

Targeted Pandemic Containment Through Identifying Local Contact Network Bottlenecks

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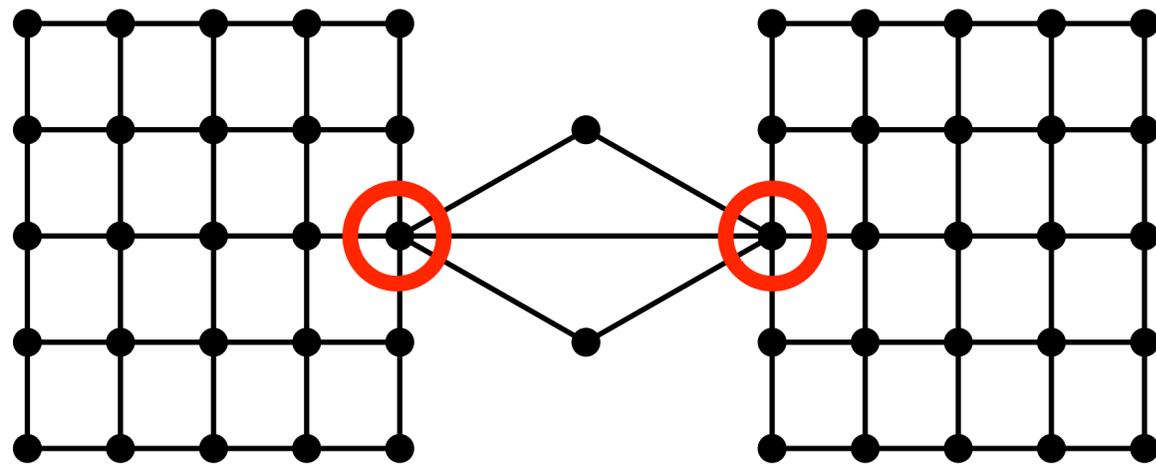


Network epidemic modelling and control strategies

- Networks are a powerful tool for modelling epidemic dynamics
- Previous models of infection control mostly focused on **node-level** interventions, **e.g., targeted vaccination**

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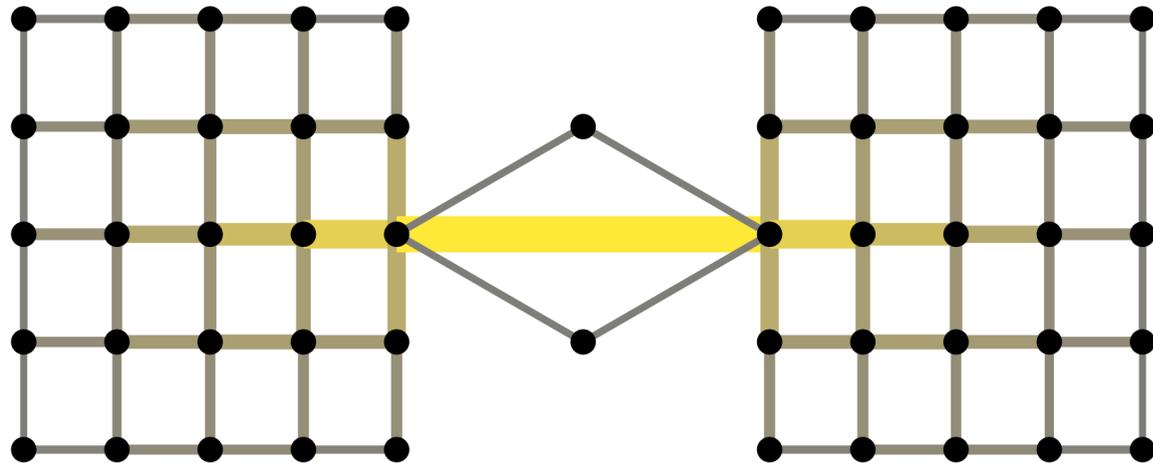
“... in networks with strong community structure, immunization interventions targeted at individuals bridging communities are more effective ...” (Salathe and Jones, 2010)

Network epidemic modelling and control strategies

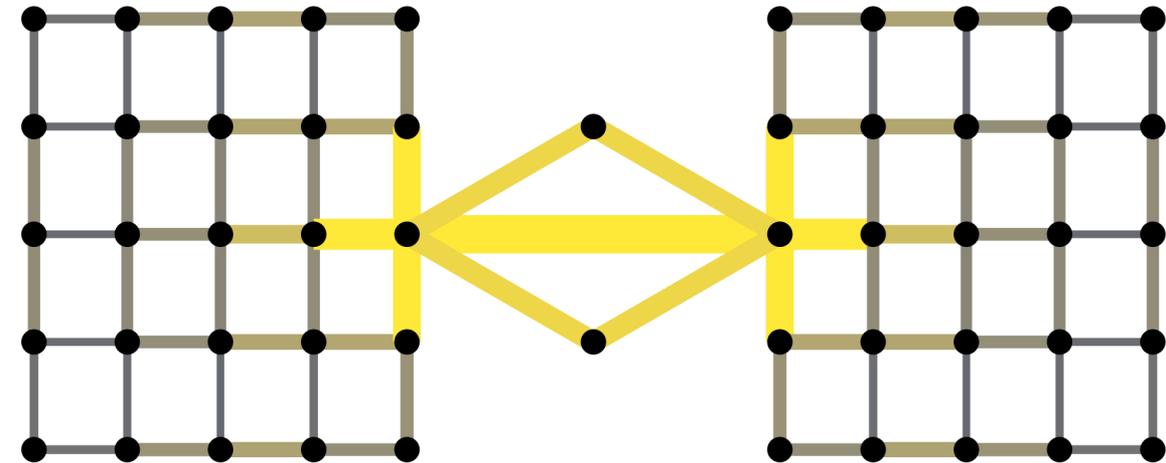
- In this work we look at **edge-level** interventions, e.g., contact reduction, physical distancing, quarantine
 - For county-level networks, selectively closing roads or quarantining towns and cities
 - For individual-level networks, enforce or encourage physical distancing by providing incentives

Network epidemic modelling and control strategies

- In this work we look at edge-level interventions, e.g., contact reduction, physical distancing, quarantine
- How to **identify important edges** for intervention strategies?



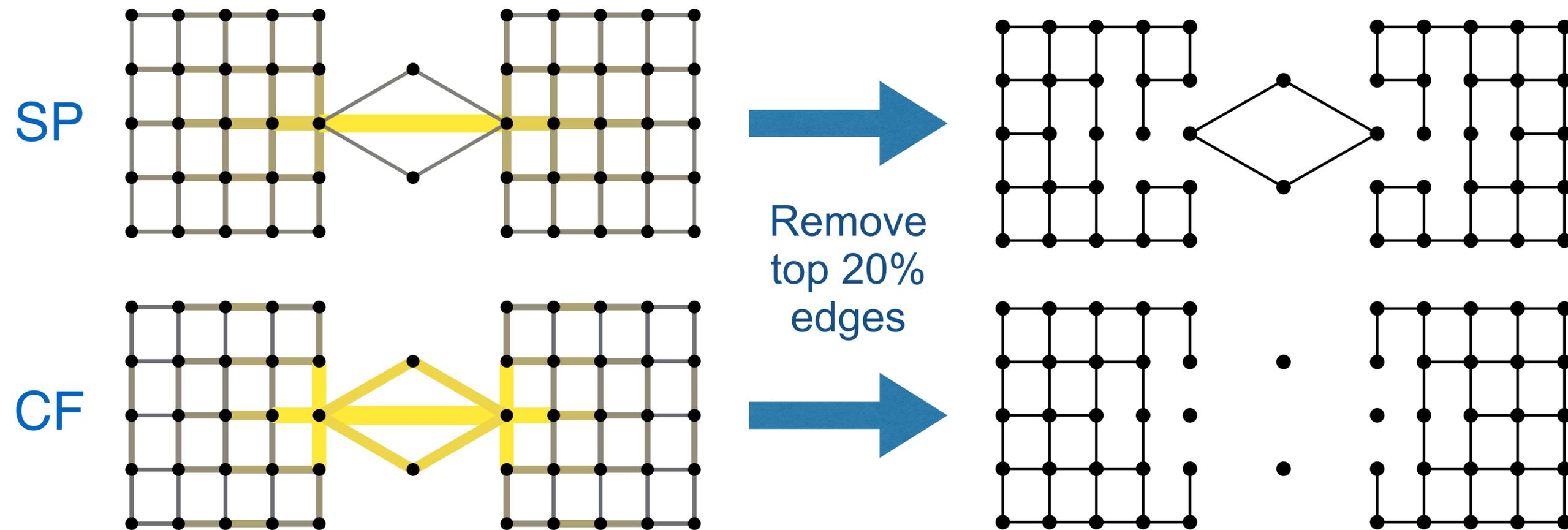
Shortest-path (SP) edge-betweenness



Current-flow (CF) edge-betweenness

Network epidemic modelling and control strategies

- SP and CF may not work well
- Global “bottlenecks” do not block **local** transmission
- Less effective in the presence of community outbreak



