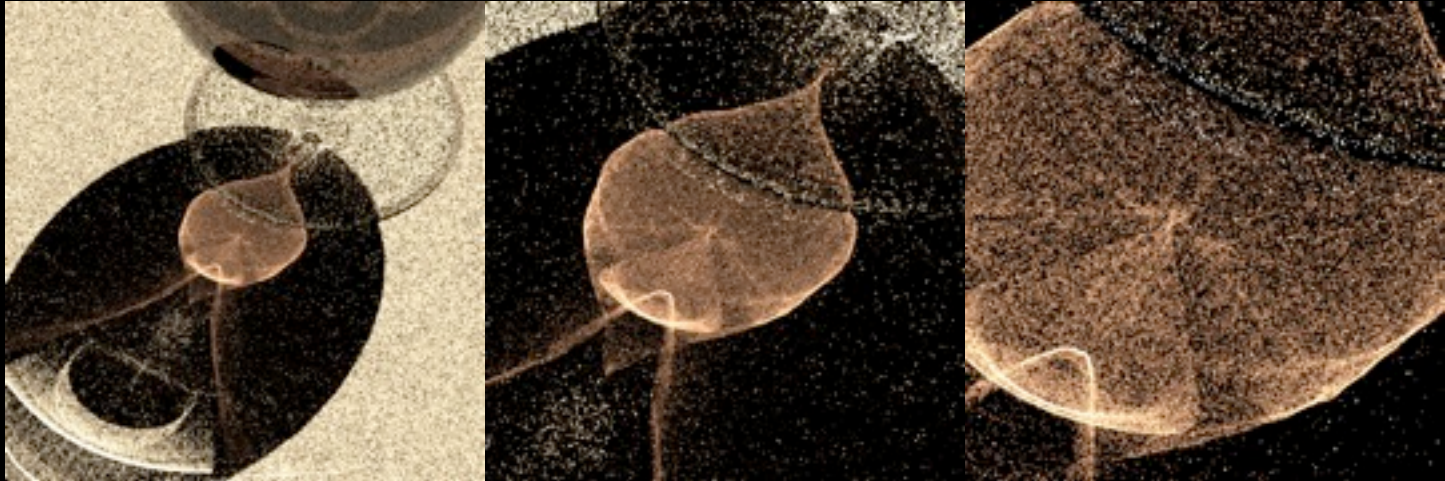
If the photon is visible:

$$V(\vec{u}) = 1$$

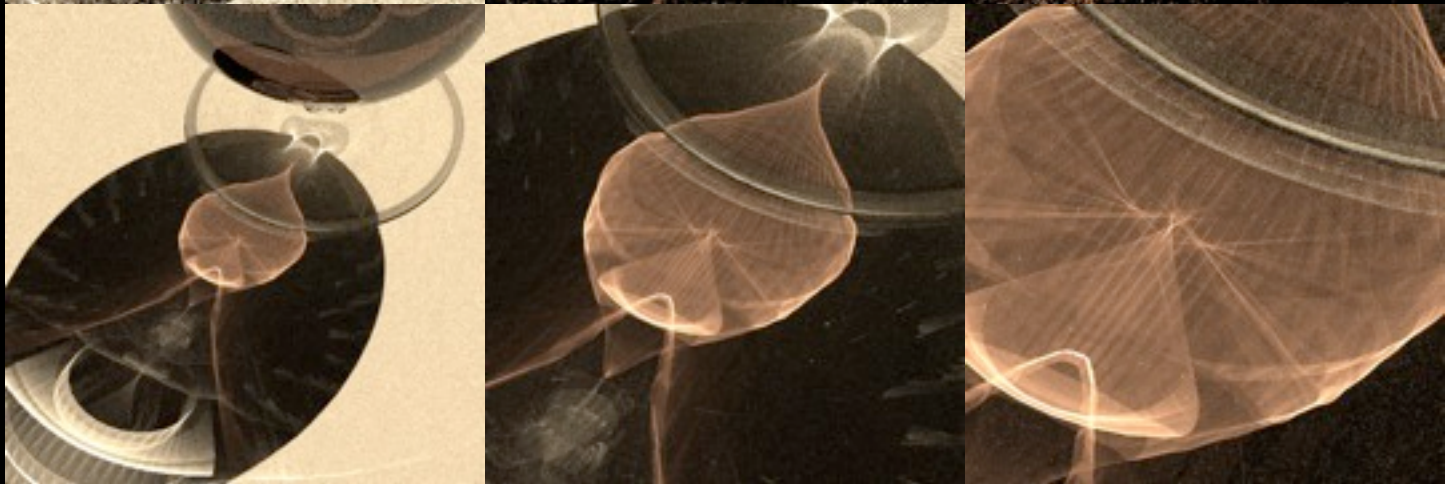
Sample  $V(\vec{u})$  using Markov chain Monte Carlo Methods

