

Directional Dipole Model for Subsurface Scattering

Toshiya Hachisuka

Collaboration with Jeppe Frisvad and Thomas Kjeldsen

The slides are based on the tech. report published in August 2013
For the latest results, please refer to the corresponding paper at TOG



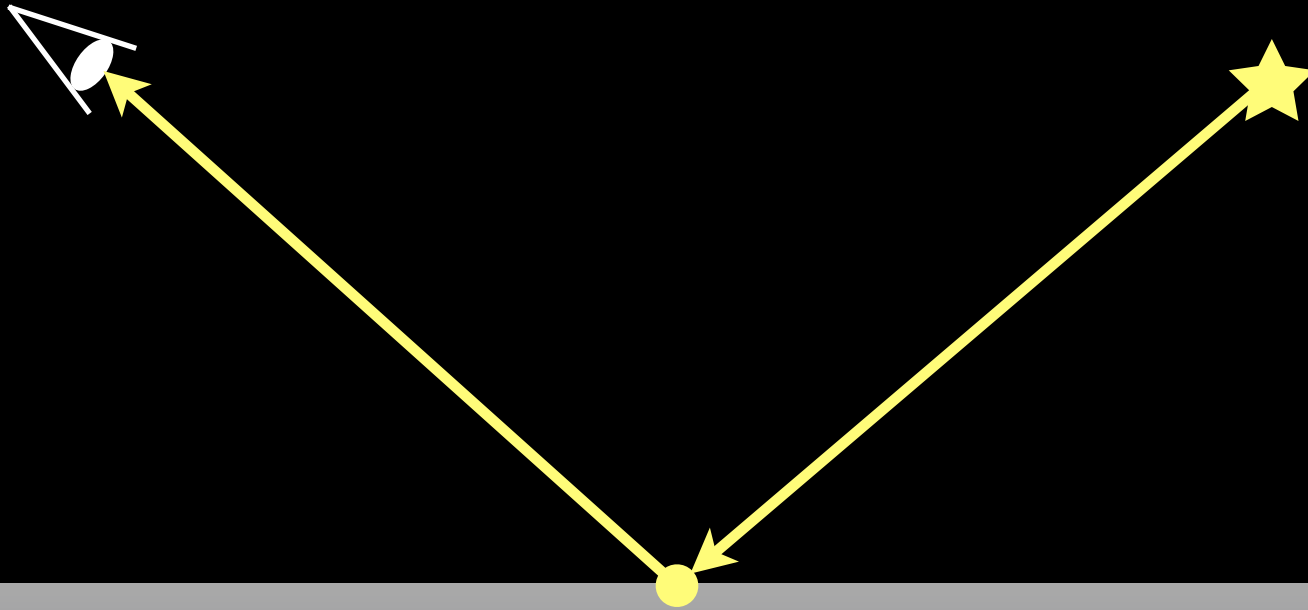








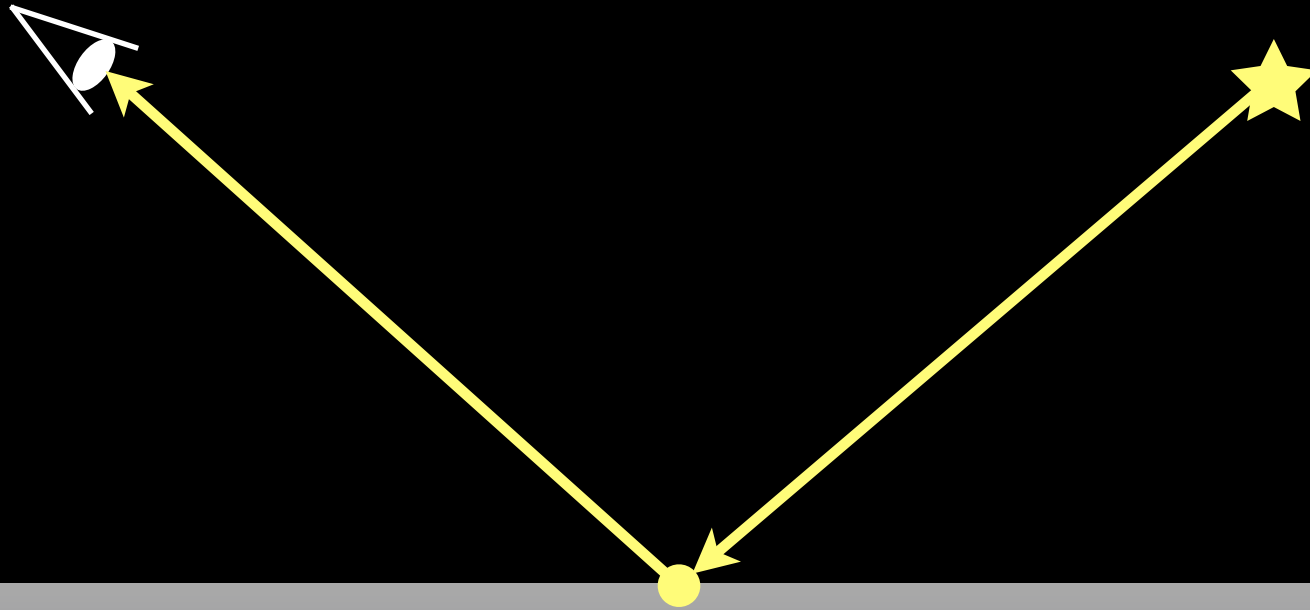
Bidirectional Reflectance Distribution Function



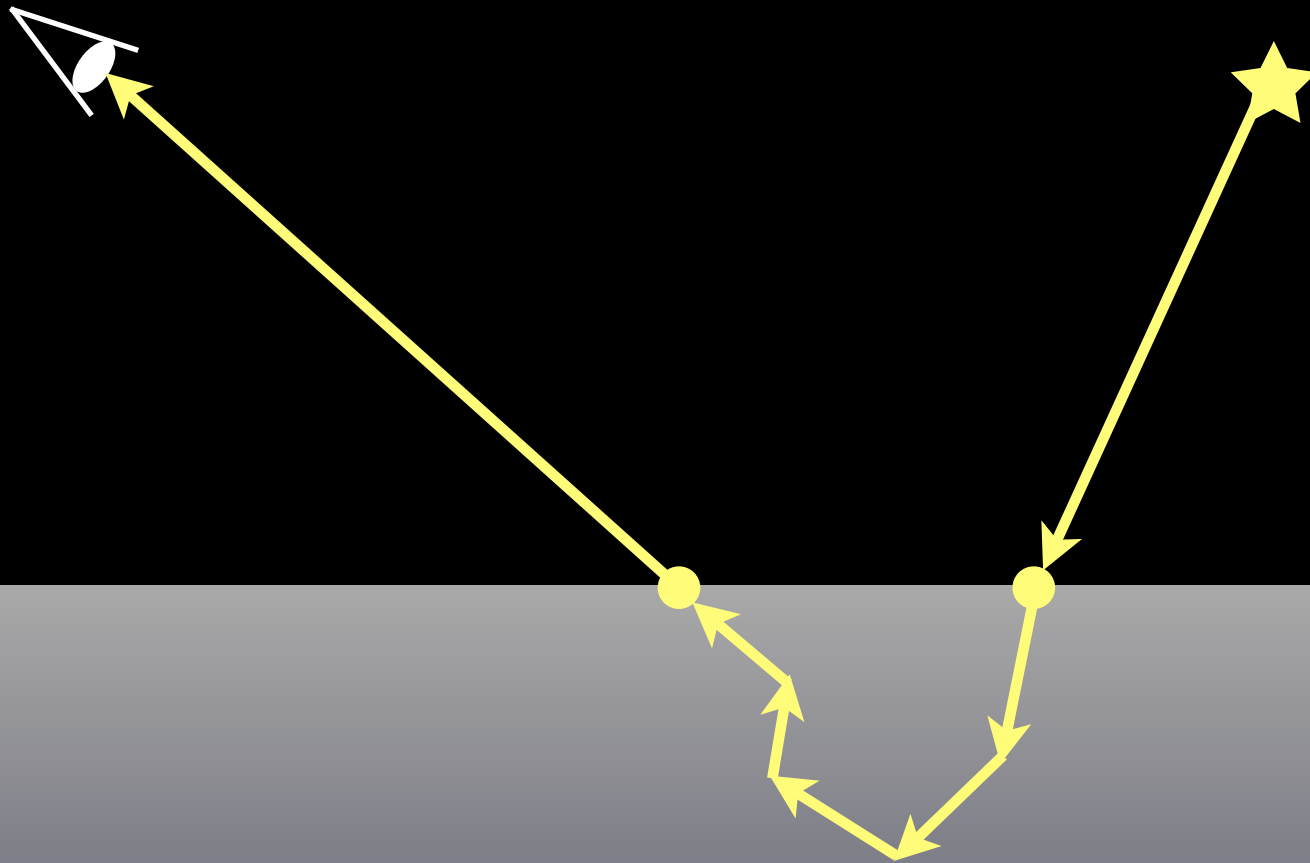
BRDF model
diffuse milk



Bidirectional Surface Scattering Reflectance Distribution Function



Bidirectional Surface Scattering Reflectance Distribution Function



BSSRDF model
skim milk



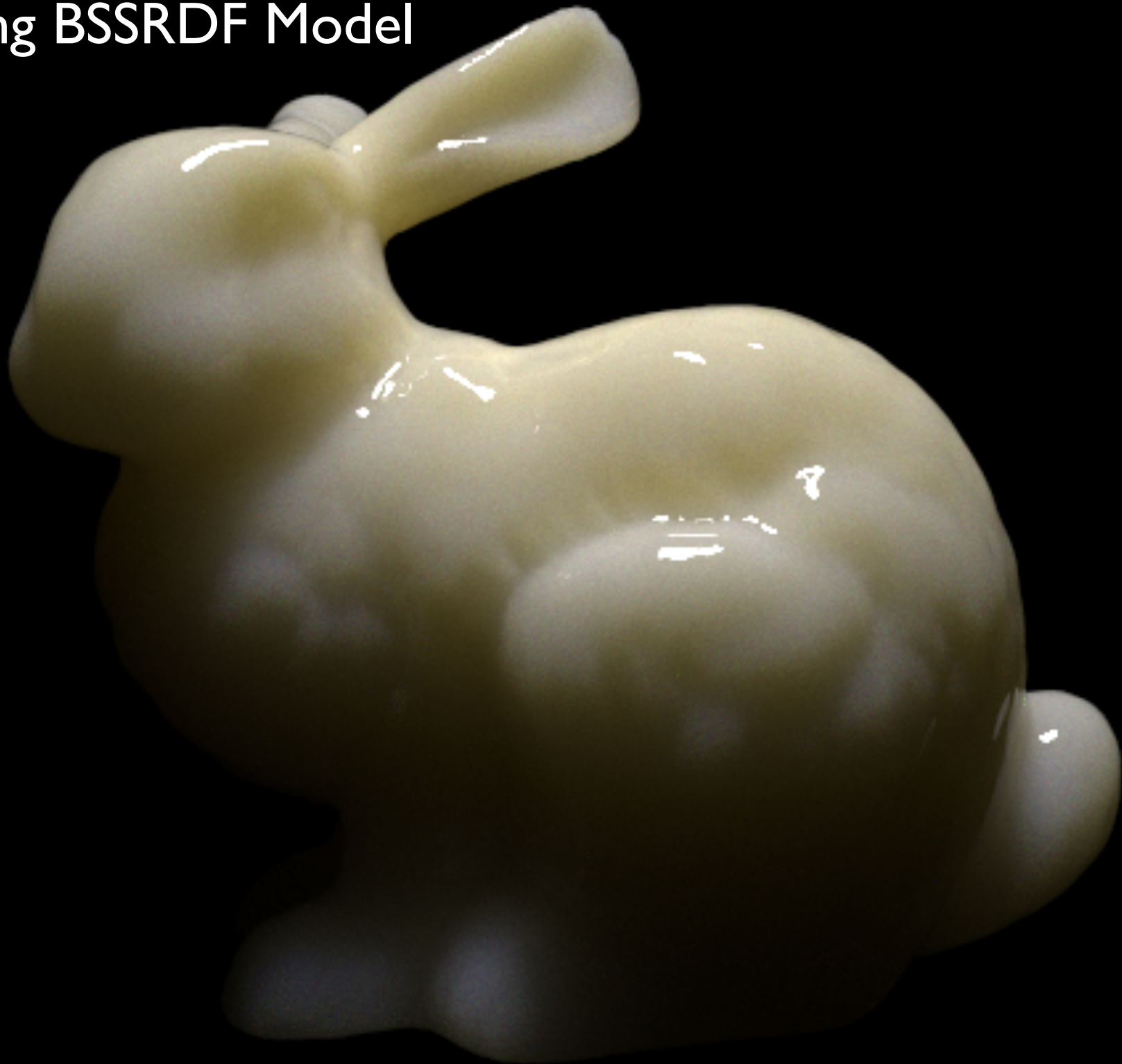
BRDF model diffuse milk



Reference Solution



Existing BSSRDF Model



Our BSSRDF Model



Previous Model A



Our Model



Previous Model B



Reference



Previous Models

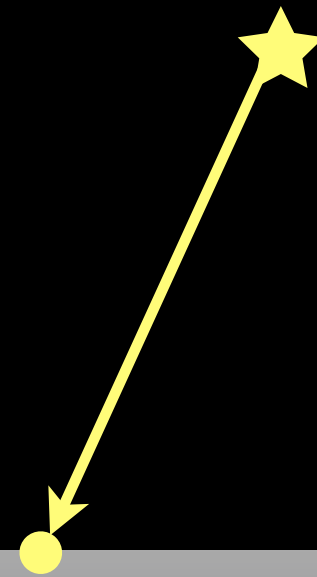
Previous Models

- Dipole [Jensen et al. 2001]
- Multipole [Donner & Jensen 2005]
- Quantized diffusion [d'Eon & Irving 2011]
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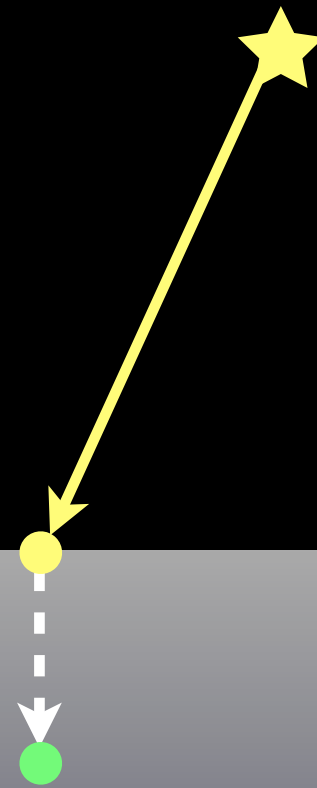
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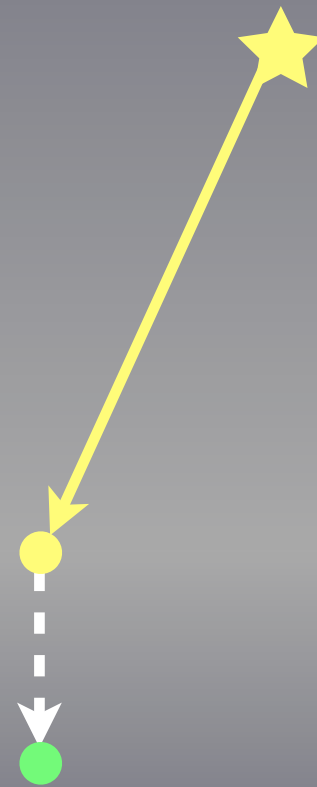
Dipole