Quantifying edge importance locally

- We need a **new edge-betweenness** measure that detects **local** bottlenecks

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- Electrical current flow

$$\begin{array}{ccc} \min \|f\|_2^2 & \text{s.t. } B^T f + \mathbf{1}_s = \mathbf{1}_t & (P') \\ \downarrow & \downarrow & \downarrow \\ f \in \mathbb{R}^{|E|} & \text{incidence matrix} & \text{indicator vector of } s \in V \end{array} \quad \begin{array}{ccc} \min x^T Lx - x^T(\mathbf{1}_s - \mathbf{1}_t) & (D') \\ \downarrow & \downarrow \\ x \in \mathbb{R}^{|V|} & \text{Laplacian matrix} \end{array}$$

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Global focus: All possible pairs $(s, t) \in V \times V$ are taken into account

Quantifying edge importance locally

- We need a new edge-betweenness measure that detects **local** bottlenecks
- **p -norm flow diffusion (for brevity, $p = 2$ in this presentation)**

$$\min \|f\|_2^2 \quad \text{s.t.} \quad B^T f + \mathbf{1}_s \leq T \quad (P)$$

$$\min_{x \geq 0} x^T L x - x^T (\mathbf{1}_s - T) \quad (D)$$

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$f \in \mathbb{R}^{|E|}$ incidence matrix indicator vector of $s \in V$

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$x \in \mathbb{R}^{|V|}$ Laplacian matrix

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$T \in \mathbb{R}_+^{|V|}$ specifies node capacities

$$\min \|f\|_2^2 \quad \text{s.t.} \quad B^T f + \mathbf{1}_s = \mathbf{1}_t \quad (P') \qquad \min x^T L x - x^T (\mathbf{1}_s - \mathbf{1}_t) \quad (D')$$

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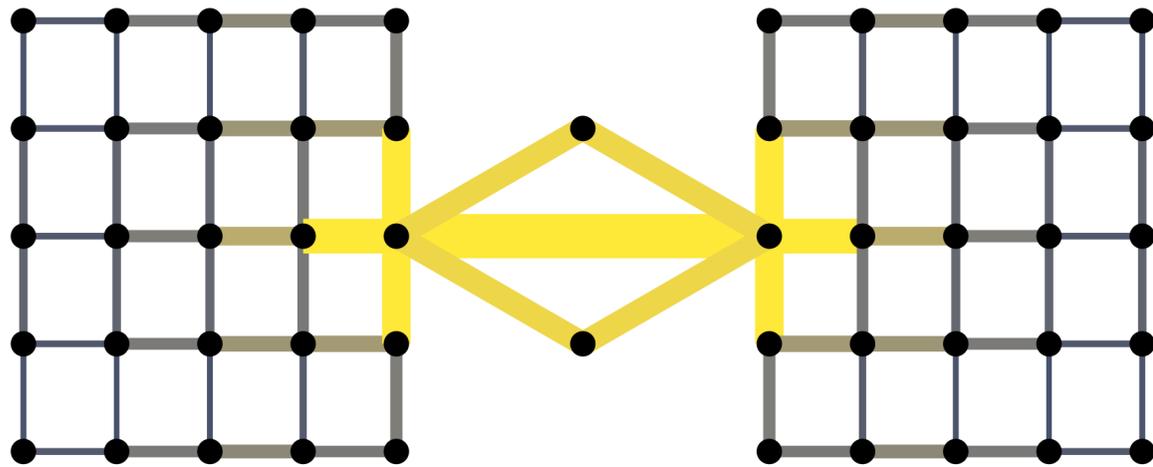
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- We set $T(v) = \text{deg}(v)/(2\lambda |E|)$, where $\lambda \in (0, 1]$ controls locality
- Denote f_s^λ the optimal flow arising from source node s with locality λ
- **Local-flow (LF) betweenness** of an edge $e \in E$ is

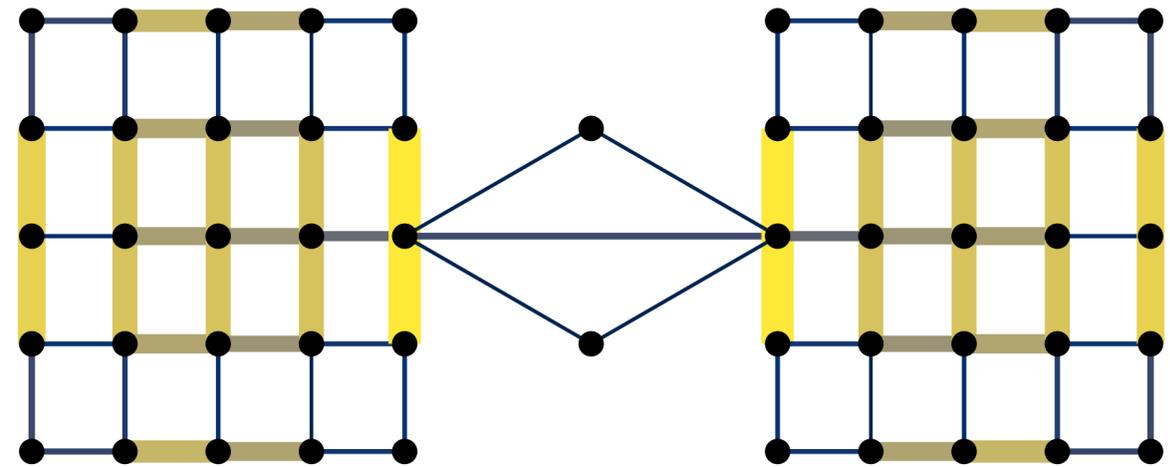
$$lb(e; \lambda) := \frac{1}{|V|} \sum_{s \in V} |f_s^\lambda(e)|$$

Quantifying edge importance locally

- Local-flow (LF) betweenness
 - Colors and edge widths are chosen to reflect relative magnitude