# Small-scale Lighting Details

Uniform



Adaptive



# Automatic Parameter Tuning



Value is too small



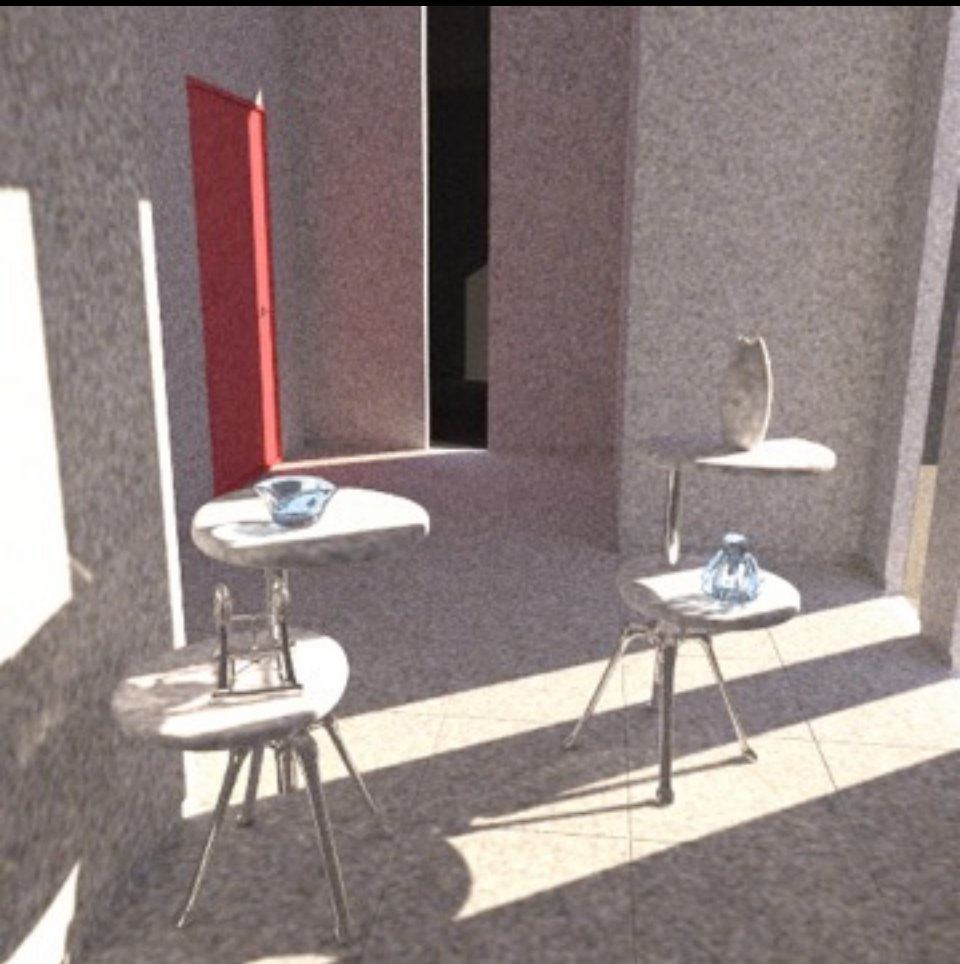
Automatic



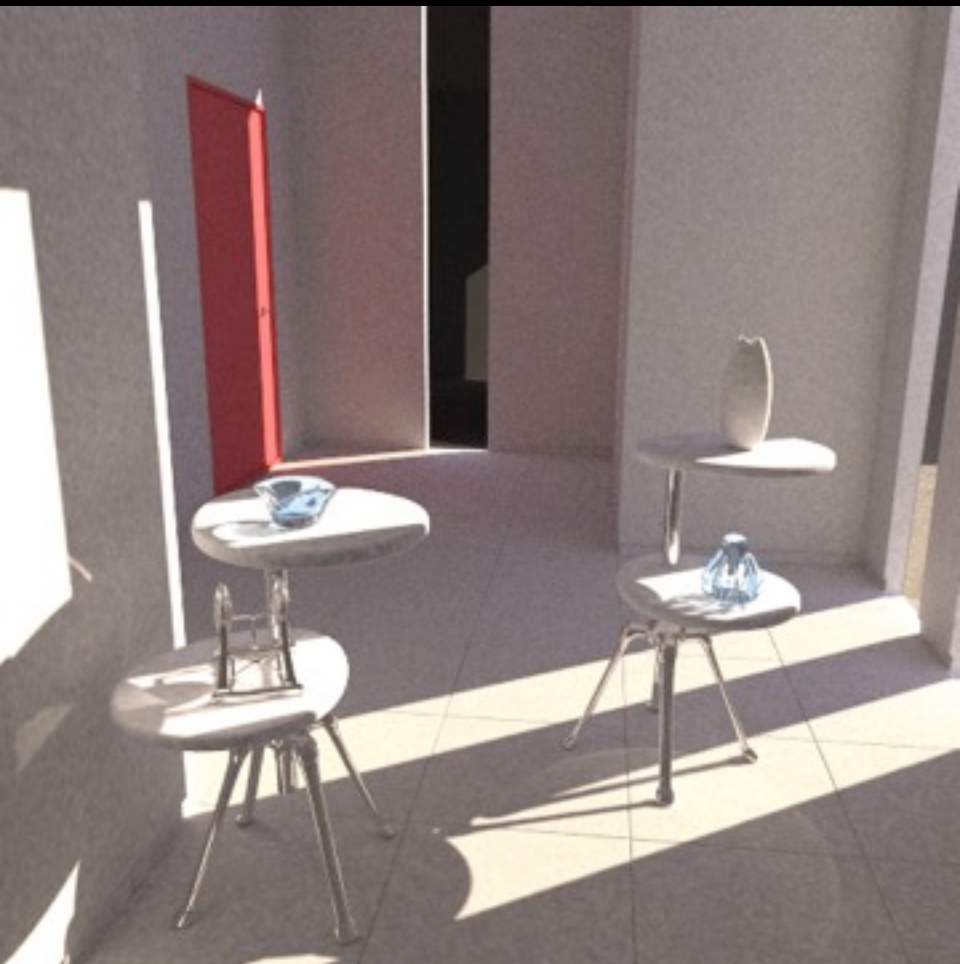
Value is too large