Dipole

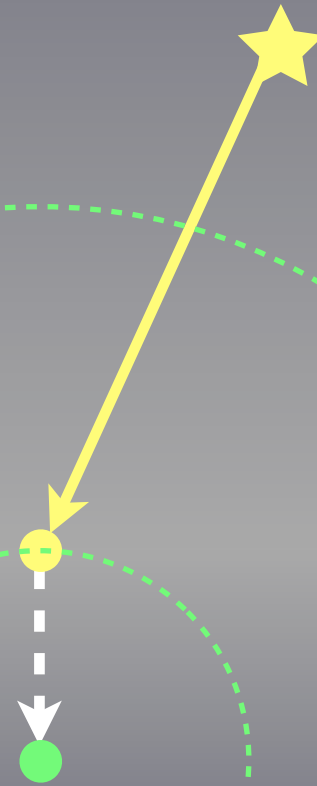


Dipole

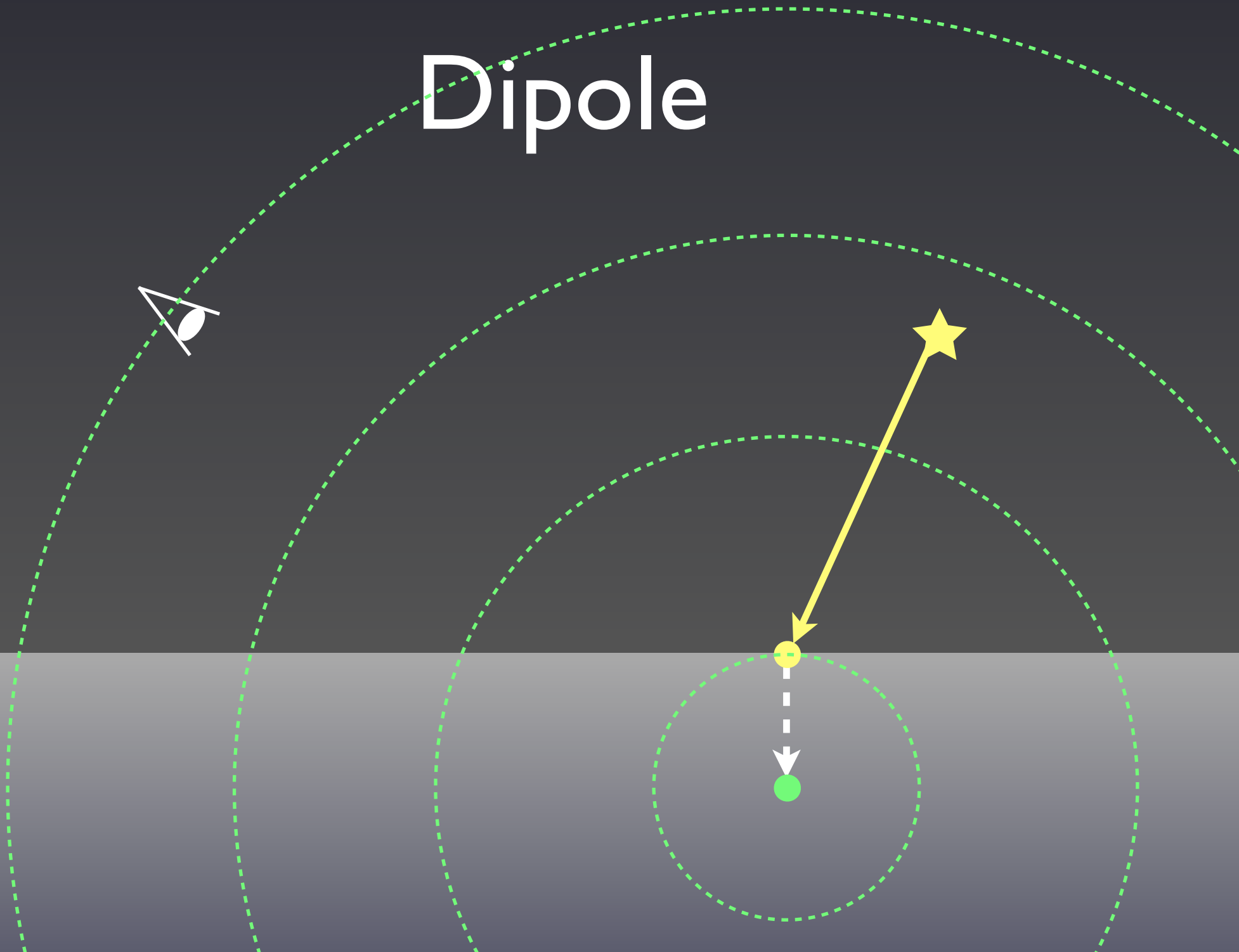


Dipole

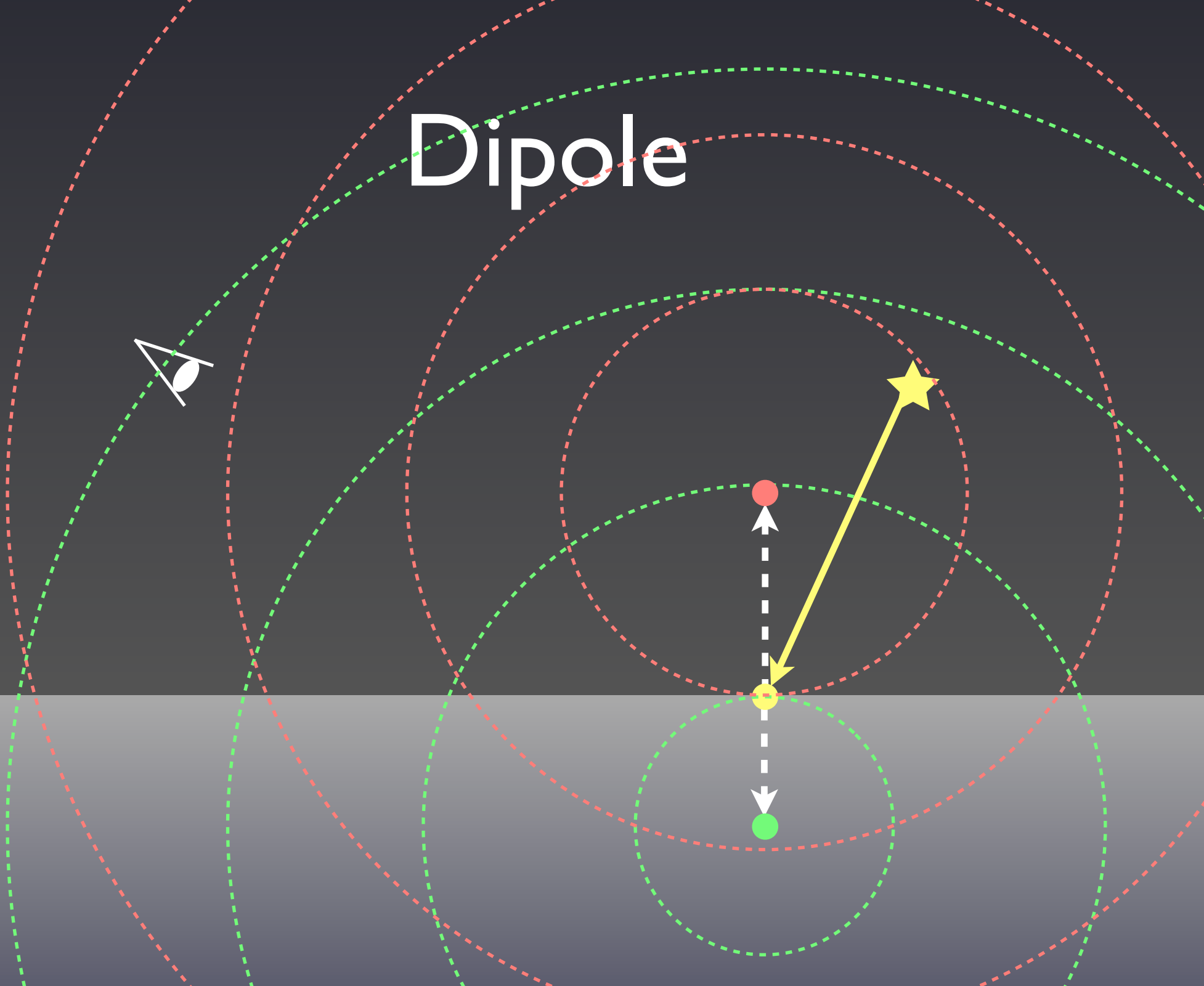
Approximate solution
[Reynolds et al. 1976]



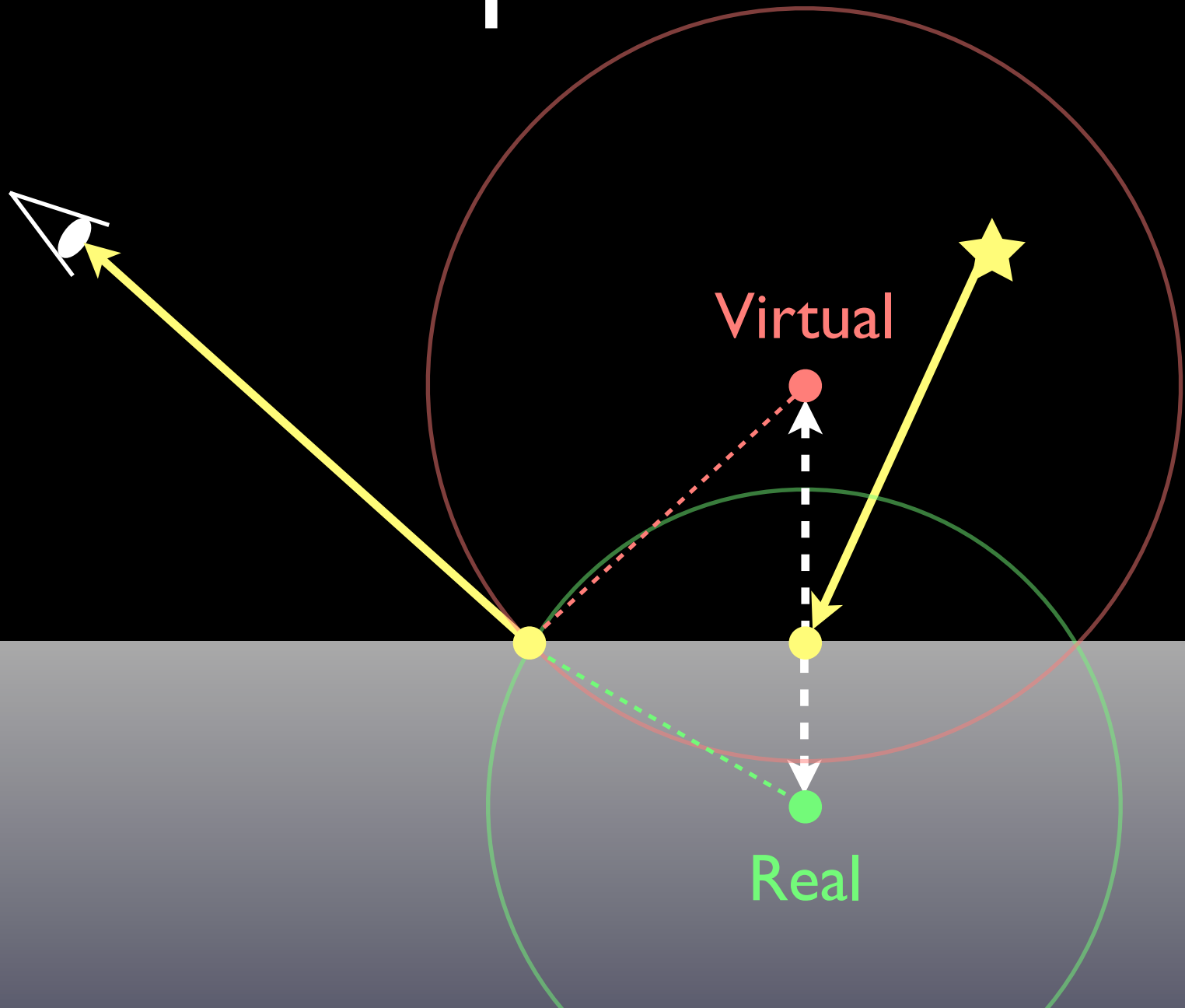
Dipole



Dipole



Dipole



Dipole



Diffuse BRDF

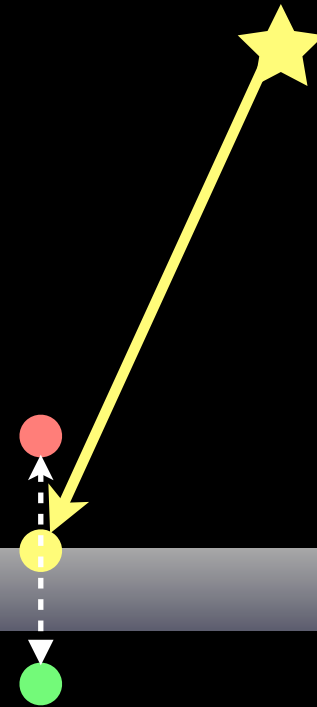


Dipole BSSRDF

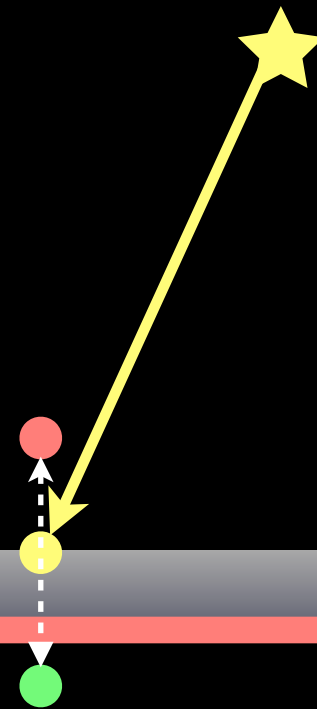
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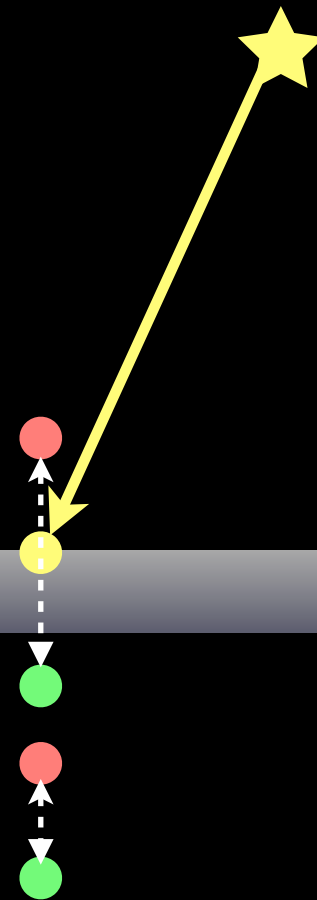
Multipole