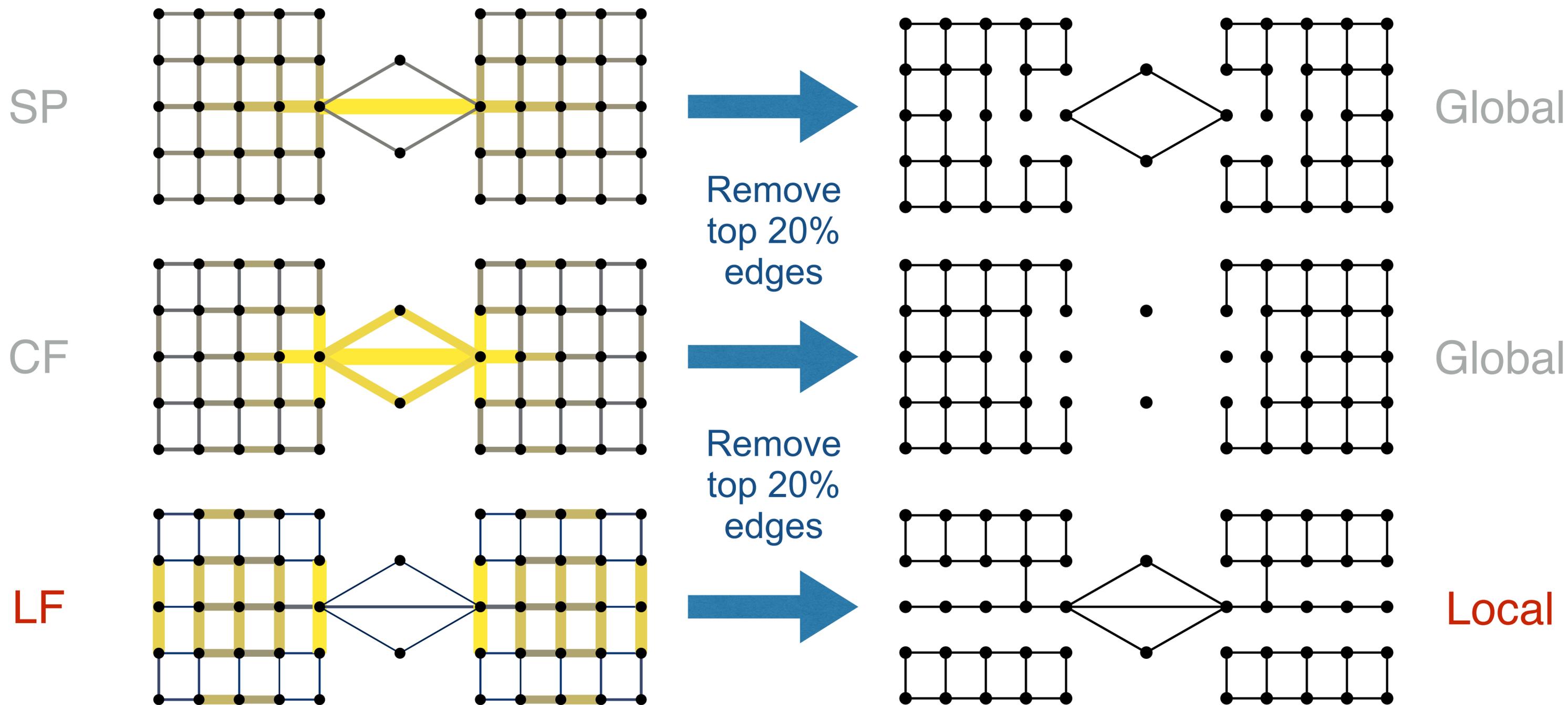


$$\lambda = 1$$



$$\lambda = 0.4$$

Quantifying edge importance locally

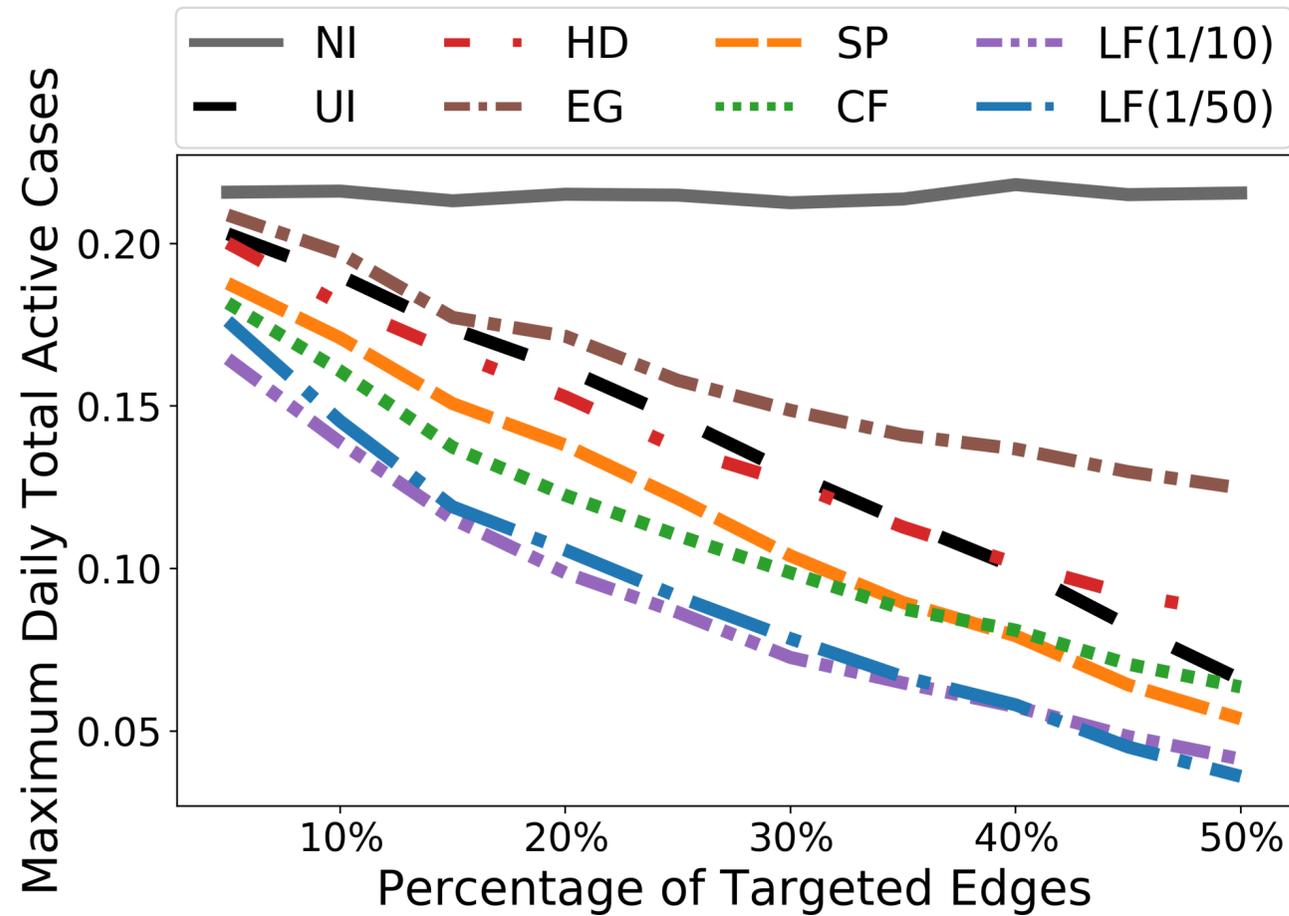


Facebook-county network

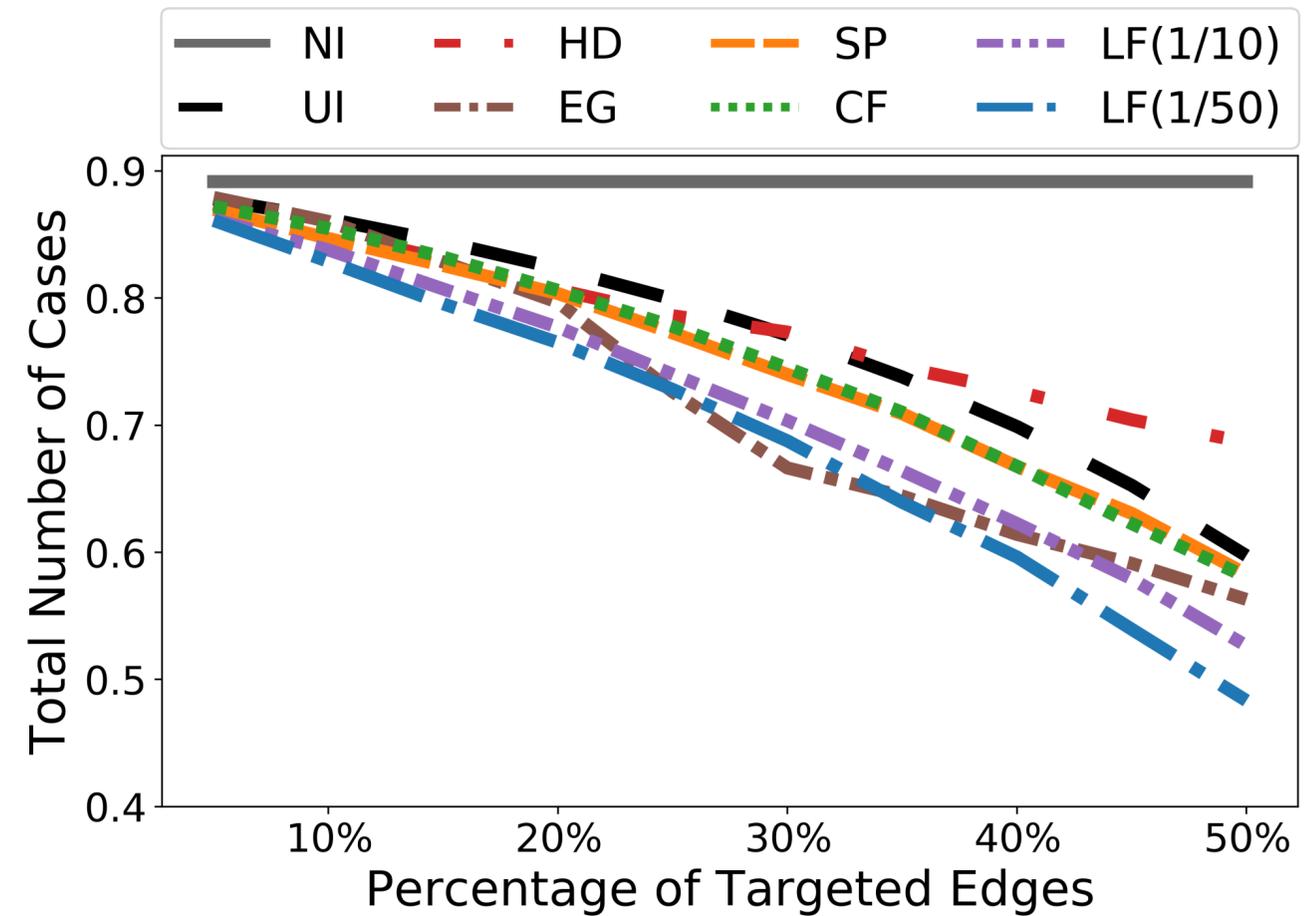
- 3100 counties
- Two counties are connected with an edge if there exists strong social interaction
- Social interaction tends to happen mostly among nearby counties



