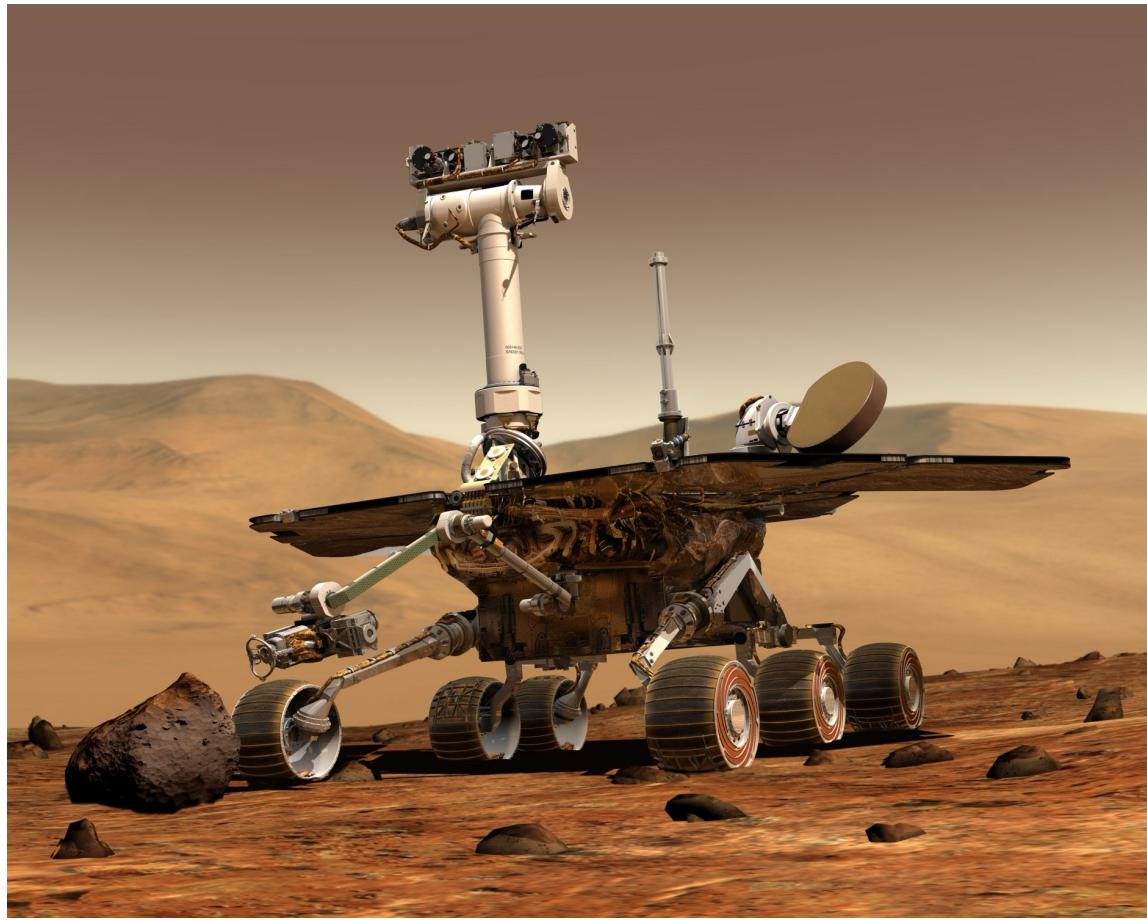
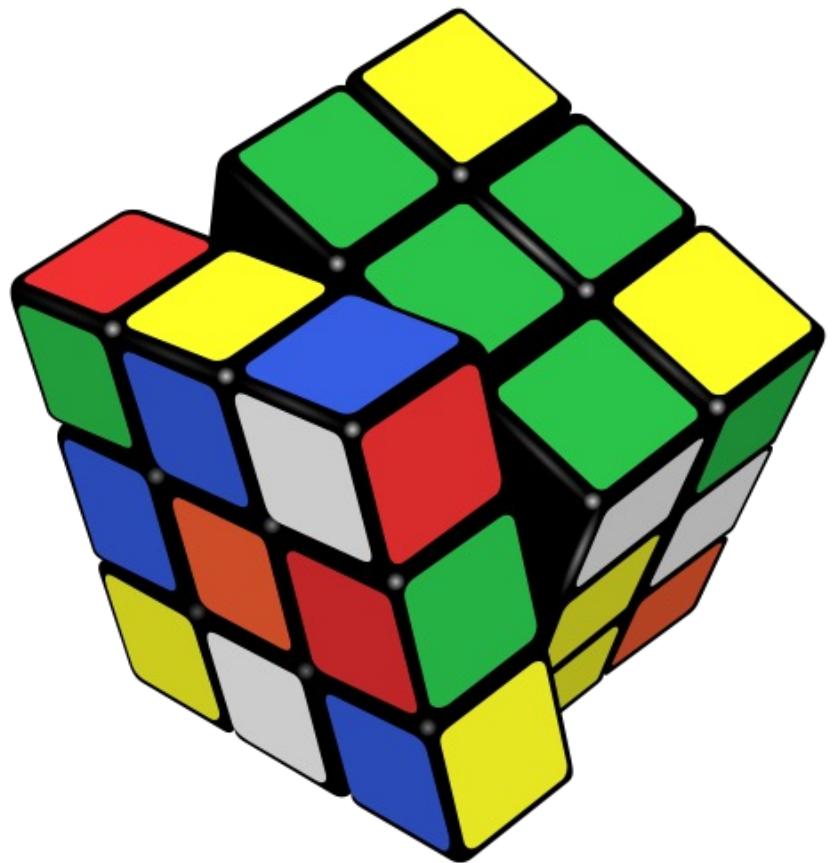