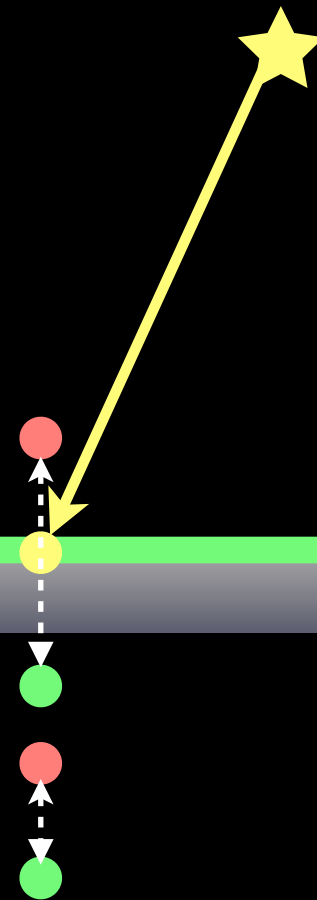
Multipole



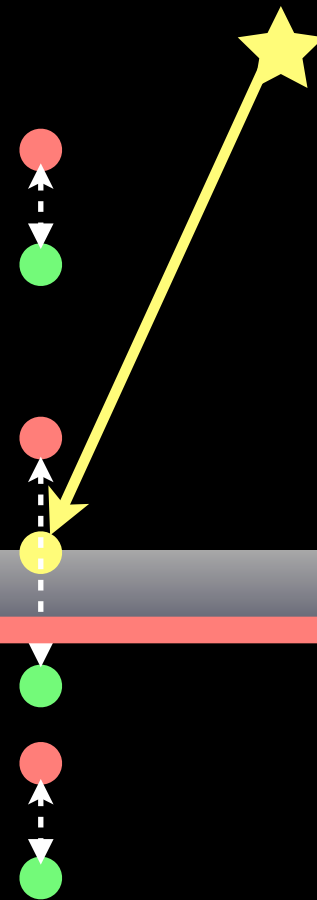
Multipole



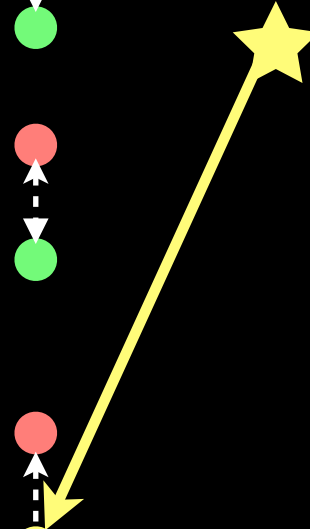
Multipole



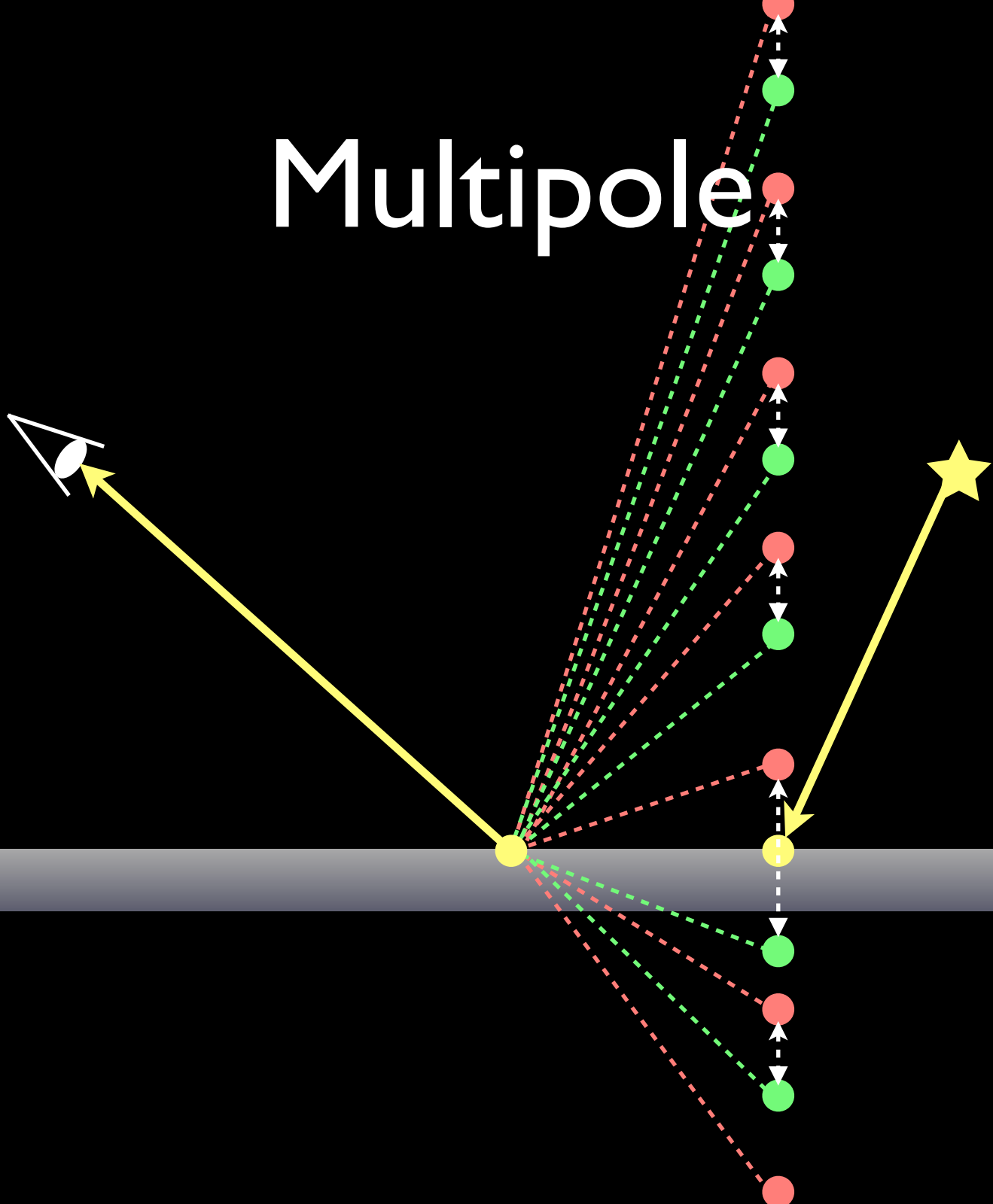
Multipole



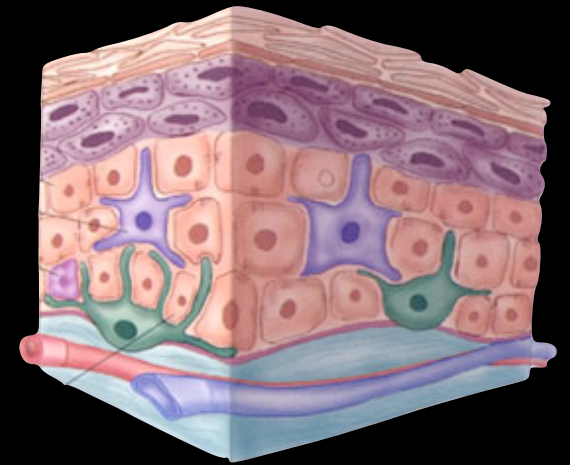
Multipole



Multipole



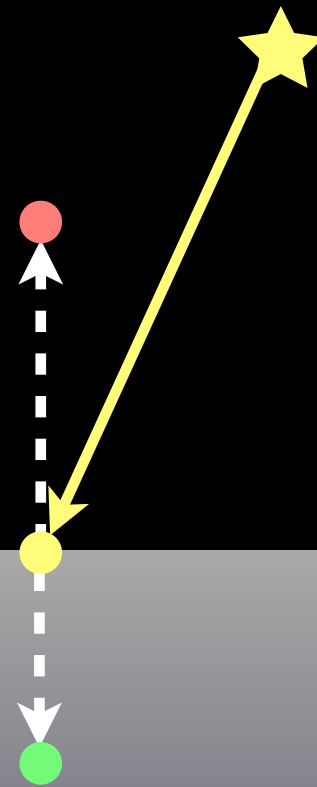
Multipole



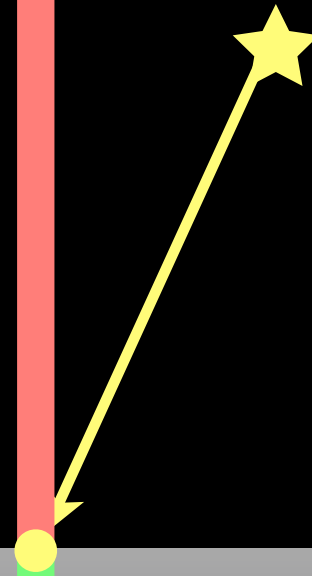
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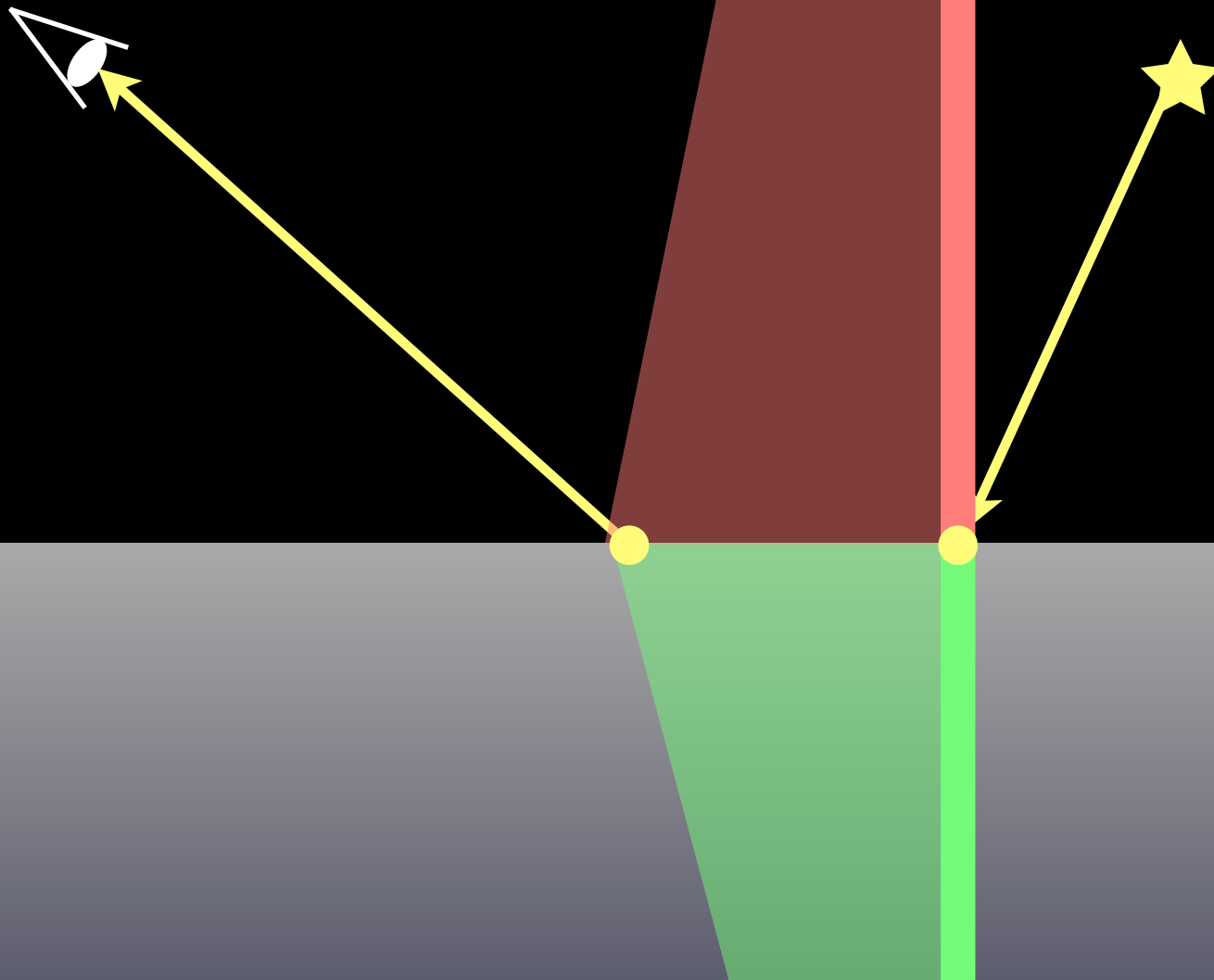
Quantized Diffusion



Quantized Diffusion



Quantized Diffusion



Quantized Diffusion



Dipole

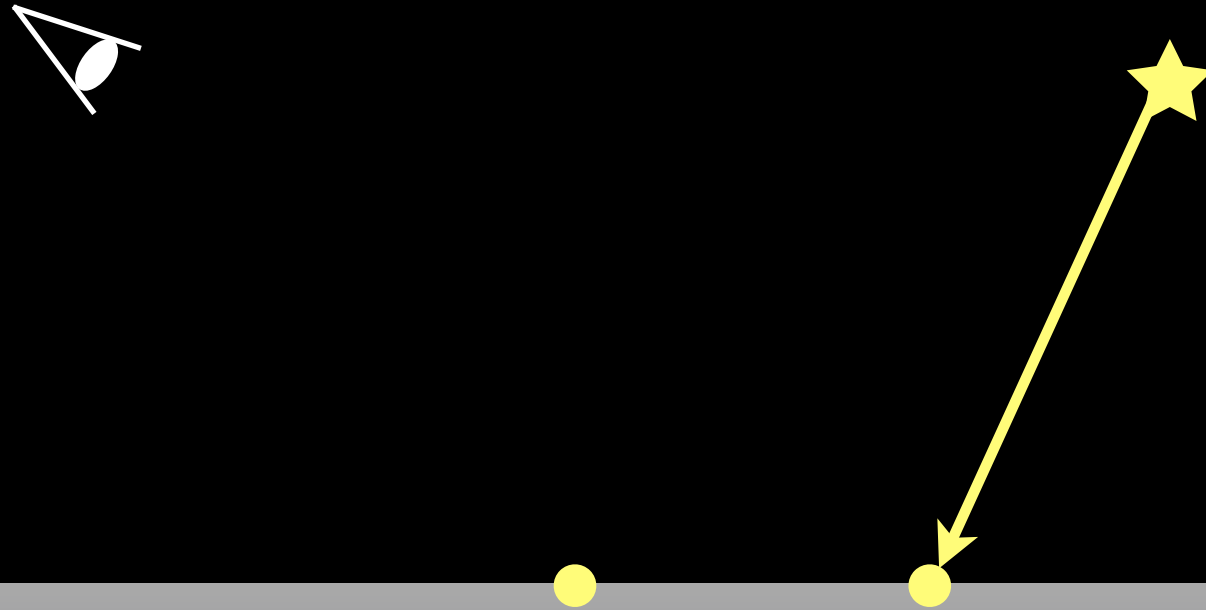


Quantized Diffusion

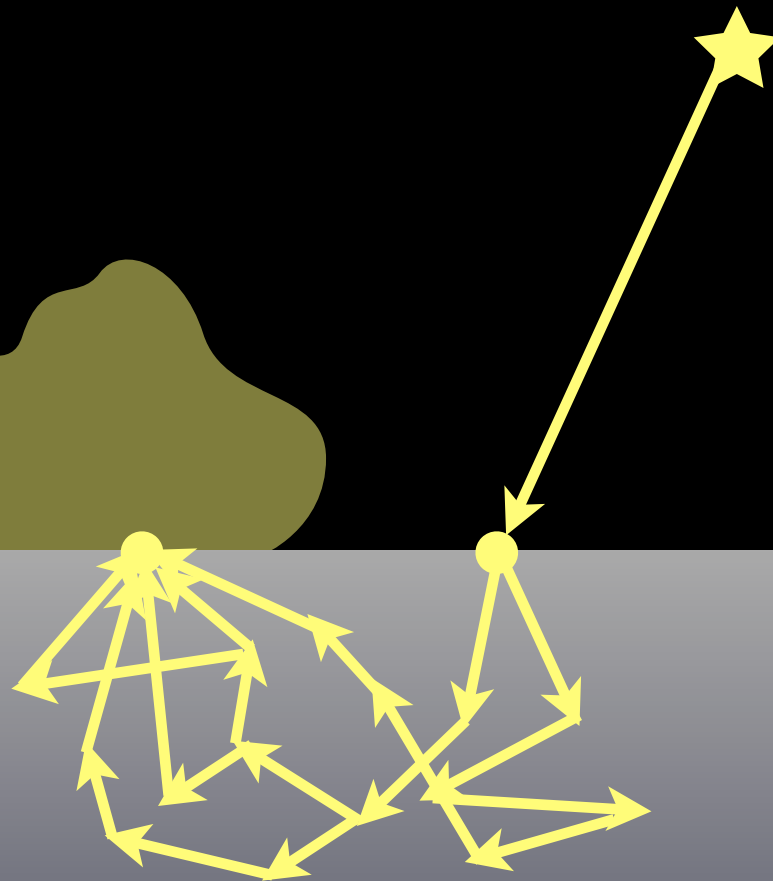
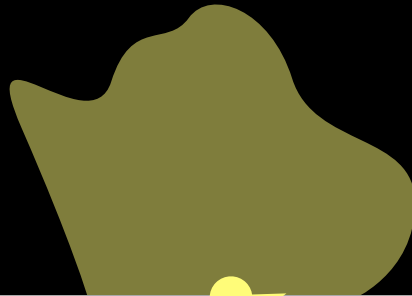
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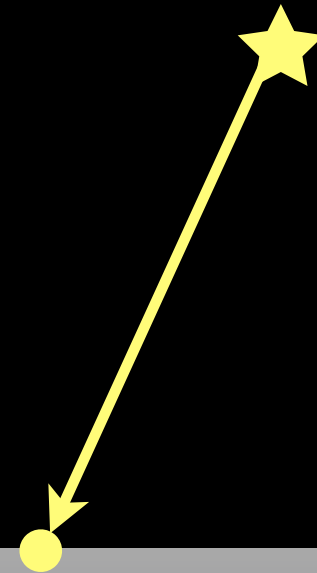
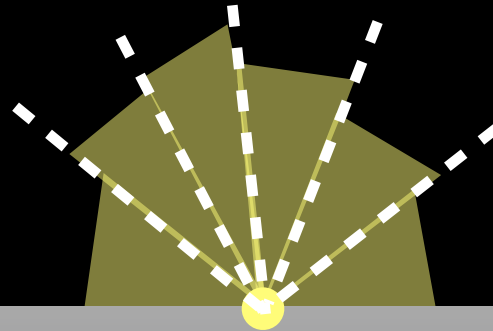
Precomputed BSSRDF