Facebook-county network - simulated epidemic dynamics



Epidemic peak



Outbreak size

NI: No Intervention

UI: Uniform Intervention

EG: Eigenvector centrality

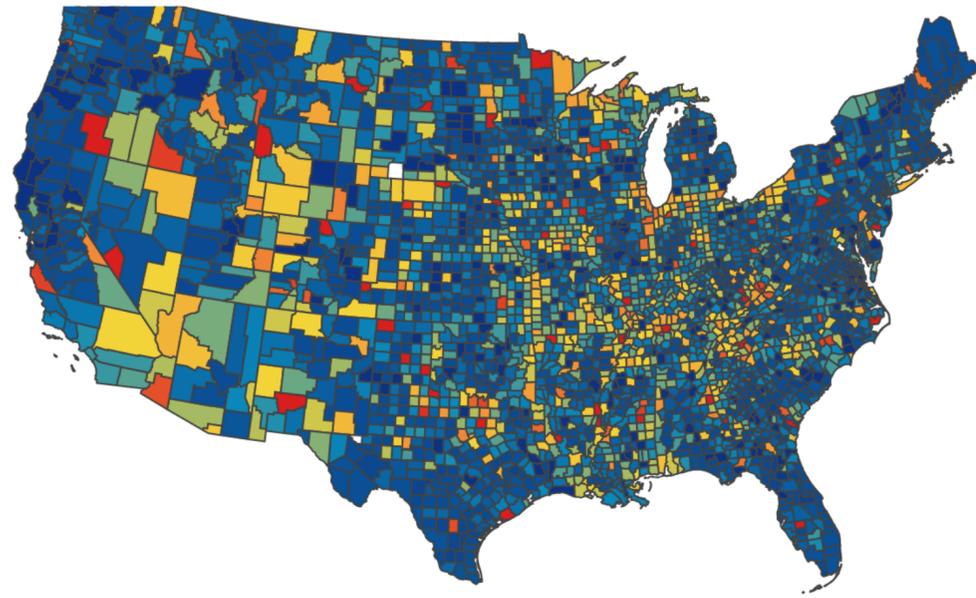
HD: Degree centrality

SP: Shortest-Path betweenness

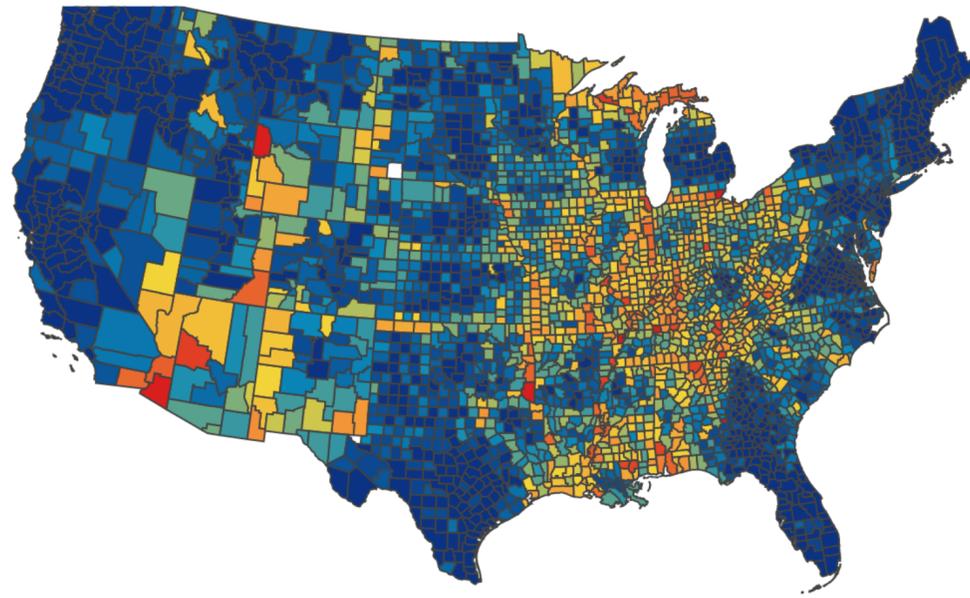
CF: Current-Flow betweenness

LF: Local-Flow betweenness

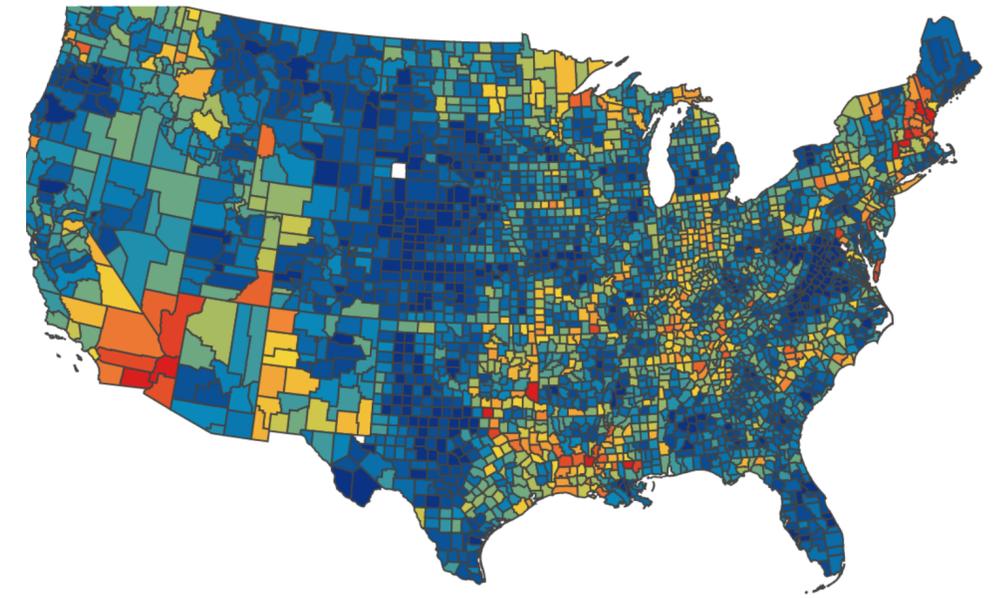
Why is LF most effective?