# Sunlit Room

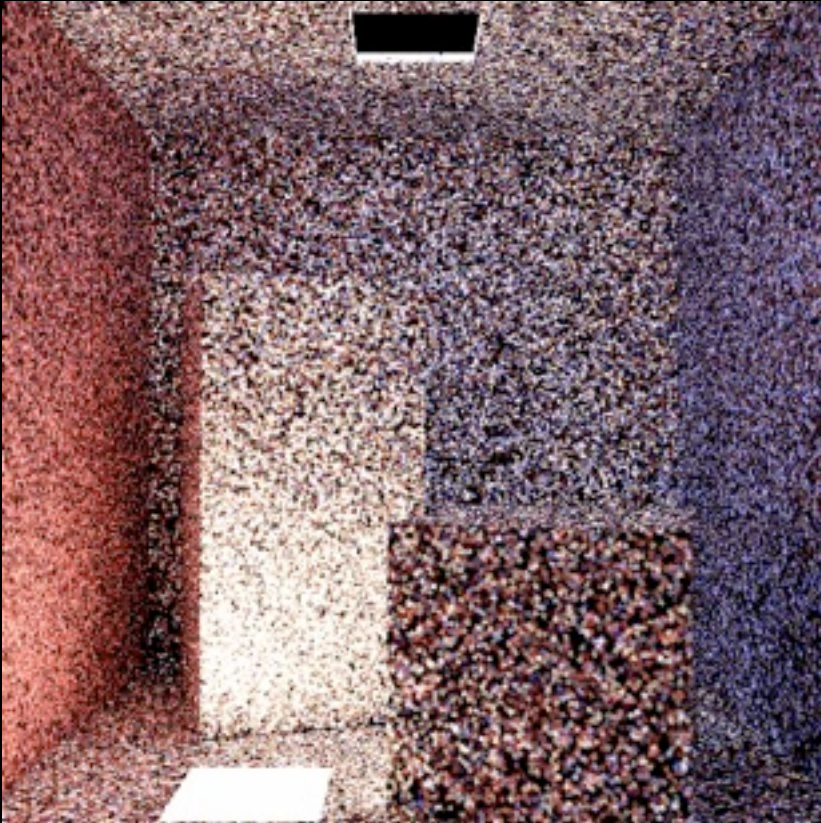


Uniform

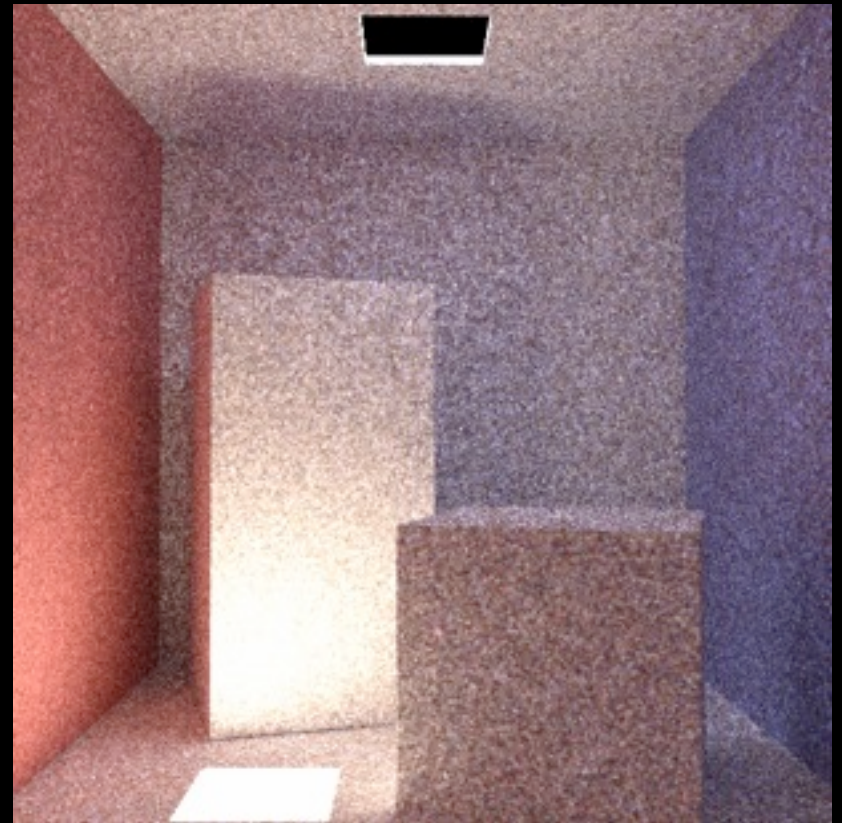


Adaptive

# Another Example



Uniform



Adaptive



# Another Example



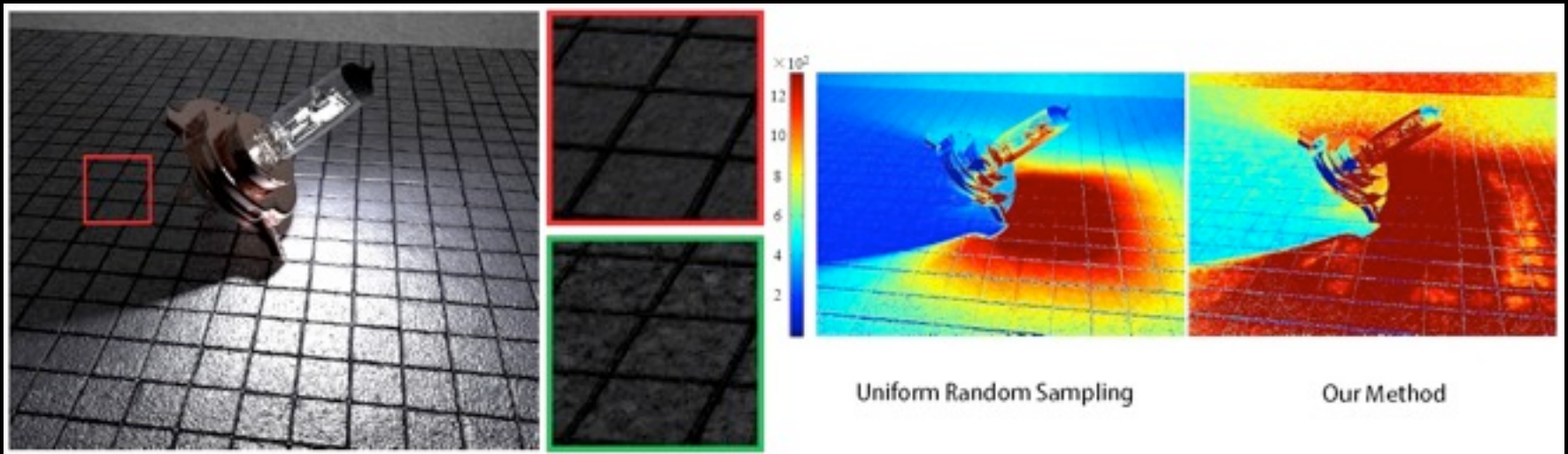