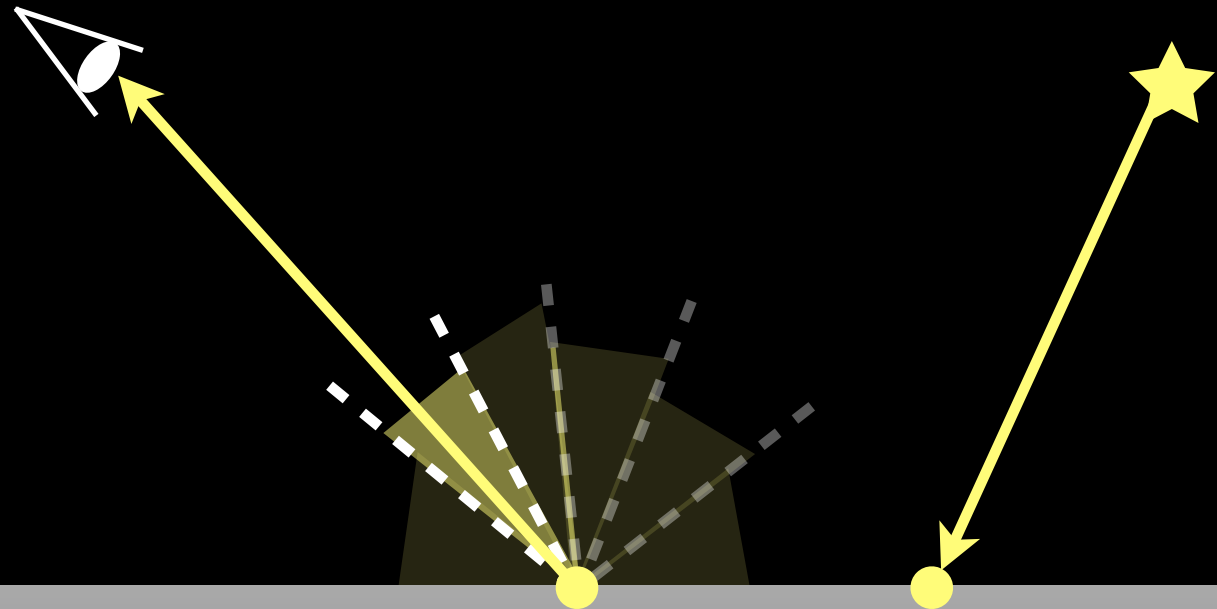
Precomputed BSSRDF



Precomputed BSSRDF



Precomputed BSSRDF



Precomputed BSSRDF



Reference
(30 hours)



Dipole
(10 min)

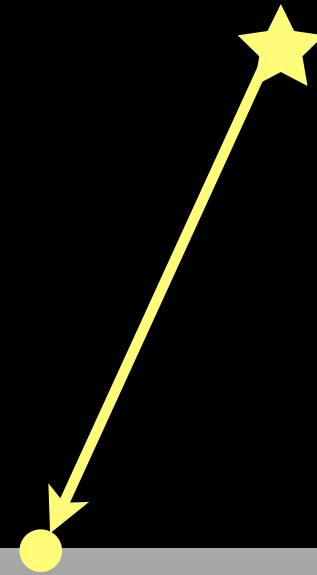


Precomputed
(30 min)

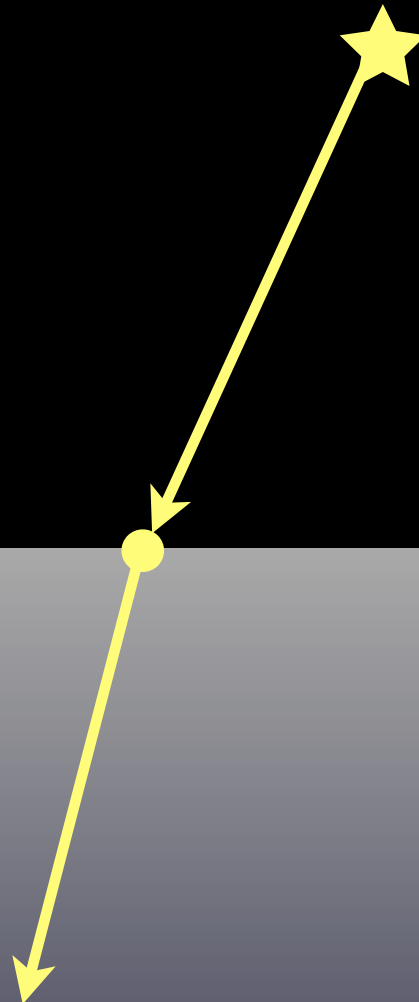
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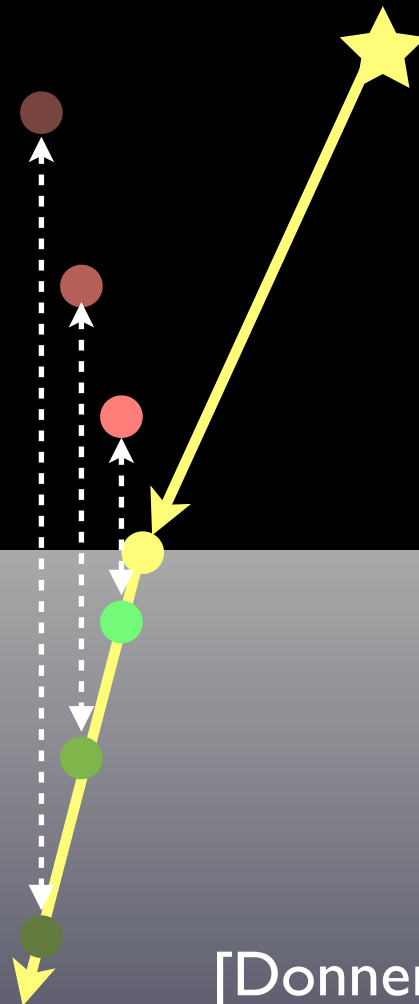
Photon Diffusion



Photon Diffusion

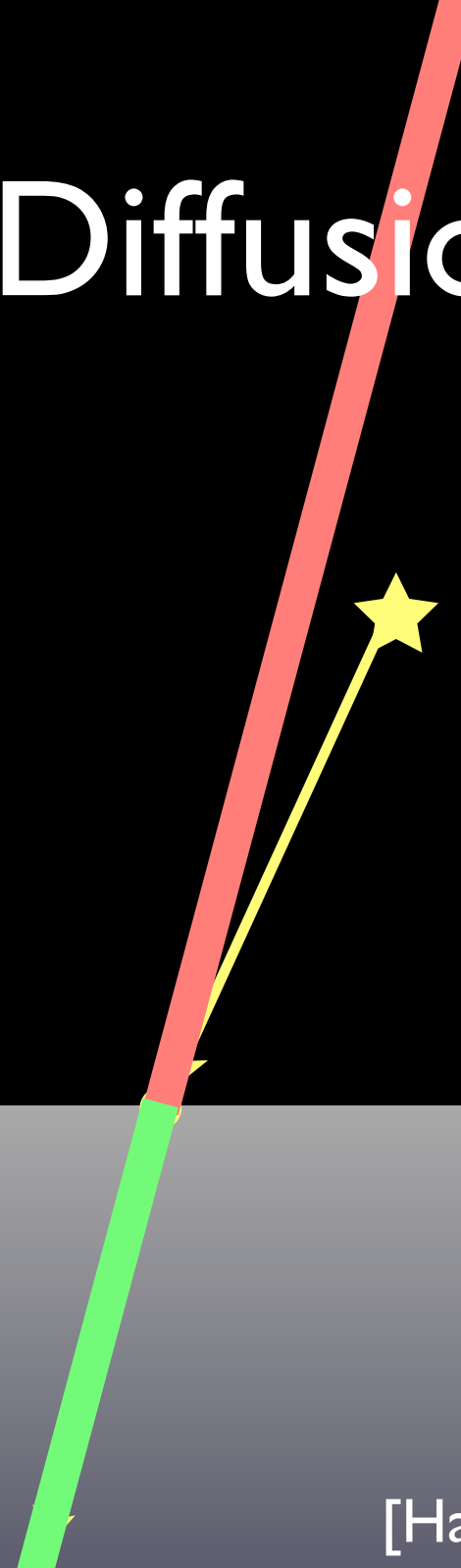


Photon Diffusion



[Donner & Jensen 2007]

Photon Beam Diffusion



Photon Diffusion



Dipole



Photon Diffusion

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- Ignores incoming light direction
 - Requires no precomputation
 - Provides fully analytical function

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- Considers incoming light direction
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- Photon diffusion [Donner & Jensen 2007] [Habel et al. 2013]
 - Considers incoming light direction
 - Requires no precomputation
 - Relies on numerical integration

Contributions

- First BSSRDF which...
 - Considers incoming light direction
 - Requires no precomputation
 - Provides fully analytical function