SP



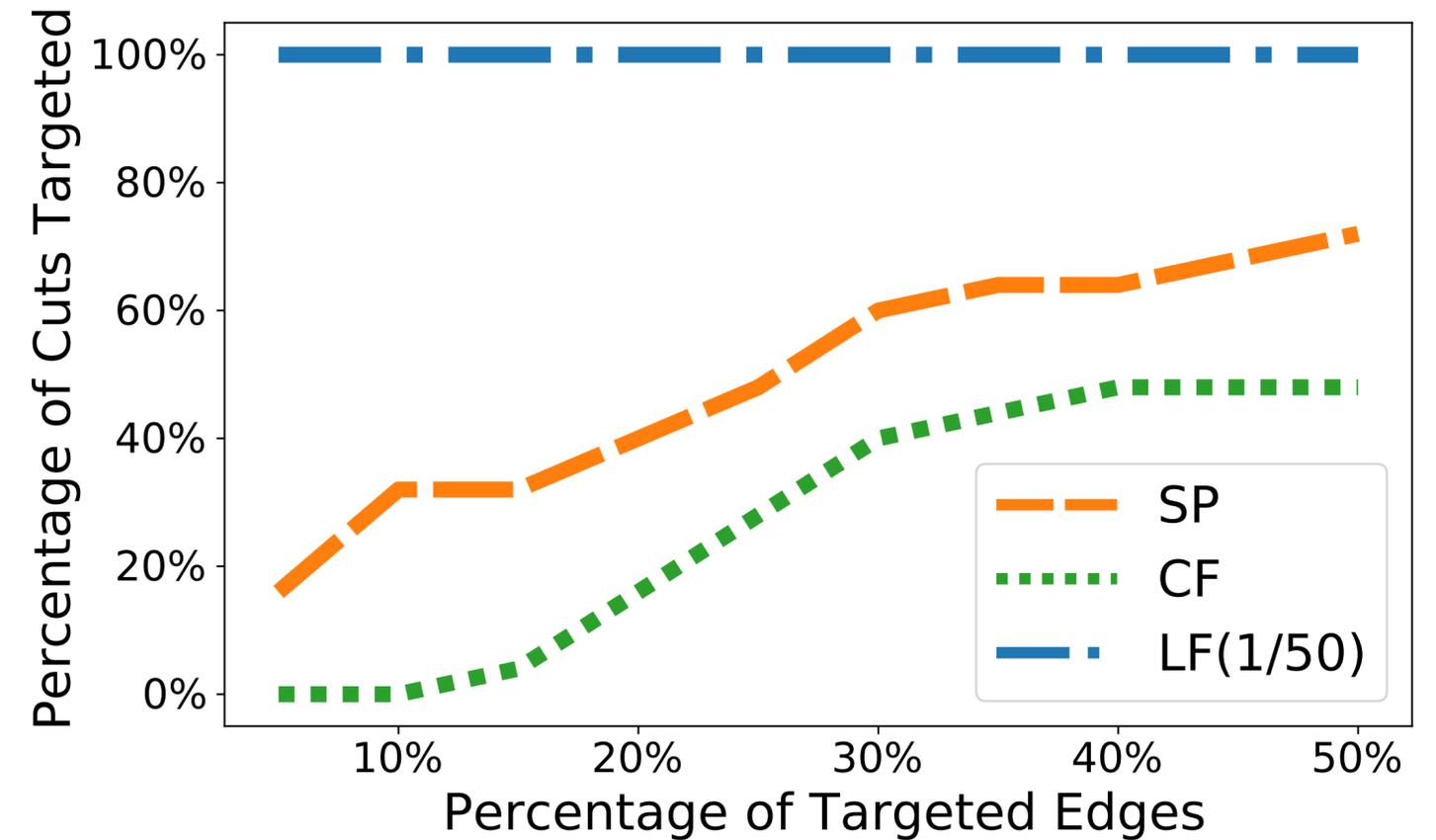
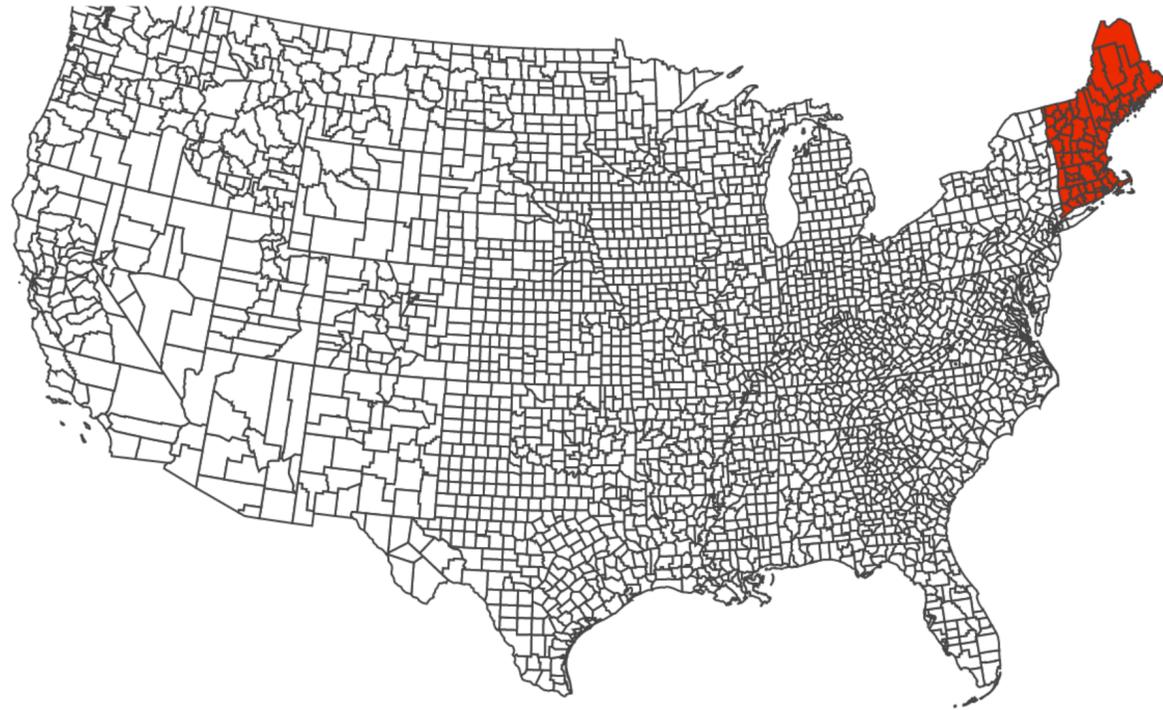
CF



LF

- **Distribution of top 25% edges** reflected by county-level colors:
 - **red** means most incident edges are reduced (in edge weights)
 - **dark blue** means few incident edges are reduced (in edge weights)

Why is LF most effective?



- Counties in red form a tightly-knit local cluster with few out-links
- 100% out-links are among top 5% edges identified by LF
- <20% out-links are identified by SP or CF

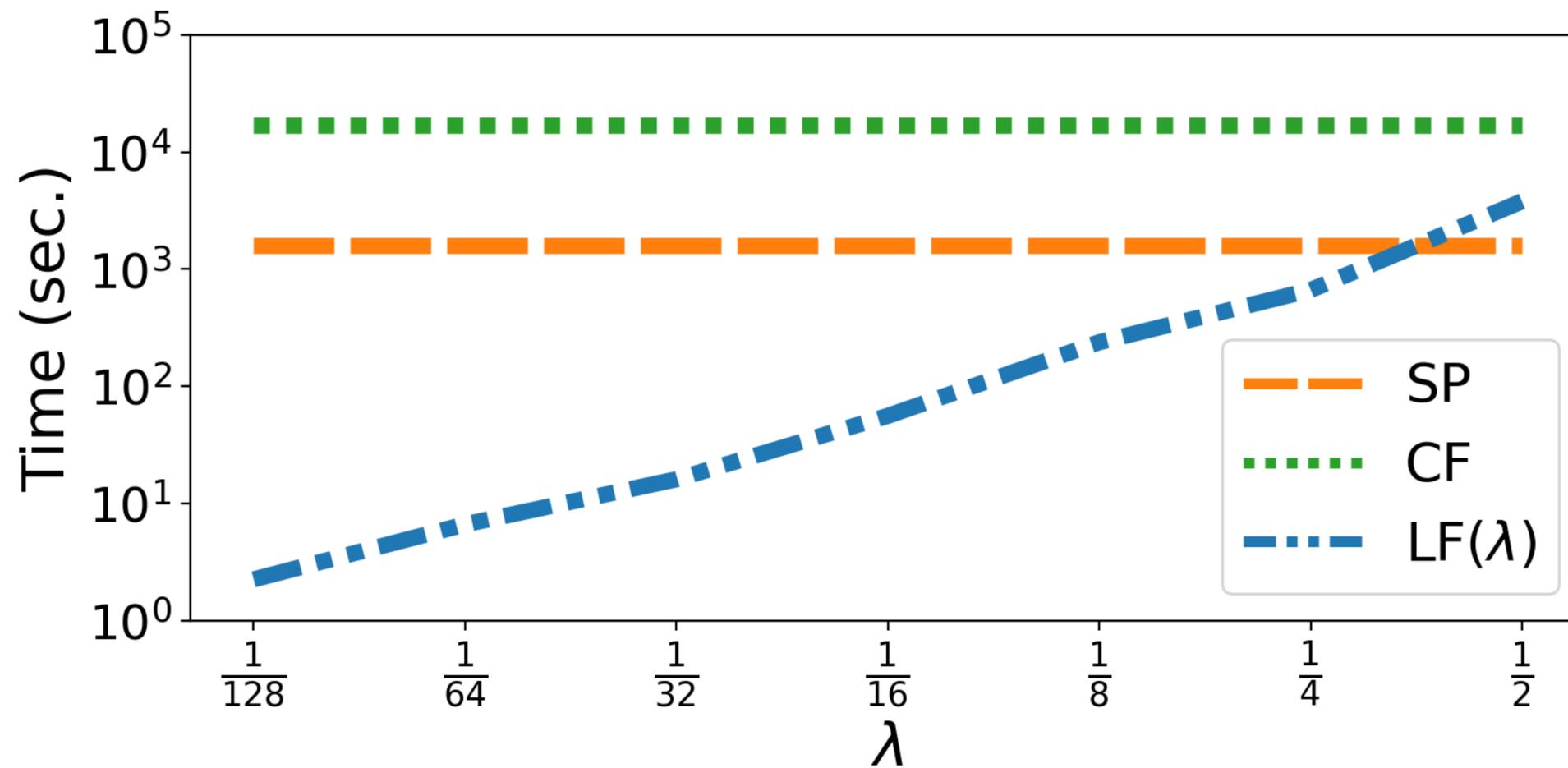
Are the results robust?