# **Lecture 2: Uninformed Search Techniques**

## **CS486/686 Intro to Artificial Intelligence**

2026-1-8

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# Outline

- Problem solving agents and search
- Properties of search algorithms
- Uninformed search
  - Breadth first
  - Depth first
  - Iterative Deepening

# Introduction

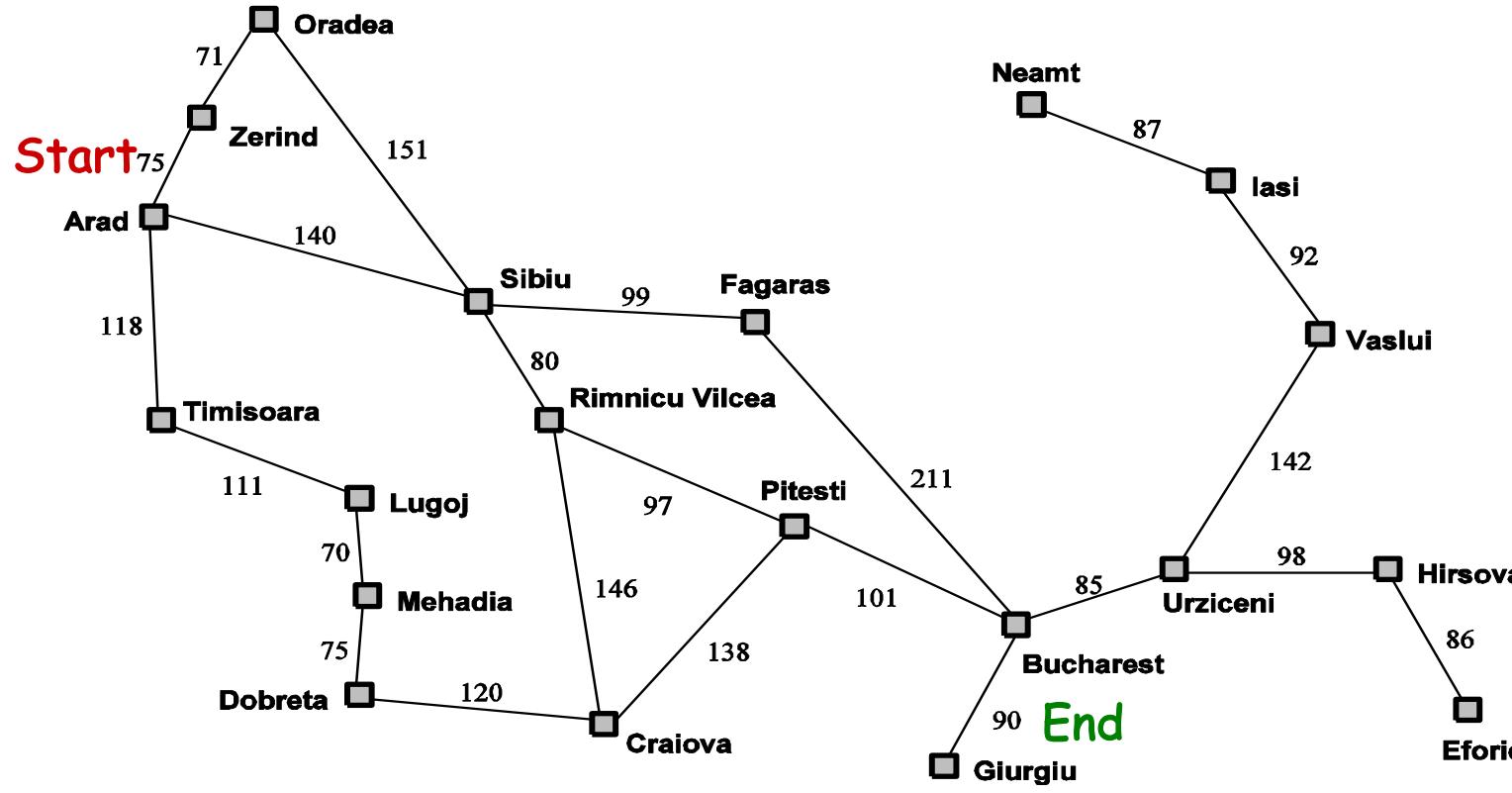
- Search was one of the first topics studied in AI
  - Newell and Simon (1961) *General Problem Solver*
- Central component to many AI systems
  - Automated reasoning, theorem proving, path planning in robotics and autonomous driving, VLSI layout, scheduling, game playing,...