Dipole



Our Model



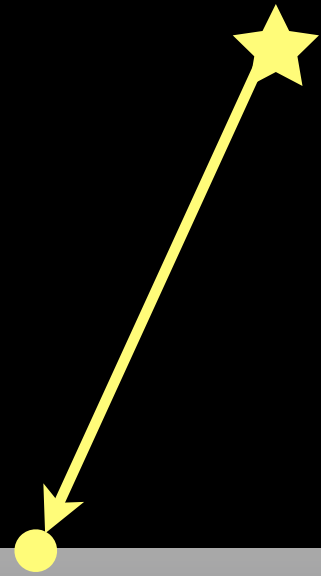
Quantized

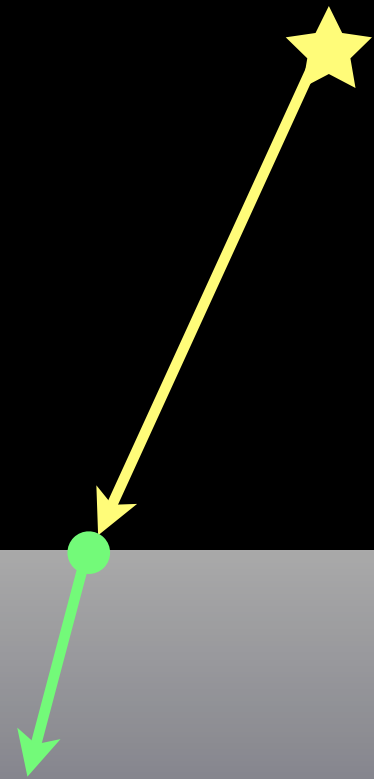


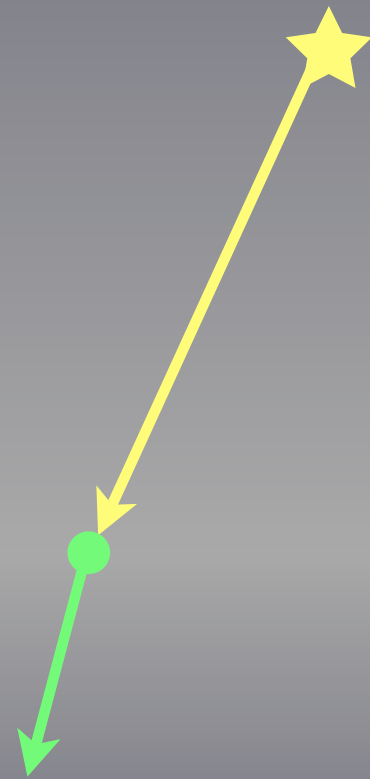
Reference



Idea

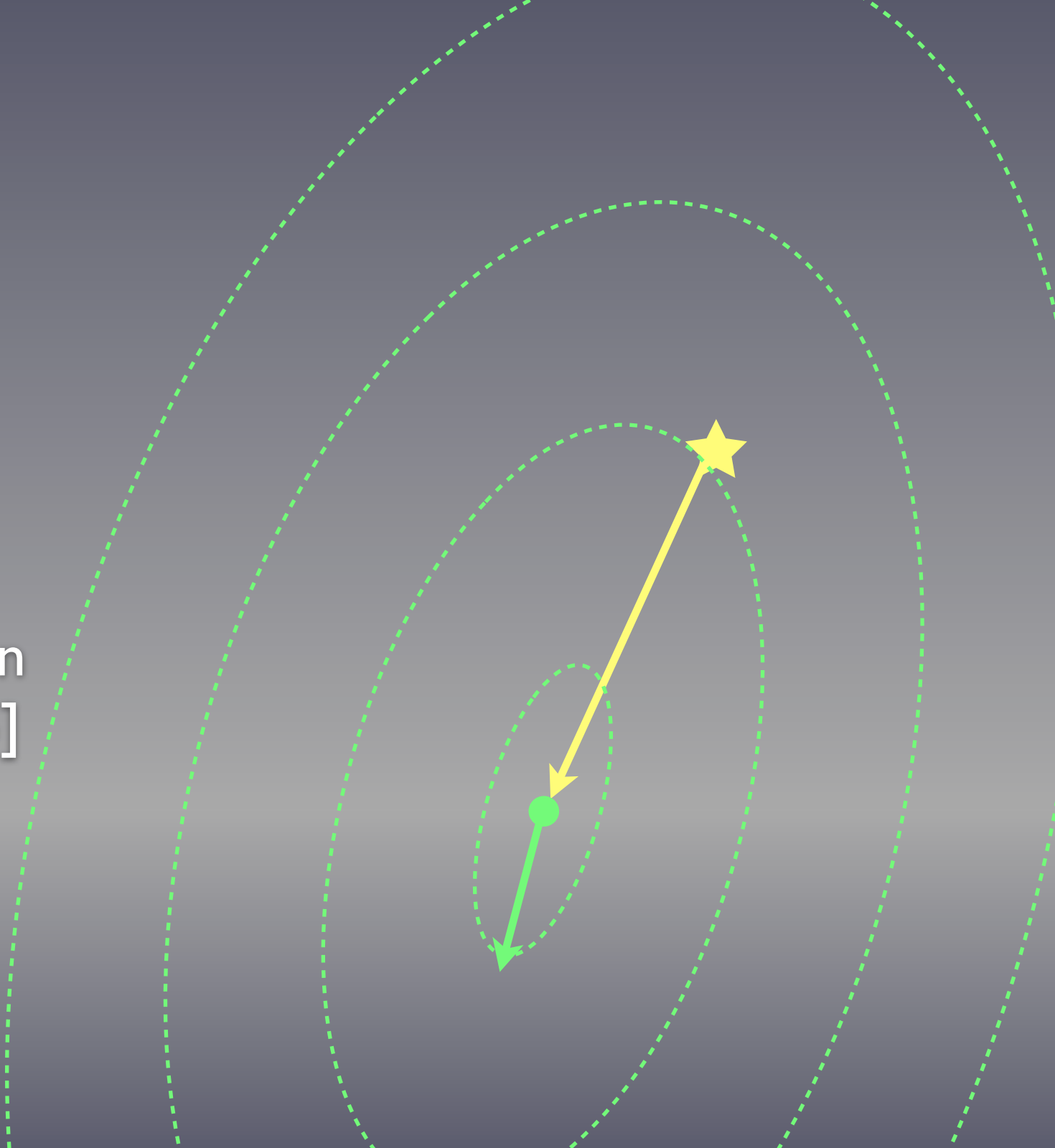


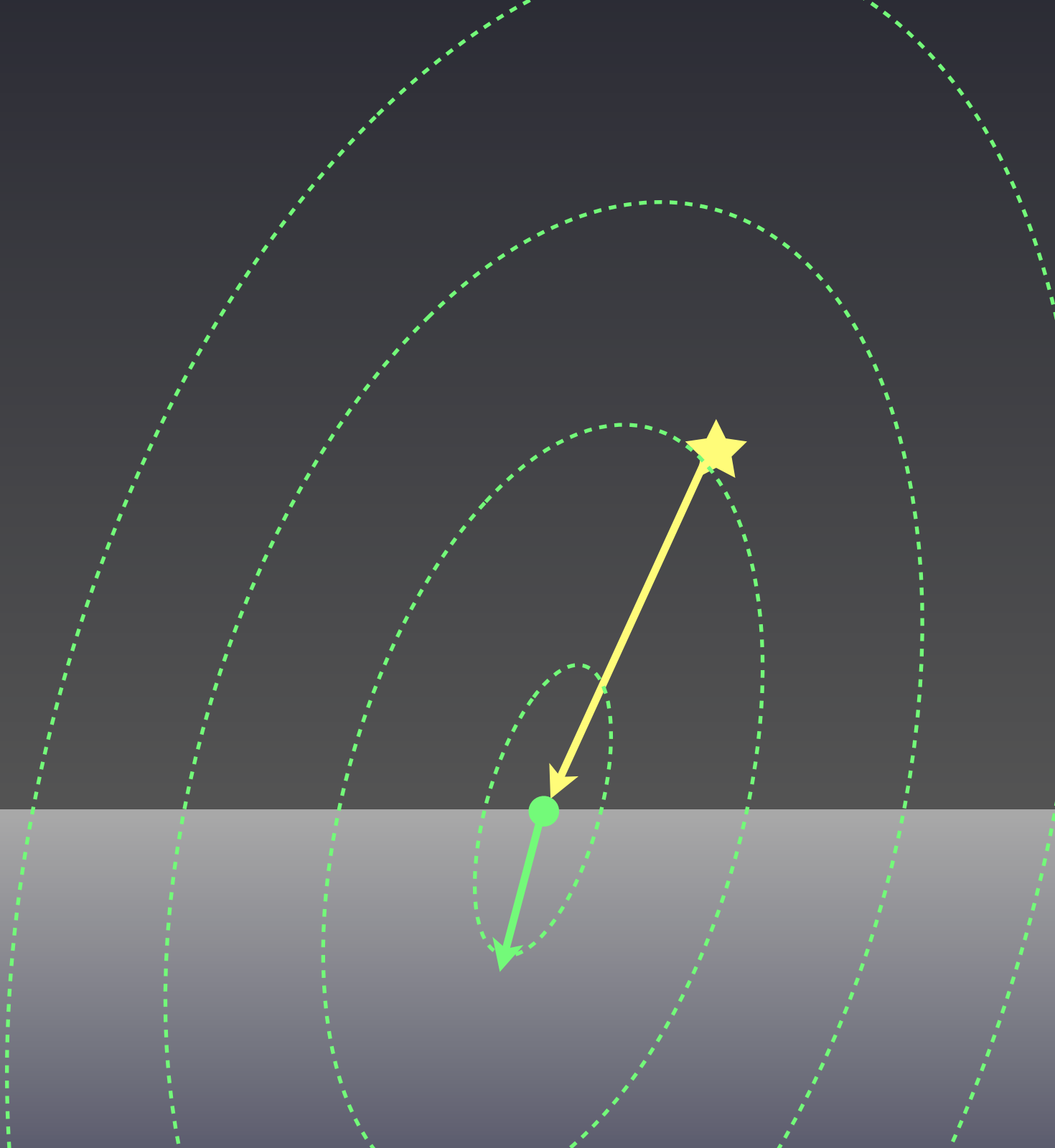






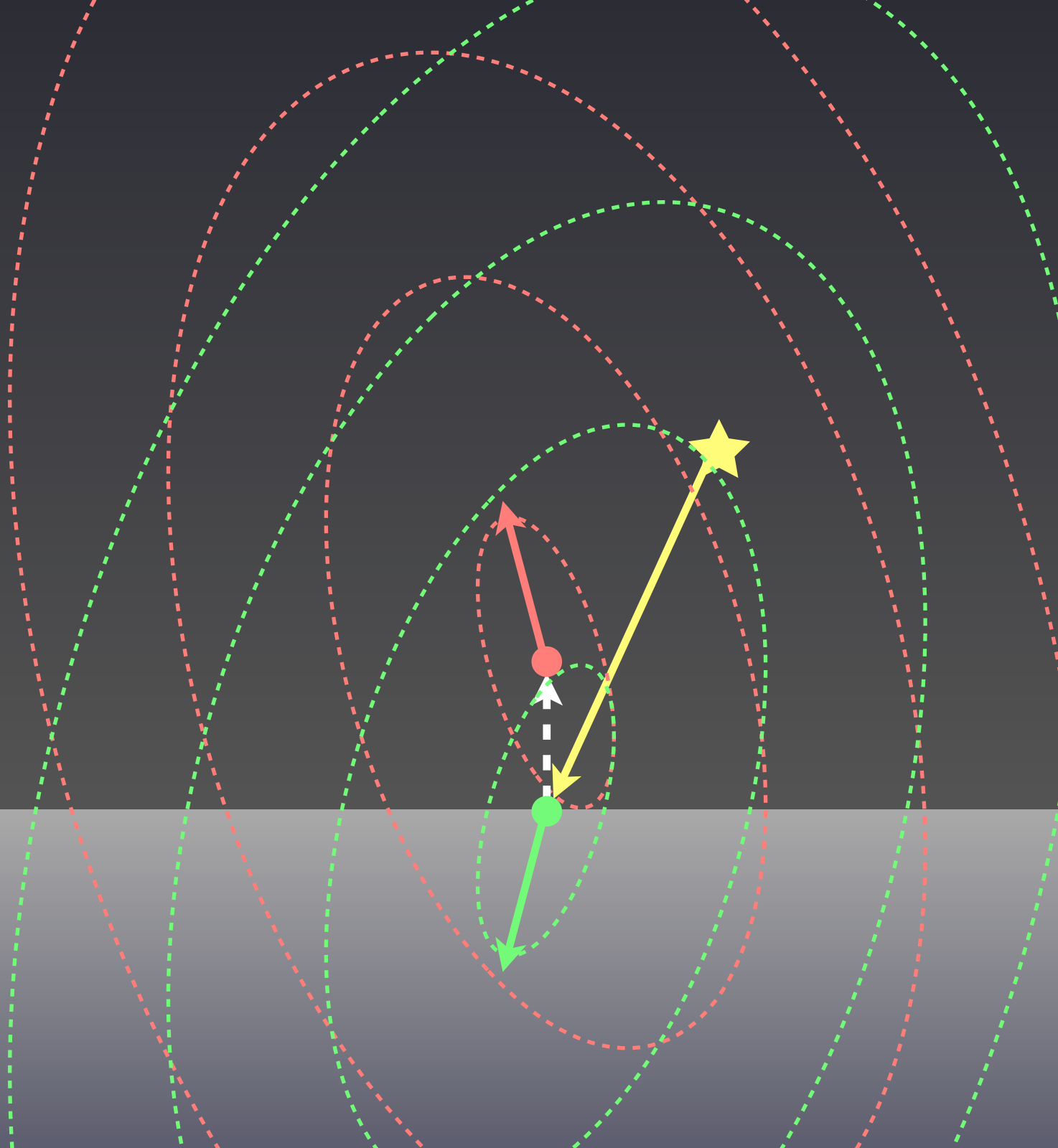
Directional solution
[Menon et al. 2005]