- Estimated reproduction number for Covid-19 is $R_0 = 2.5$
- We tried varying reproduction numbers $R_0 \in \{1.5, 2.5, 3.5, 4.5\}$
- 3 very different initializations from where epidemic starts
 - randomly chosen 1% counties spread across the network
 - a tightly-knit cluster of counties
 - single cities: Chicago, New York, Los Angeles
- Delayed interventions applied in the middle of the epidemic (not from the start)
- **All these different settings produce consistent results**

Thank you!

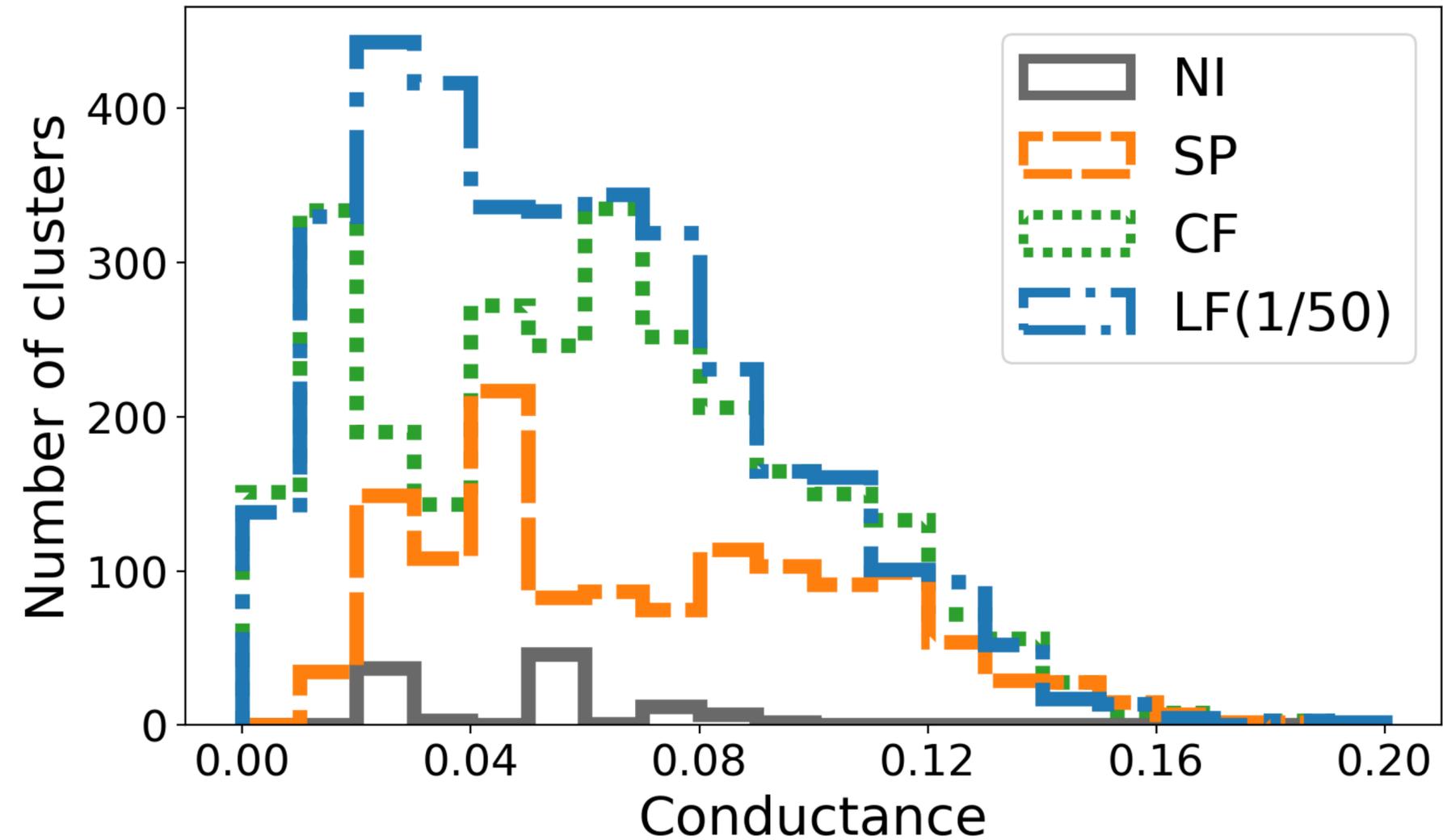
Computation time

- Computing LF for all edges requires $O(\lambda |V| |E|)$, $\lambda \in (0,1]$



$|V| = 10,000, |E| = 199,128$

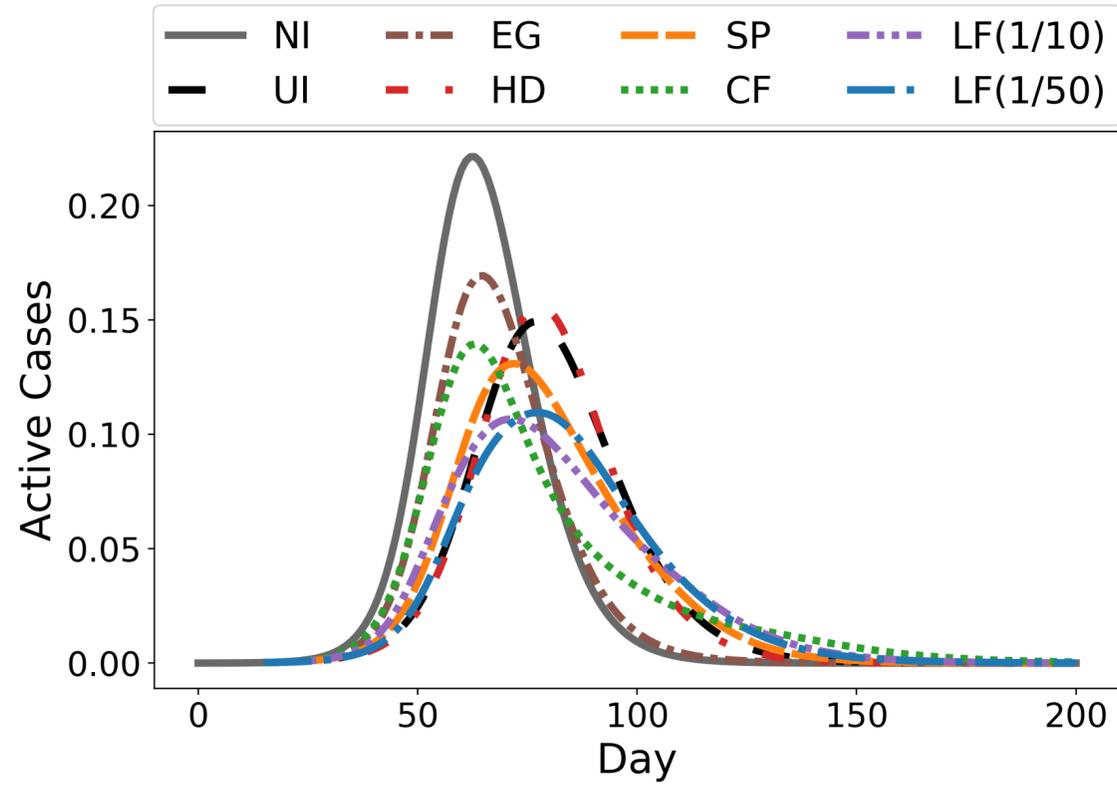
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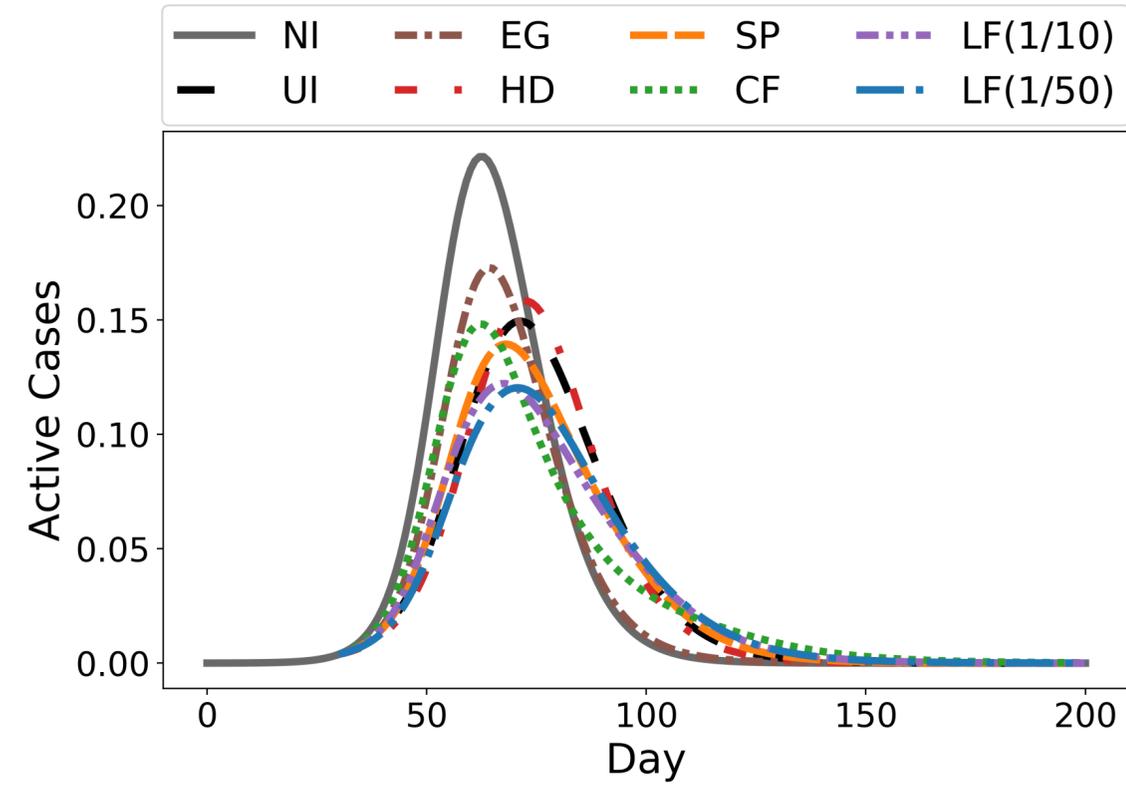
- **Distribution of small-size clusters** (consisting of ≤ 100 counties) by conductance