Uniform



Adaptive

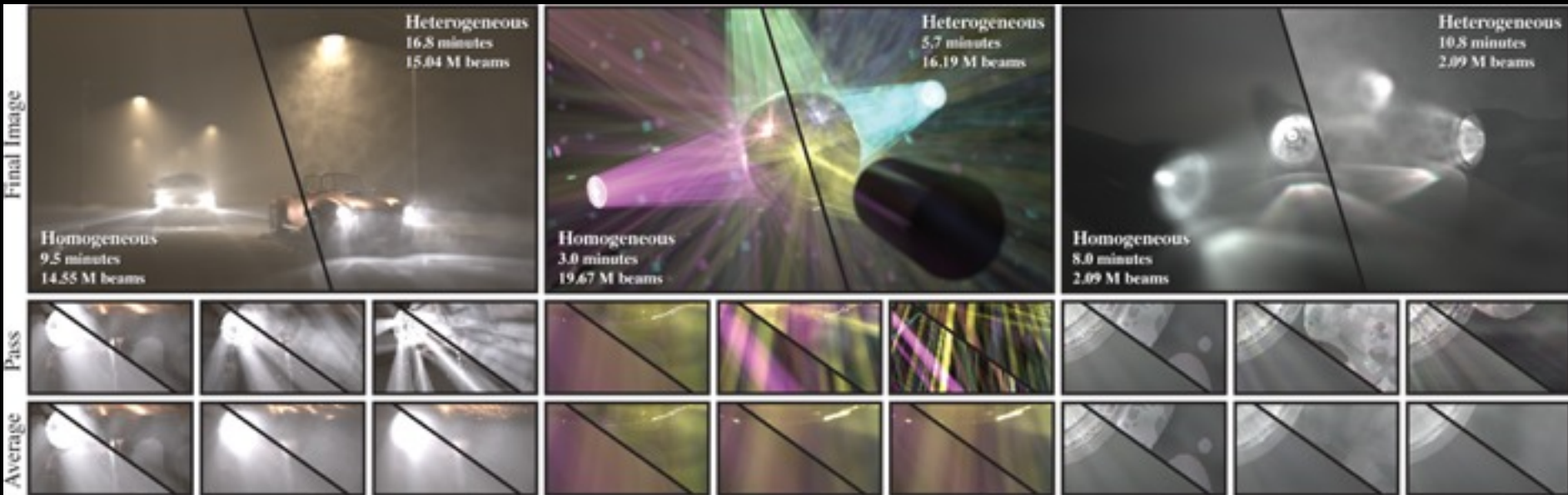
# Some Related Work

- Adaptive photon tracing based on photon density on the image [Chen et al. 2011]



# Some Related Work

- Progressive photon beams [Jarosz et al. 2011]





# Some Related Work

- Efficient rendering of dynamic scenes  
[Weiss and Grosch 2012]



# Some Related Work

- Combine density estimation and MC integration [Hachisuka et al. 2012]



# FAQs

- Q: Is PPM unbiased?