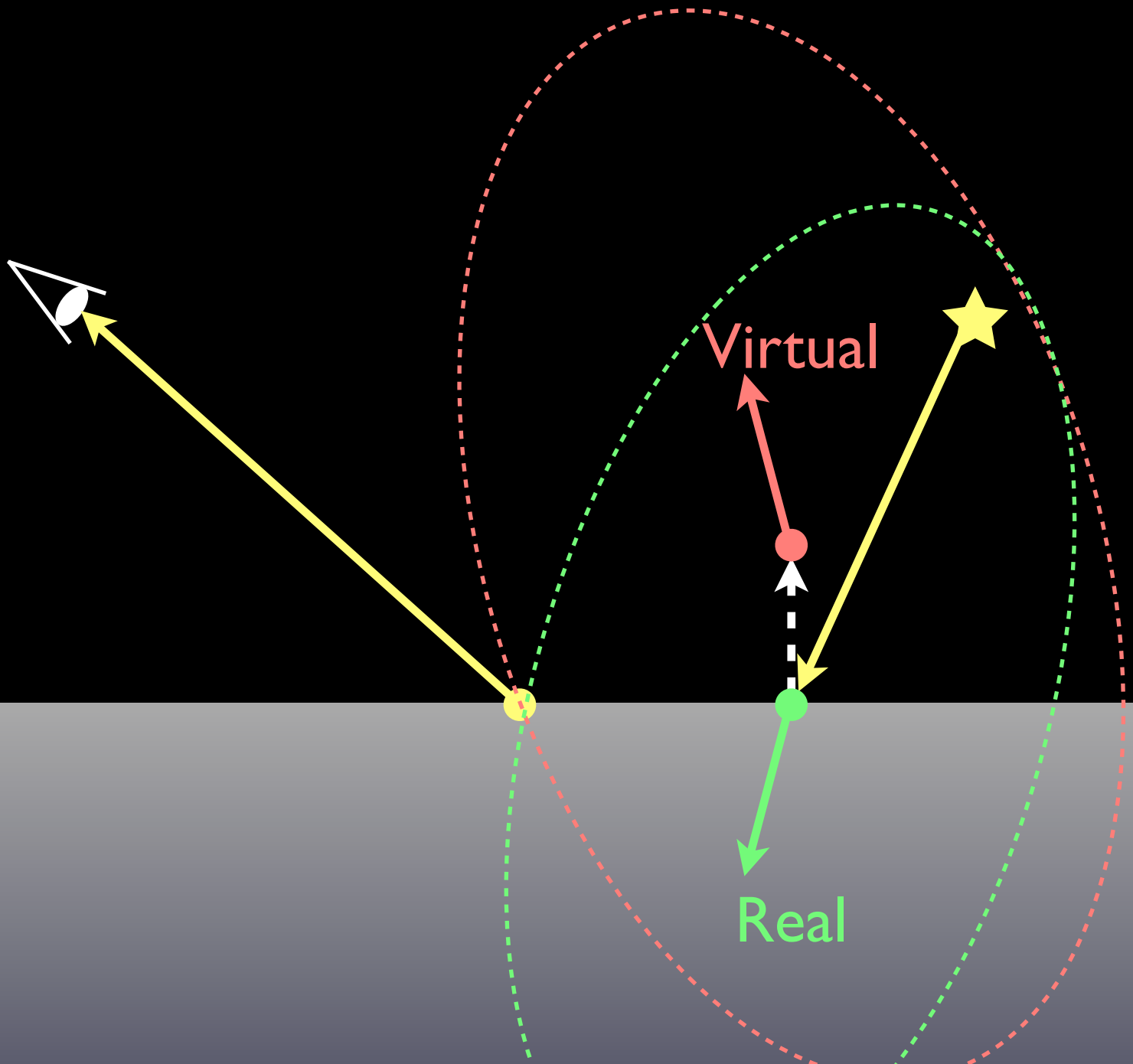




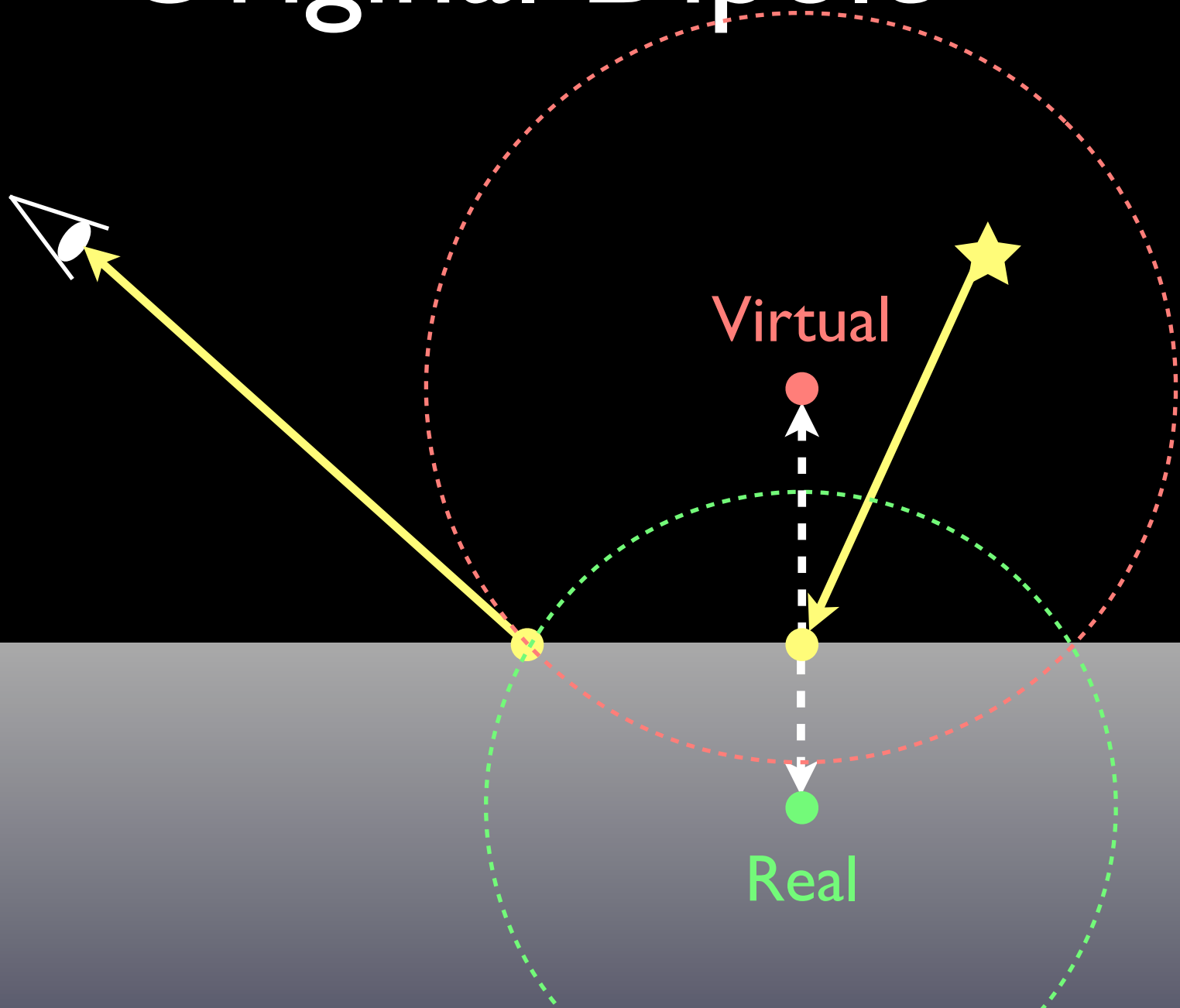


Mirror direction
&
Offset location

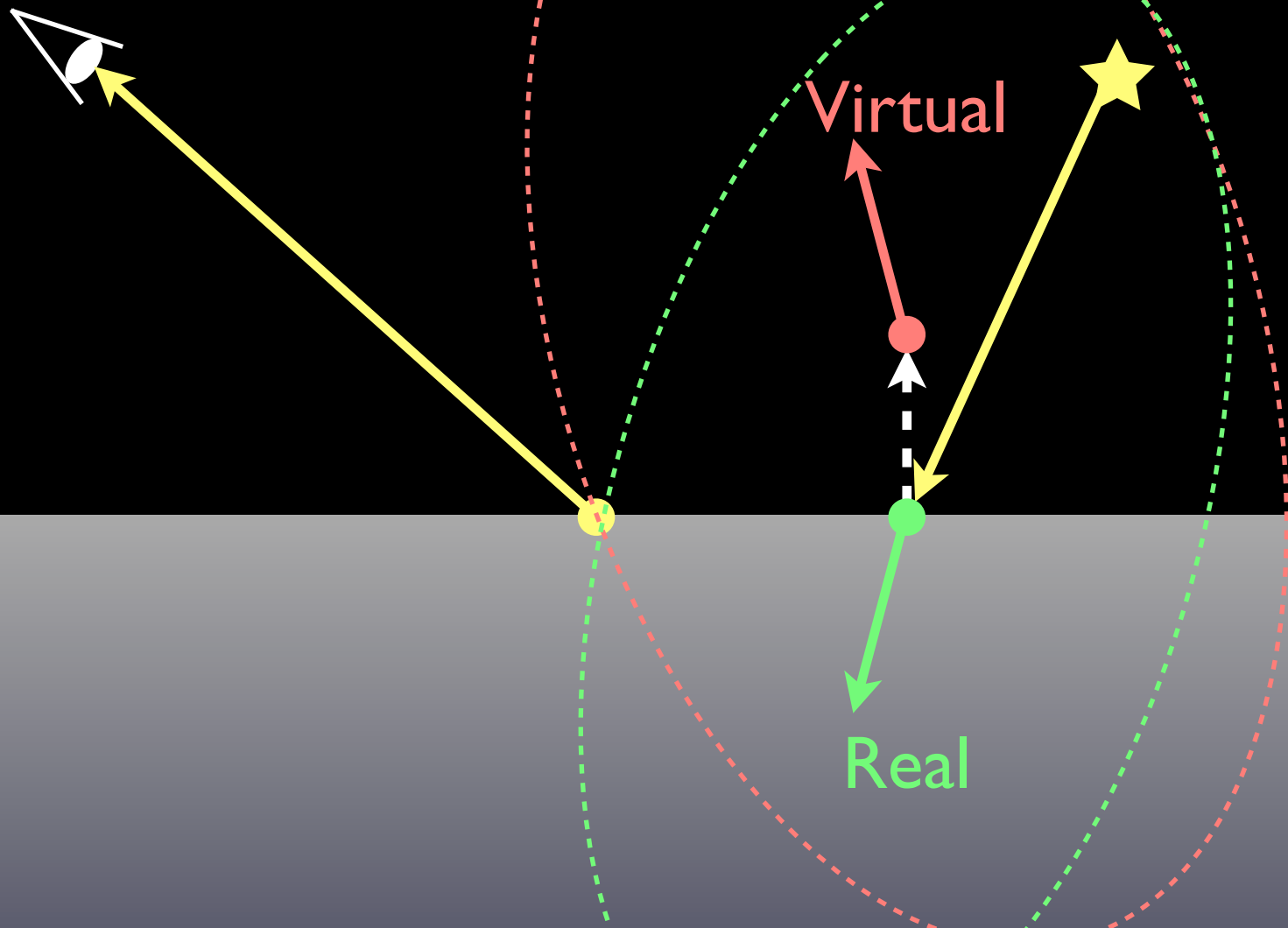




Original Dipole



Directional Dipole



Two Challenges

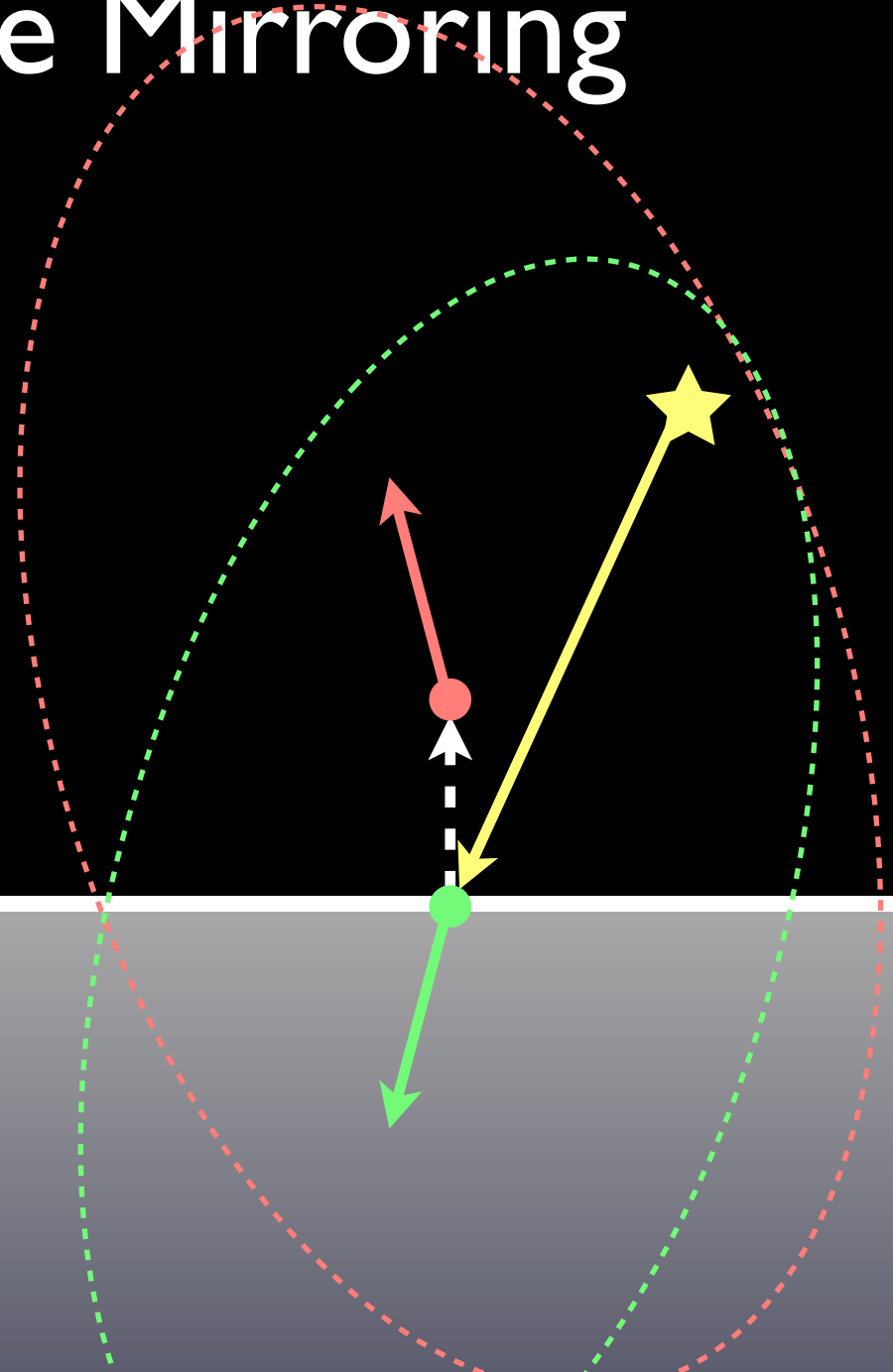
- Mirroring sources is unstable
- Singularity at the real source

Two Challenges

- Mirroring sources is unstable
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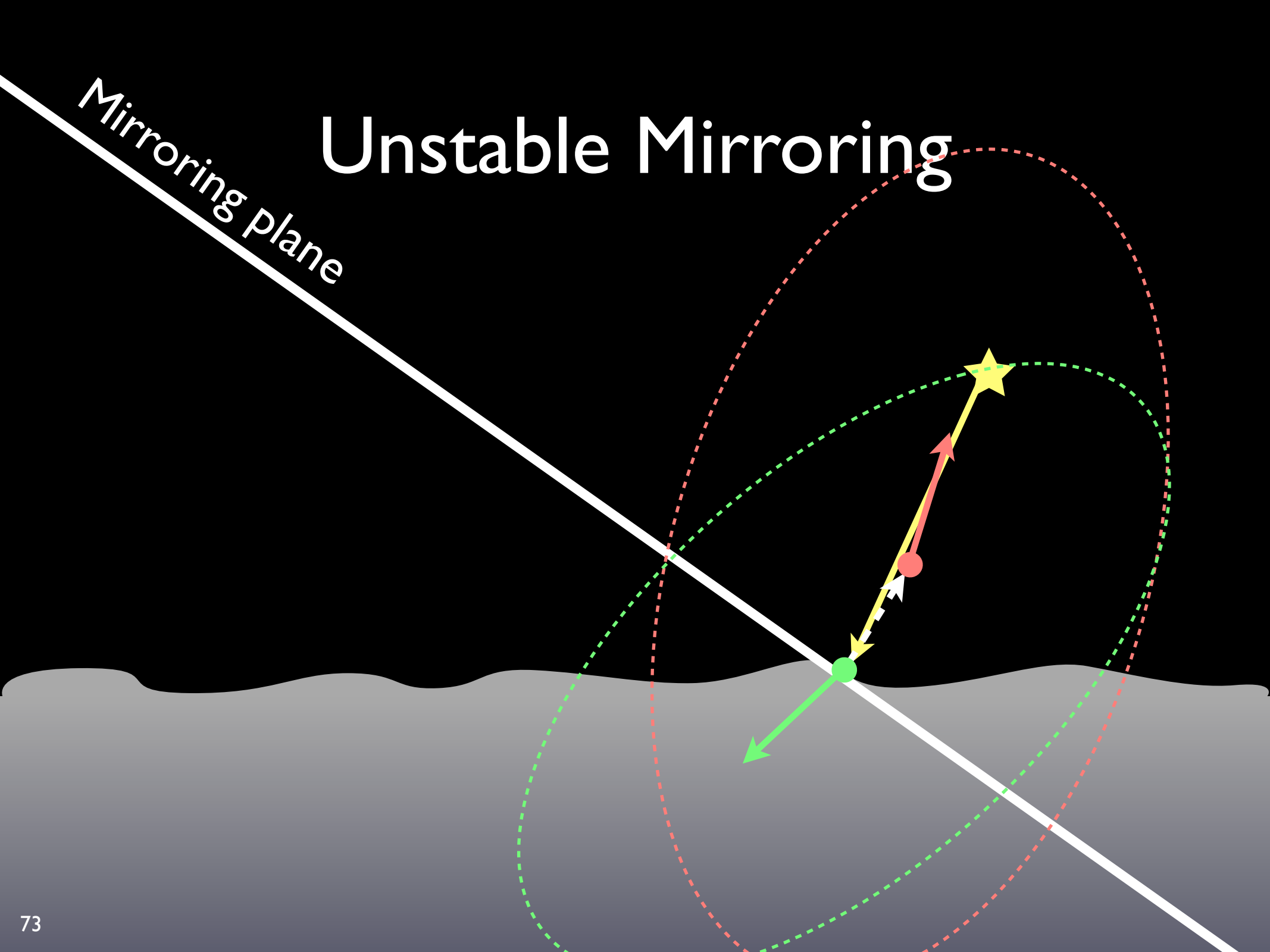
Unstable Mirroring