Facebook-county network - simulated epidemic dynamics

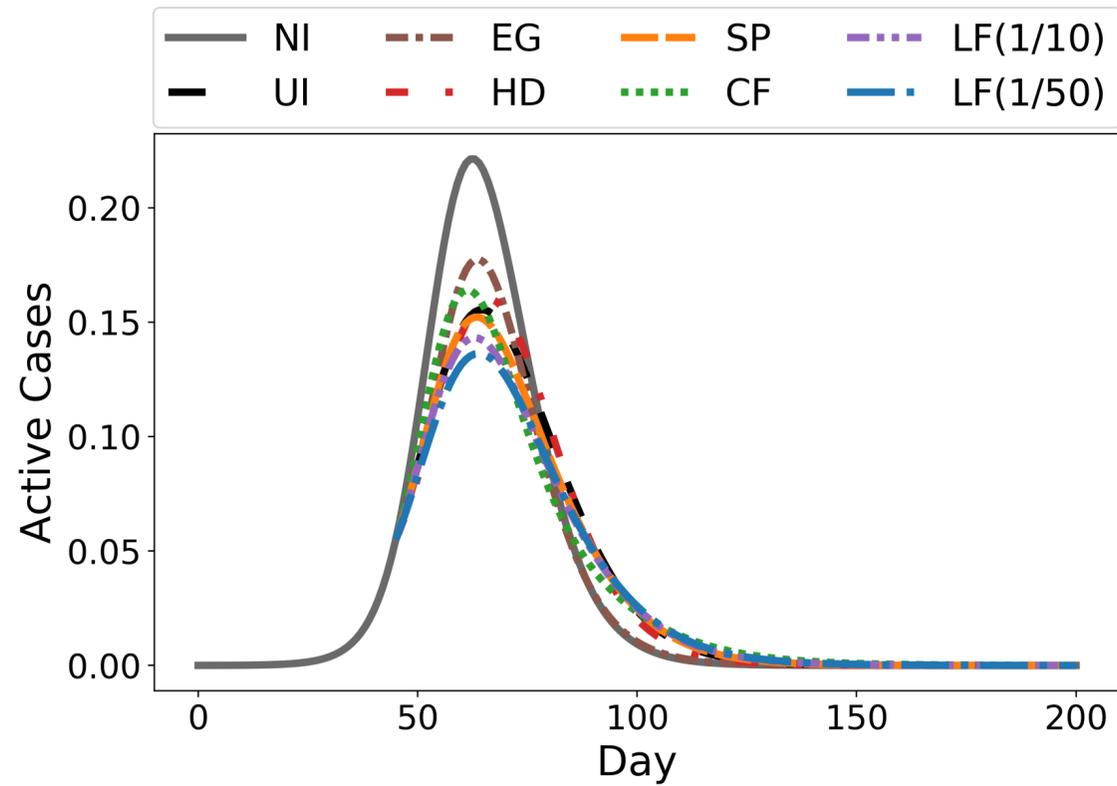
15-day
delay



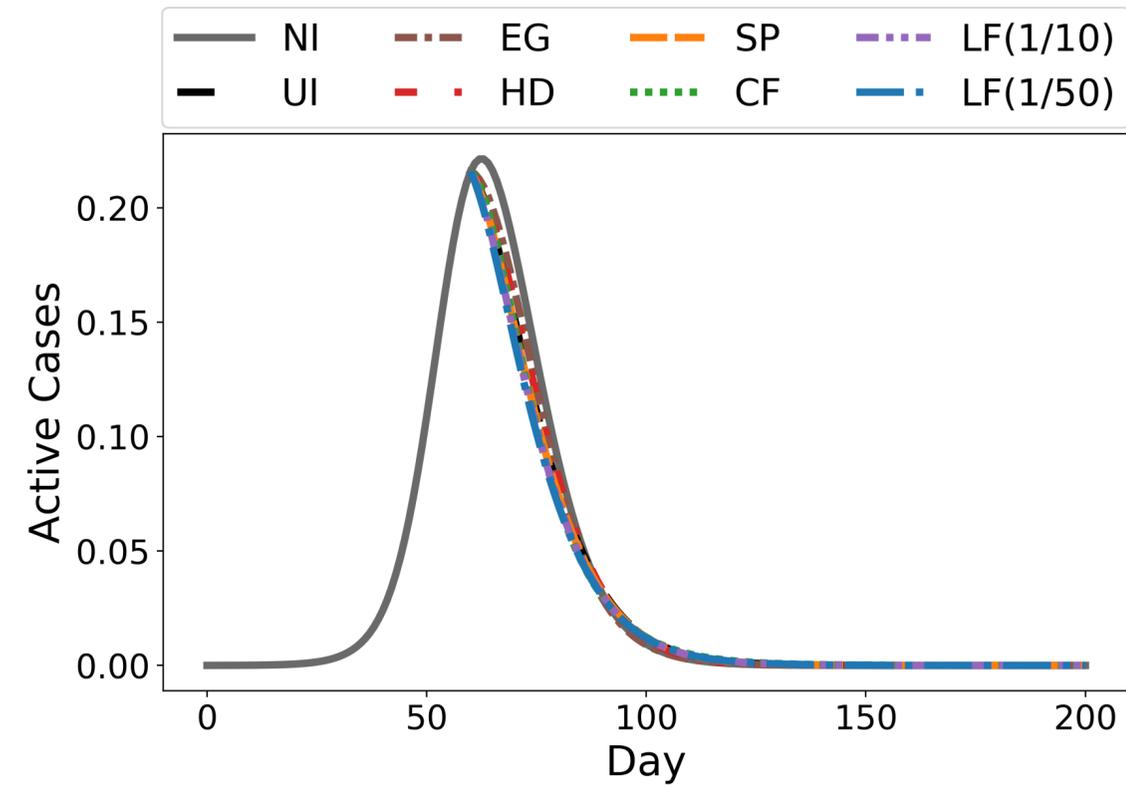
30-day
delay



45-day
delay

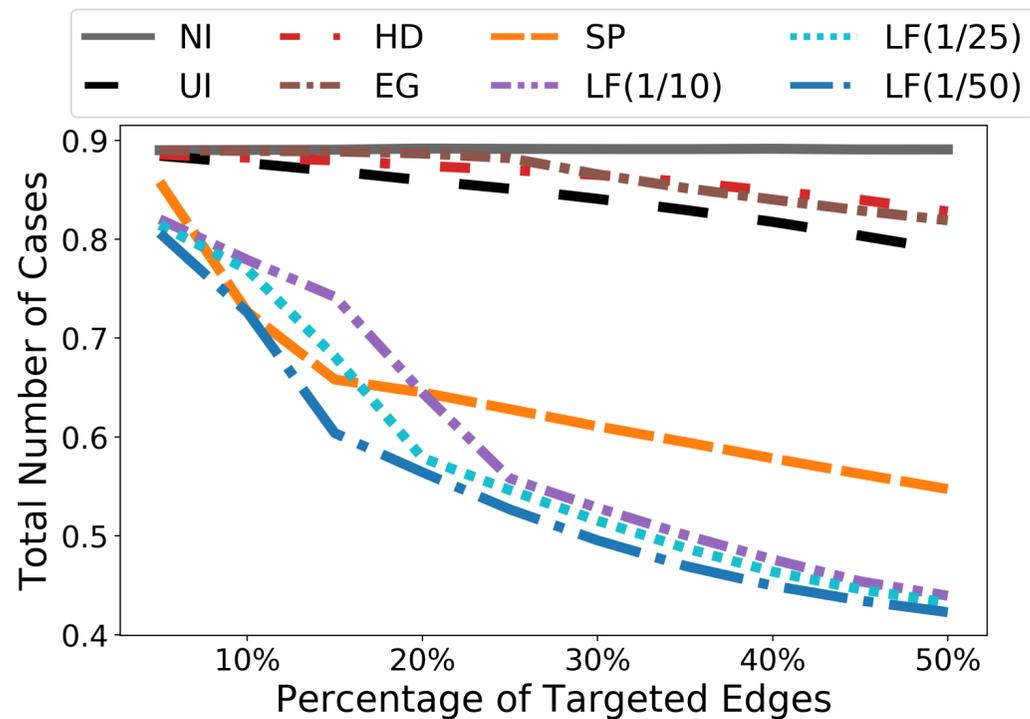


60-day
delay

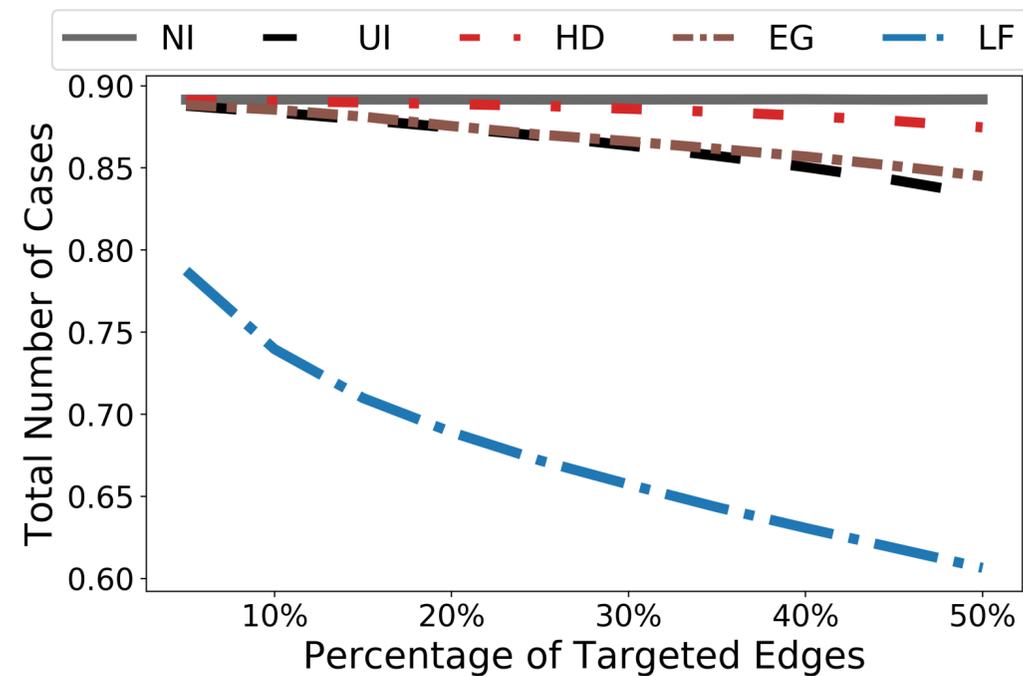


More datasets

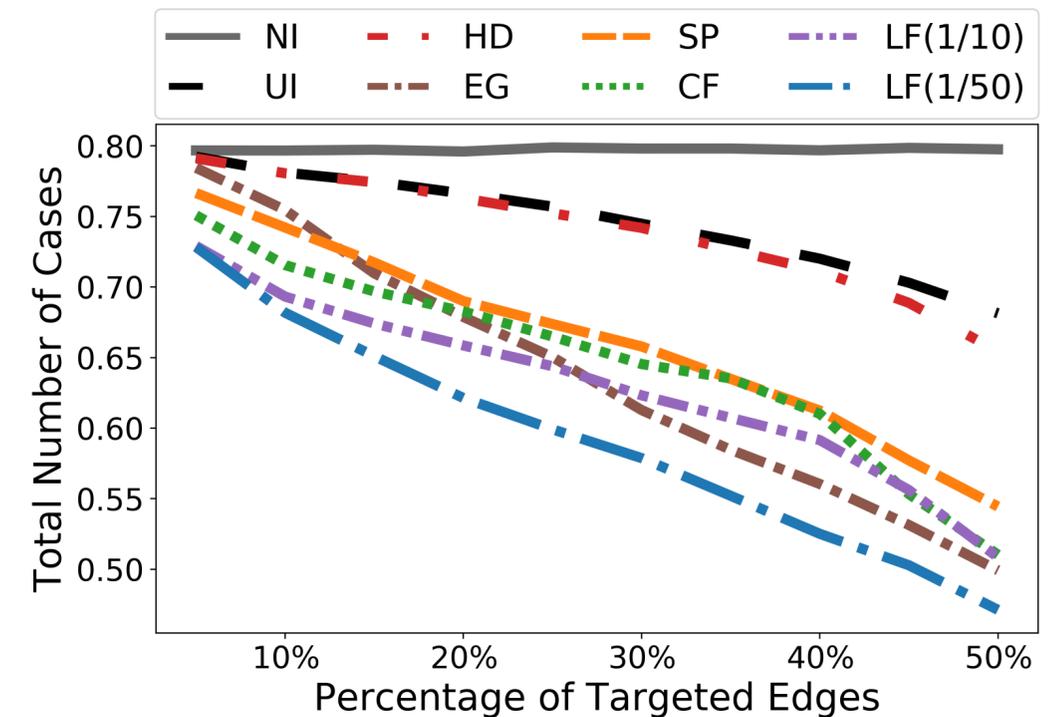
- *Wi-Fi hotspots Montreal* network, $|V| = 103\text{K}$, $|E| = 631\text{K}$
- *Portland, Oregon* network, $|V| = 1.6\text{M}$, $|E| = 31\text{M}$
- *Sub-sampled Portland, Oregon* network, $|V| = 10\text{K}$, $|E| = 199\text{K}$
- Agent-based SEIR network model



Wi-Fi Montreal



Portland



Portland Sub-sampled