# FAQs

- **Q:** Is PPM unbiased?
- **A:** It is biased and consistent, but does not matter in practice.

$$E[X] = \lim_{\boxed{N \rightarrow \infty}} \sum_{i=1}^N x_i$$

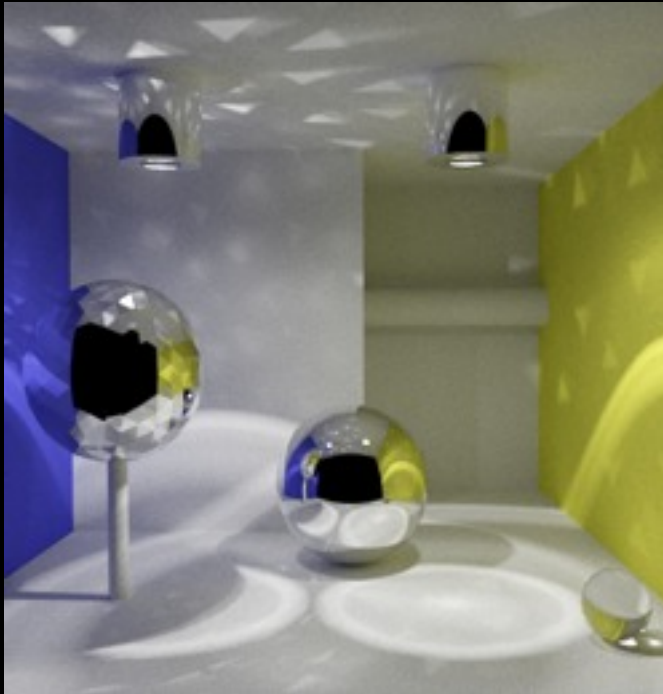
**BOTH unbiased and consistent methods need inf. samples!**

# FAQs

- Q: Do we still use global + caustics separation?

# FAQs

- **Q:** Do we still use global + caustics separation?
- **A:** Just render everything as one.



# FAQs

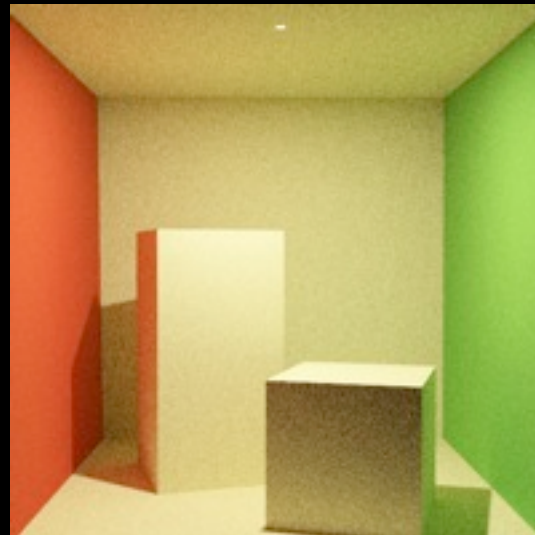
- **Q:** Is PPM slower for diffuse scenes than other methods?

# FAQs

- **Q:** Is PPM slower for diffuse scenes than other methods?
- **A:** True, but not much, and you can do more.



PT



PPM



# Summary

- SPPM = PPM + Distributed Ray Tracing
- Error estimation is available
- Adaptive photon tracing based on visibility
- Lots of interesting extensions
- My opinion: PPM + Extensions is the hardest rendering algorithm to “break” at the moment

[cs.au.dk/~toshiya](http://cs.au.dk/~toshiya)



# Next Talk

- Probabilistic formulation of PPM
- “How to turn your PM into PPM in a minute!”