Mirroring plane

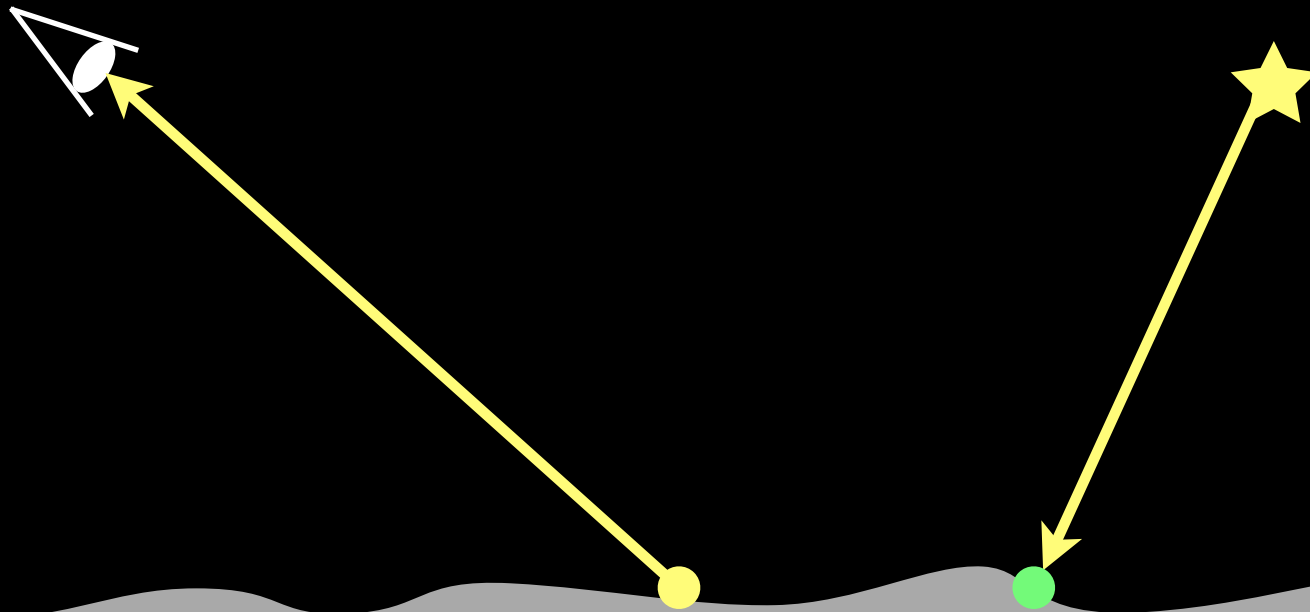


Unstable Mirroring

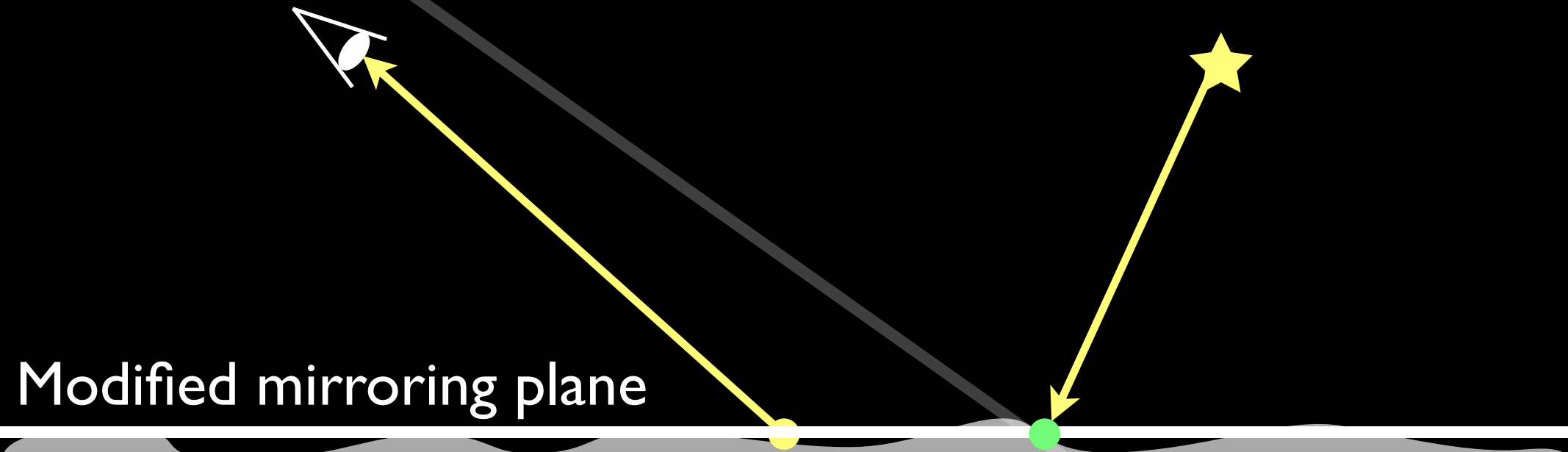
Mirroring plane



Modified Mirroring Plane

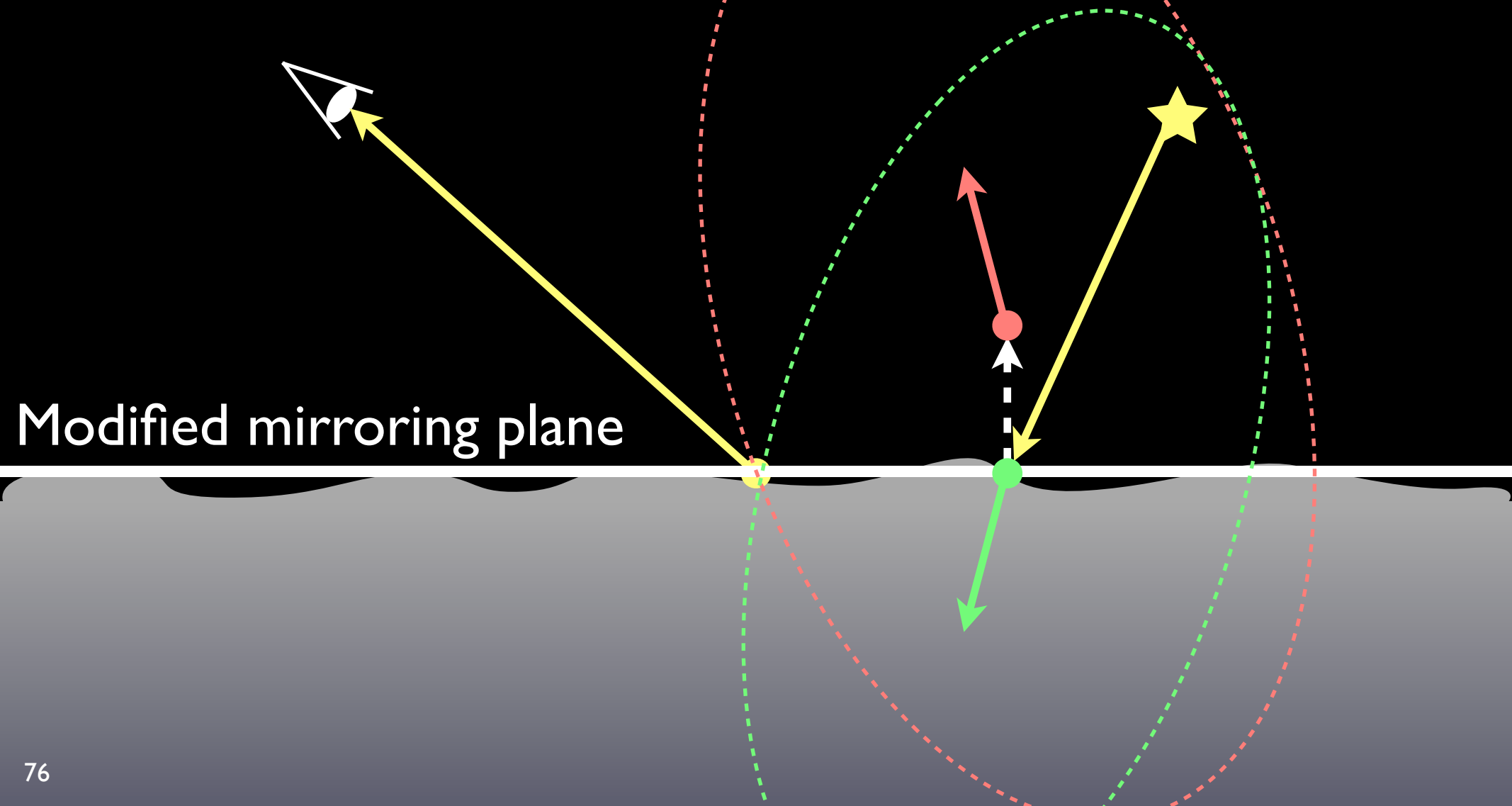


Modified Mirroring Plane



Modified mirroring plane

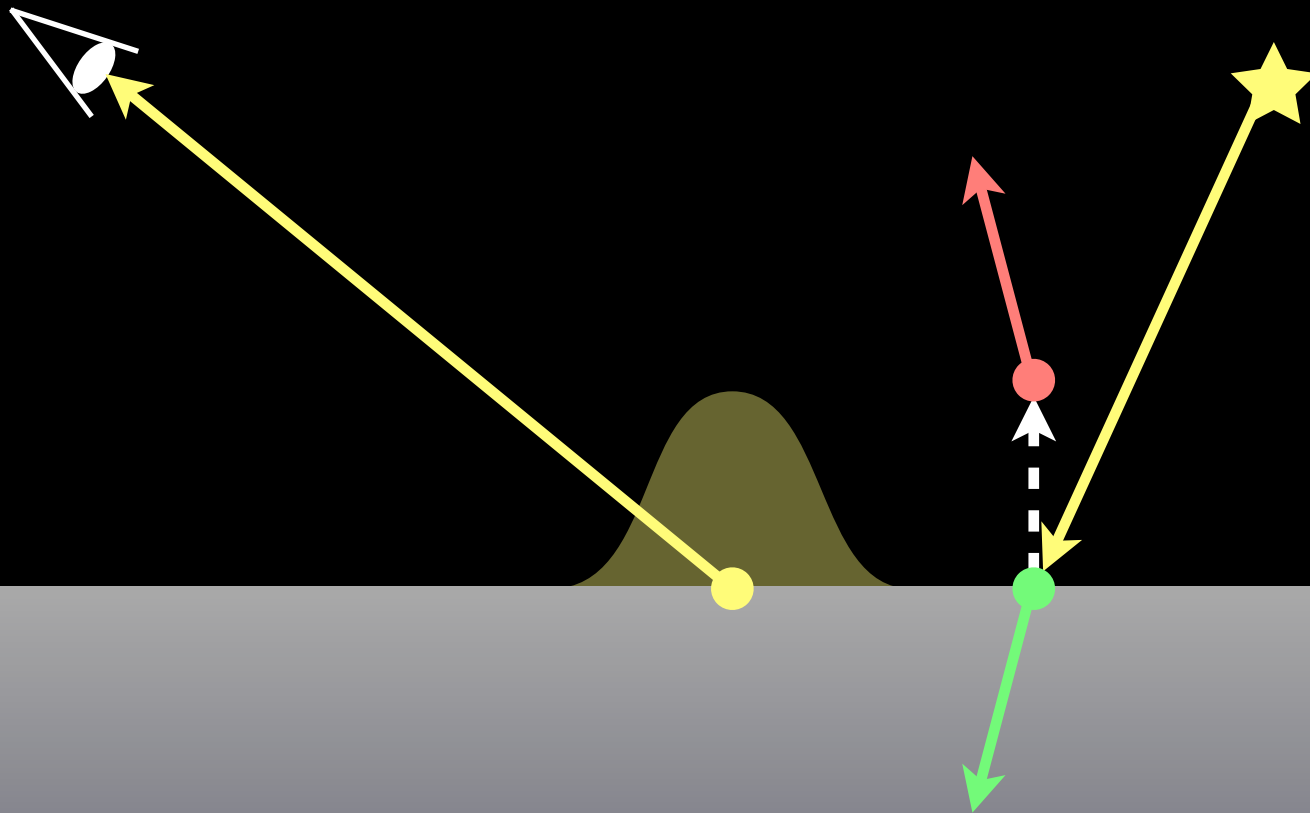
Modified Mirroring Plane



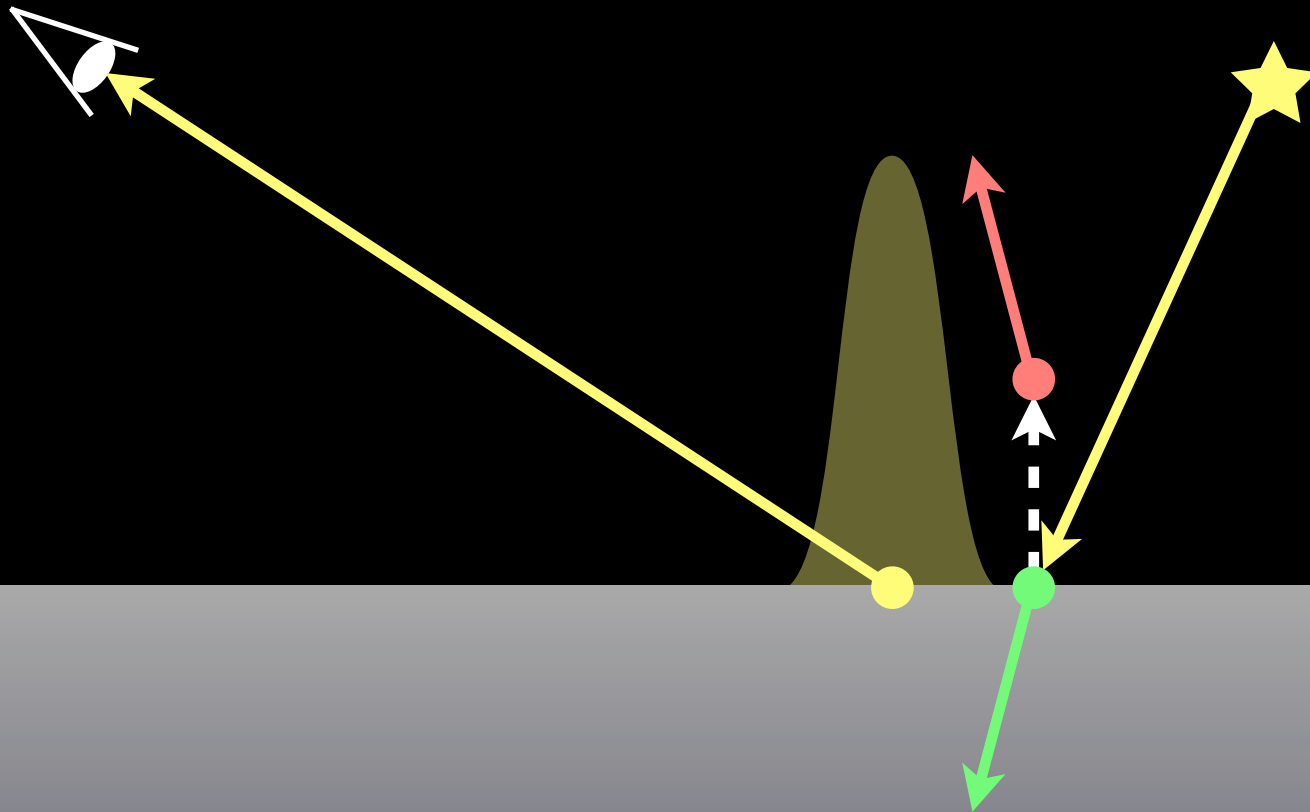
Two Challenges

- Mirroring sources is unstable
- Singularity at the real source

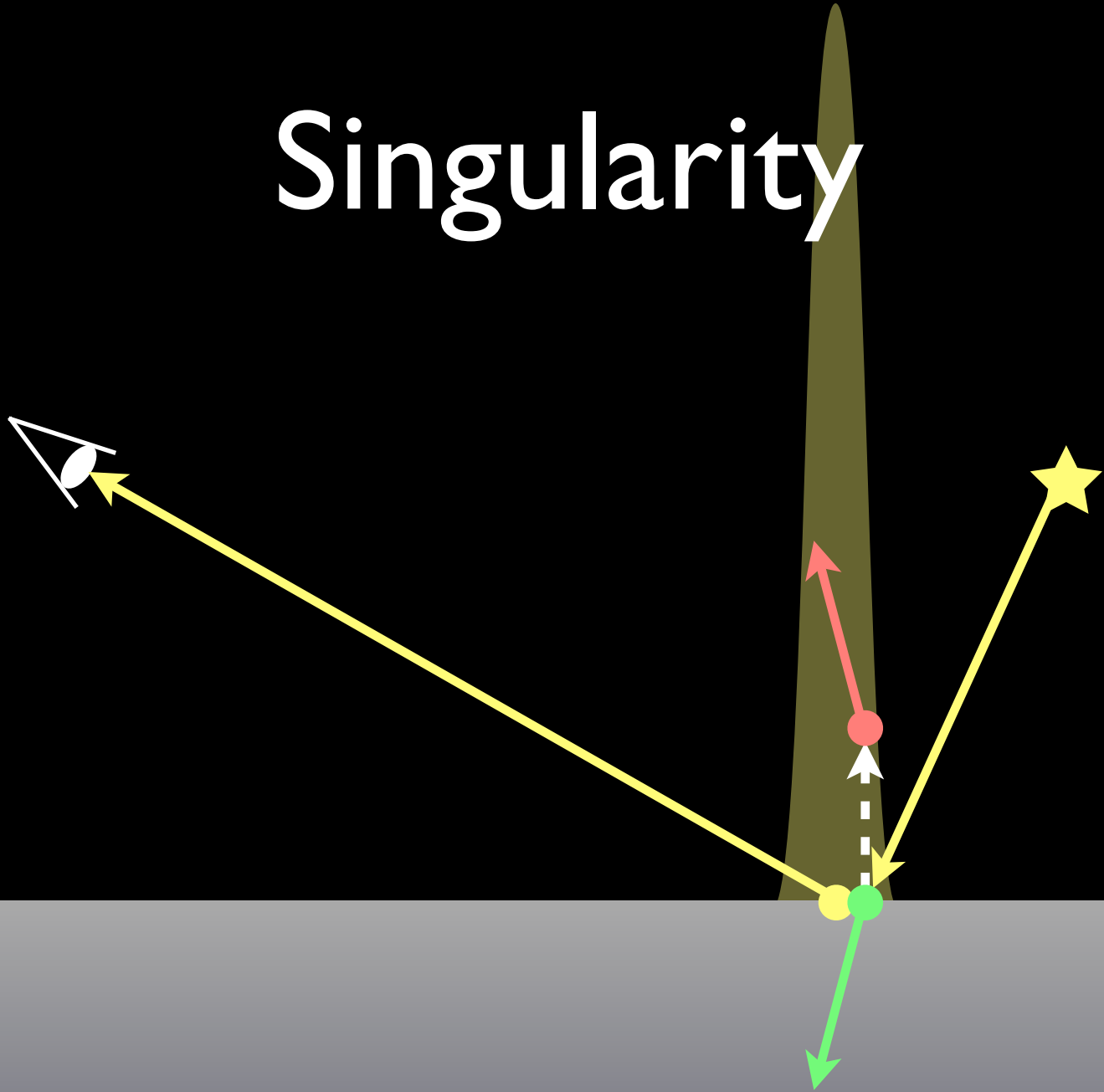
Singularity



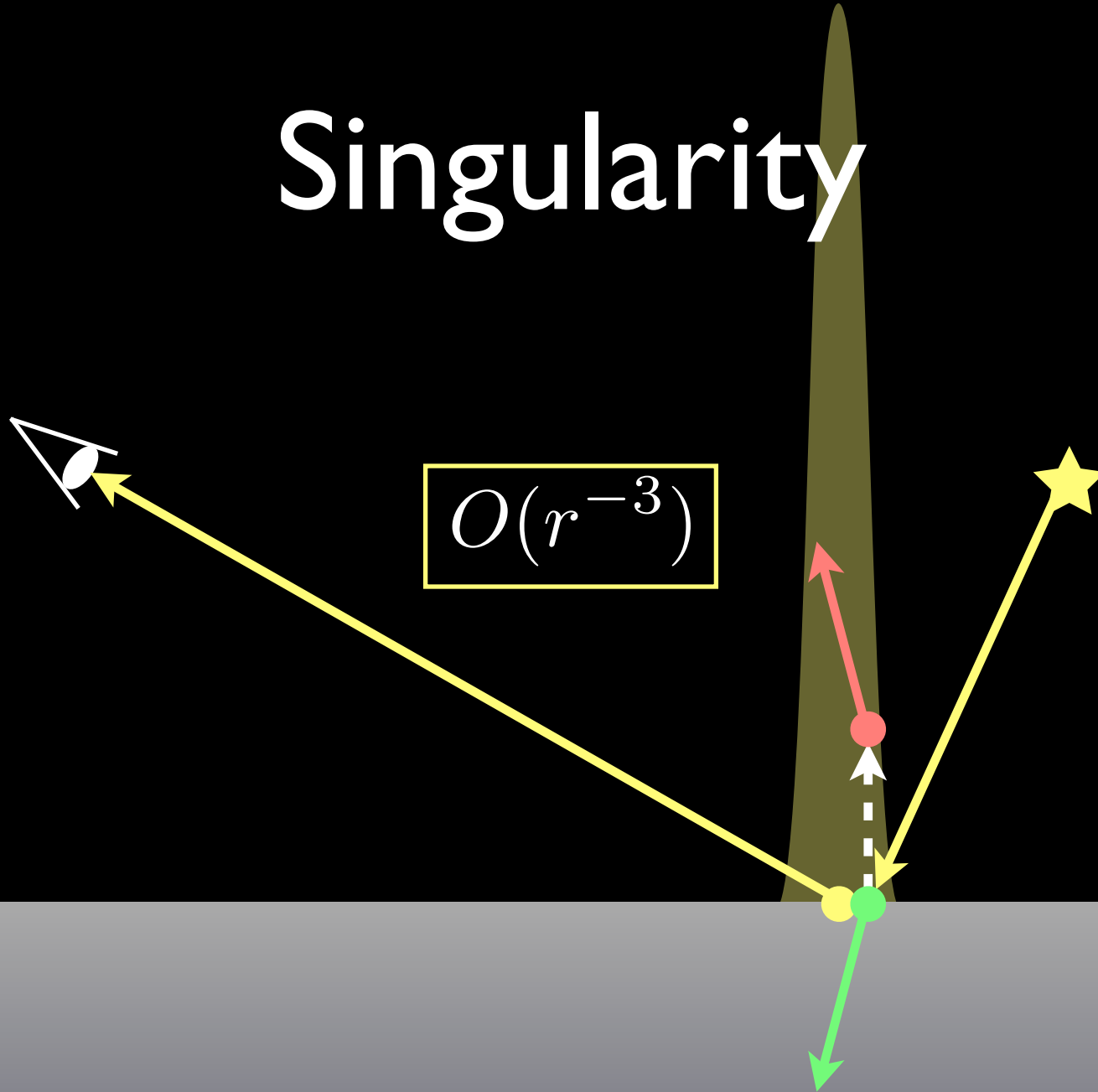
Singularity



Singularity



Singularity



Distance Correction

- Inspired by the correction technique in computational physics [Elliot 86]

$$\boxed{r'} = \sqrt{\boxed{r}^2 + \boxed{z_0}^2}$$

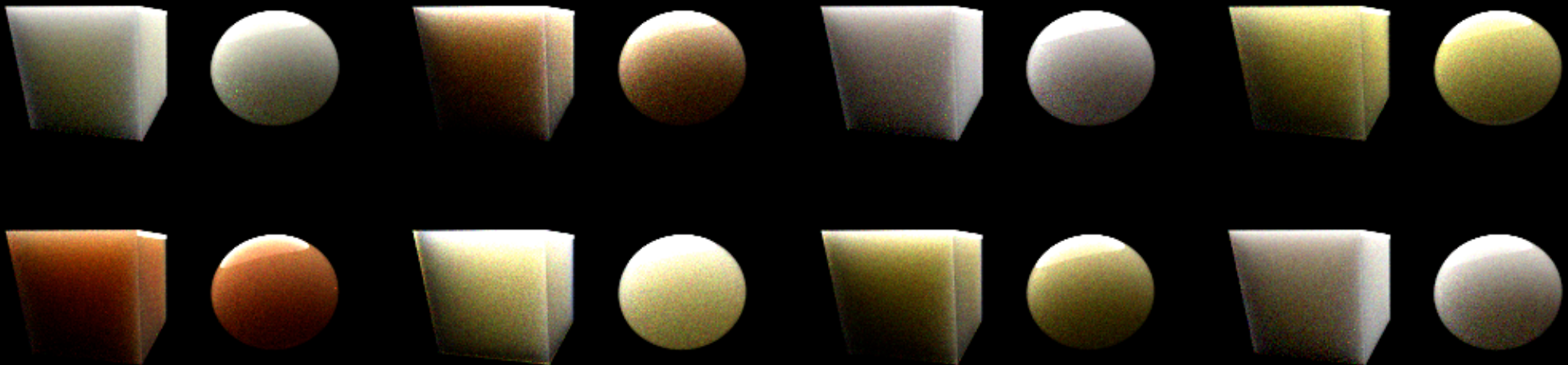
corrected distance distance correction factor

The diagram illustrates the distance correction formula. The equation is $r' = \sqrt{r^2 + z_0^2}$. The term r' is enclosed in a green box, and an arrow points from the label "corrected distance" below to it. The term r is enclosed in a red box, and an arrow points from the label "distance" below to it. The term z_0 is enclosed in a yellow box, and an arrow points from the label "correction factor" below to it. The labels "corrected distance", "distance", and "correction factor" are written in green, red, and yellow respectively, matching the colors of the boxes.

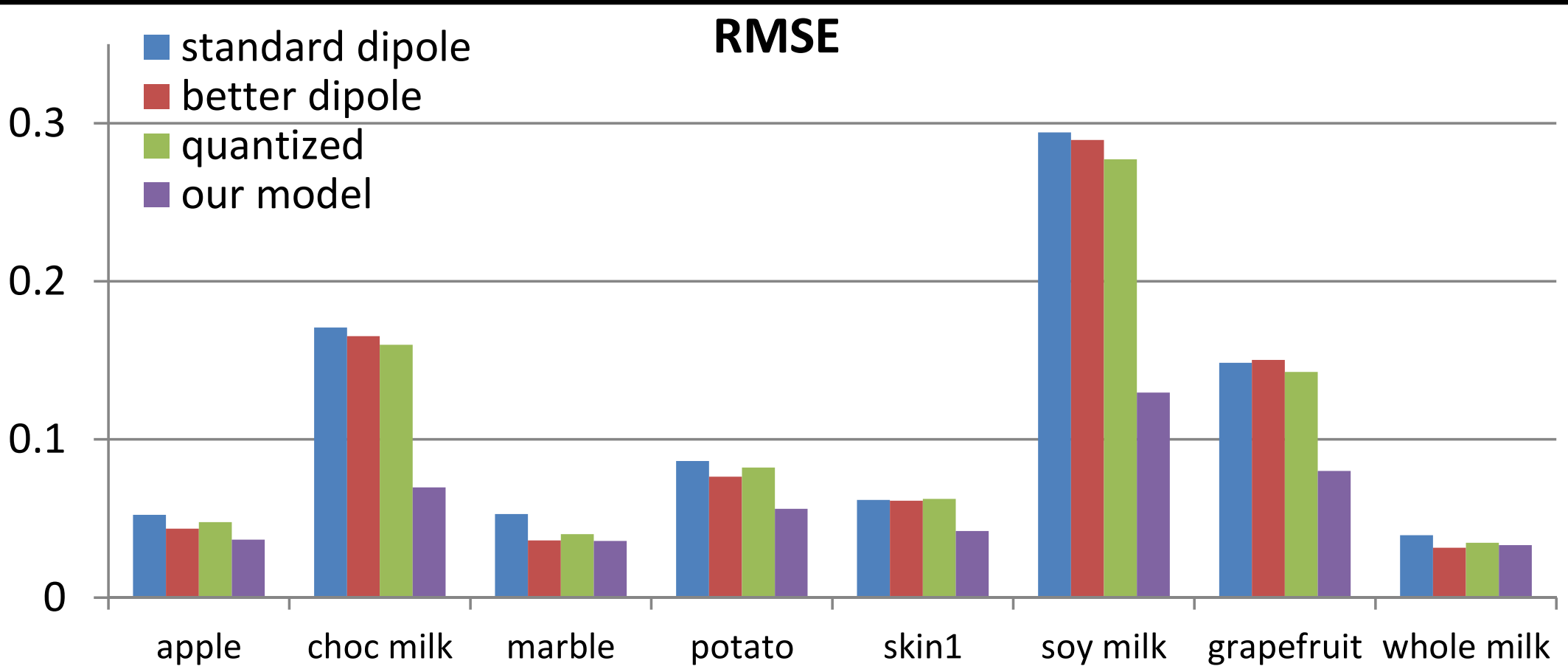
Results

Simple Test Cases

- Various measured materials
- Comparisons with Monte Carlo simulation
- Highly directional lighting

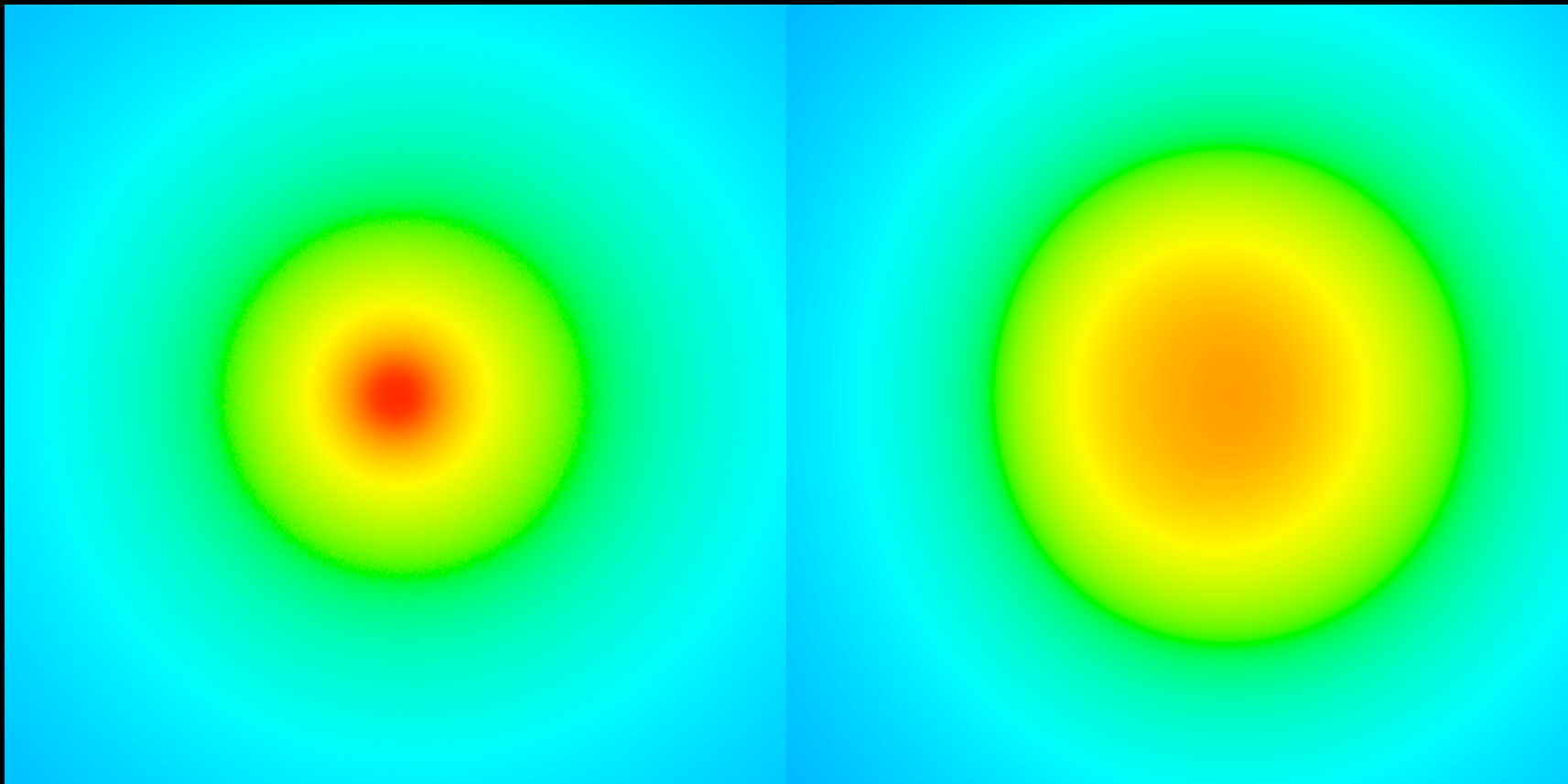


Simple Test Cases



Directional Effect

- Incident angle: 30°

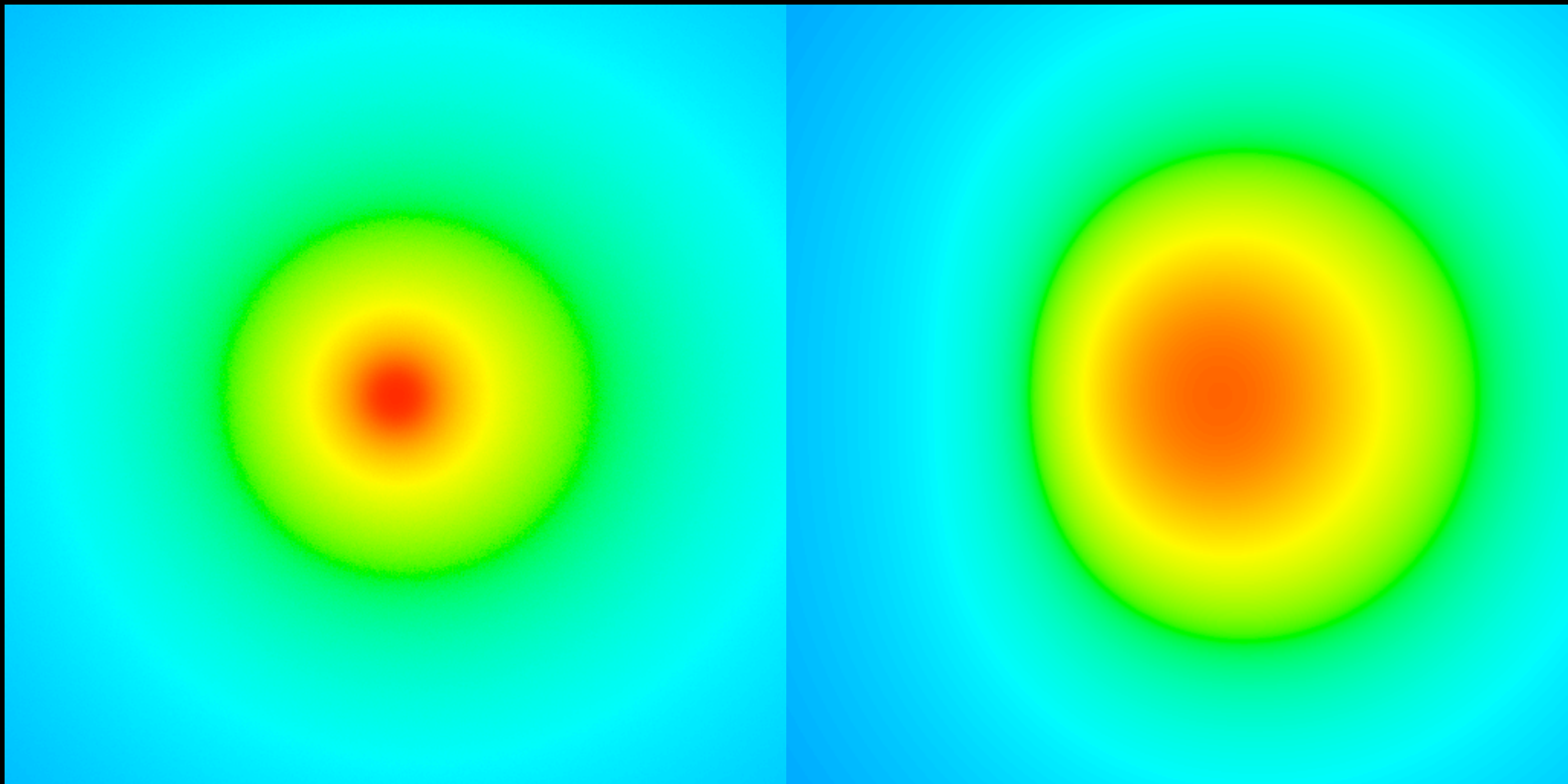


Quantized

Ours

Directional Effect

- Incident angle: 45°

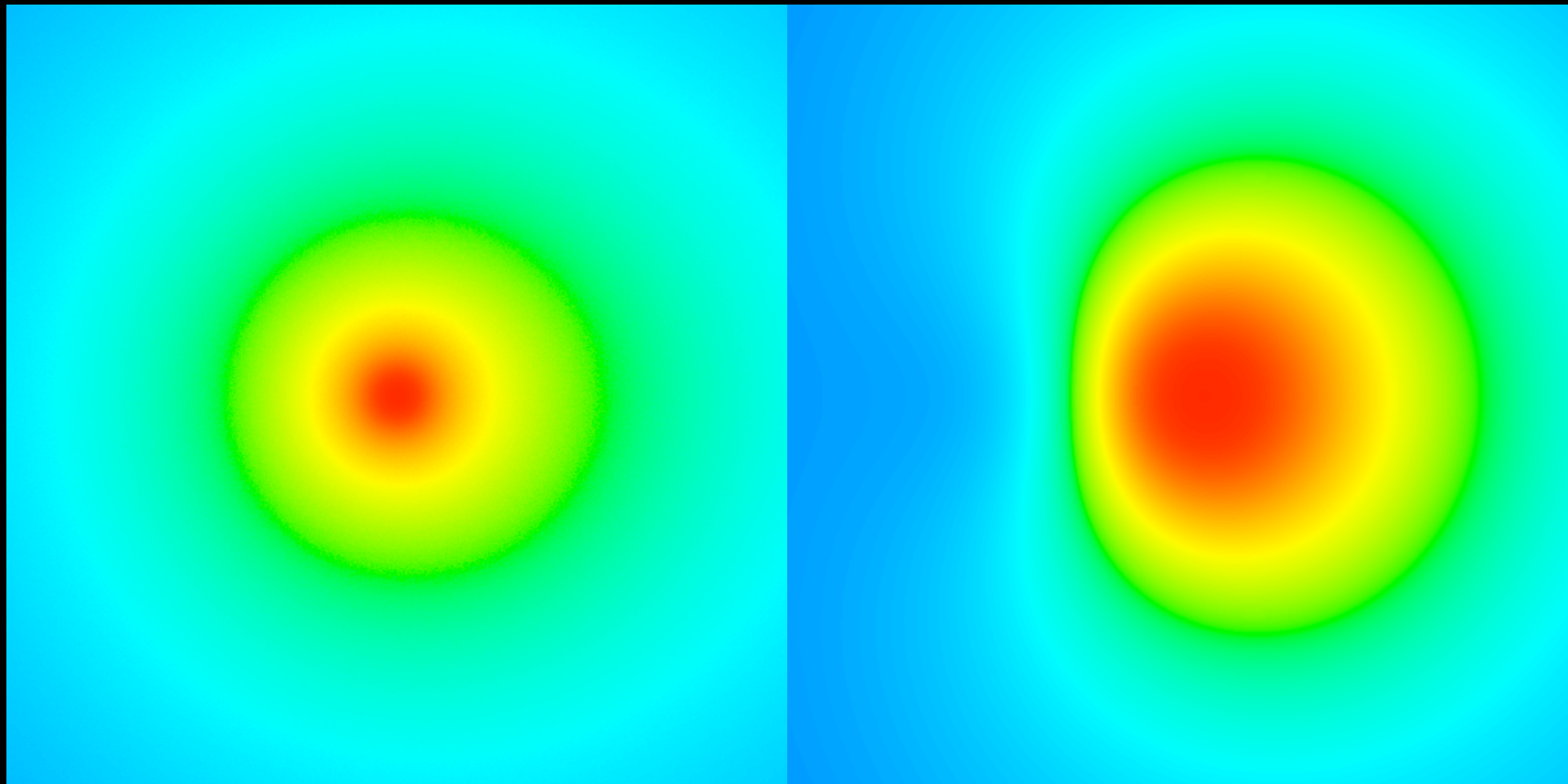


Quantized

Ours

Directional Effect

- Incident angle: 60°



Quantized

Ours

Grapefruits Bunny

Dipole



Quantized



Ours



Reference



Image Based Lighting



Quantized

Ours

Image Based Lighting



Quantized

Ours

Image Based Lighting



Quantized

Ours

Failure Case

- Low albedo materials (e.g., Cranberry juice)



Dipole

Ours

Conclusions

- First BSSRDF which...
 - Considers incoming light direction
 - Requires no precomputation
 - Provides fully analytical solution
- Far more accurate than previous models

Thank You

- **First** BSSRDF which...
 - Considers incoming light direction
 - Requires no precomputation
 - Provides fully analytical solution

http://cs.au.dk/~toshiya/dirpole_tr.pdf