# Problem-solving agents

```
function SIMPLE-PROBLEM-SOLVING-AGENT(percept) returns an action
  static: seq, an action sequence, initially empty
         state, some description of the current world state
         goal, a goal, initially null
         problem, a problem formulation

  state  $\leftarrow$  UPDATE-STATE(state, percept)
  if seq is empty then do
    goal  $\leftarrow$  FORMULATE-GOAL(state)
    problem  $\leftarrow$  FORMULATE-PROBLEM(state, goal)
    seq  $\leftarrow$  SEARCH(problem)
    action  $\leftarrow$  FIRST(seq)
    seq  $\leftarrow$  REST(seq)
  return action
```

# Example: Traveling in Romania



## Formulate Goal

Get to Bucharest

## Formulate Problem

Initial state: In(Arad)

Actions: Drive between cities

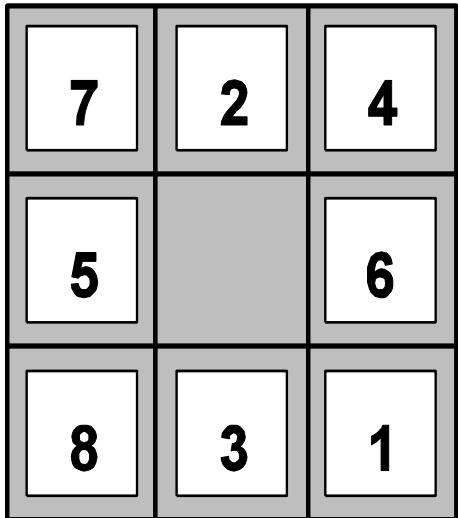
Goal Test: In(Bucharest)?

Path cost: Distance between cities

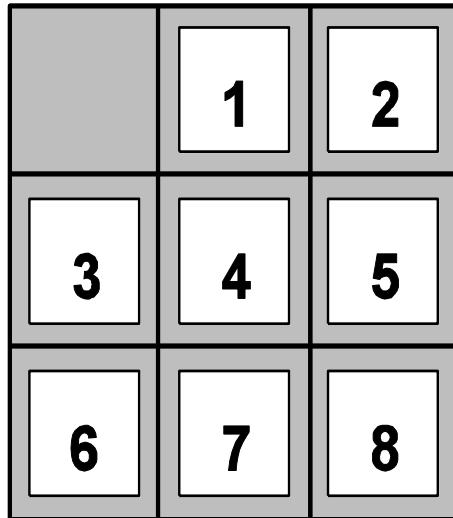
## Find a solution

Sequence of cities: Arad, Sibiu, Fagaras, Bucharest

# Example: 8-Tile Puzzle



Start State



Goal State

**States:** Locations of 8 tiles and blank

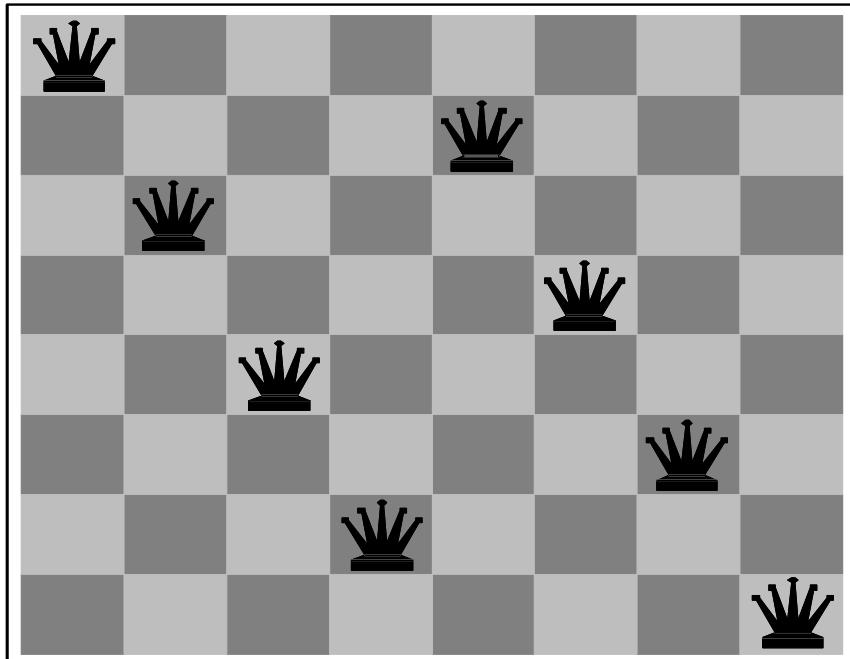
**Initial State:** Any state

**Succ Func:** Generates legal states that result from trying 4 actions (blank up, down, left, right)

**Goal test:** Does state match desired configuration

**Path cost:** Number of steps

# Example: 8-queen problem



**States:** Arrangement of 0 to 8 queens on the board

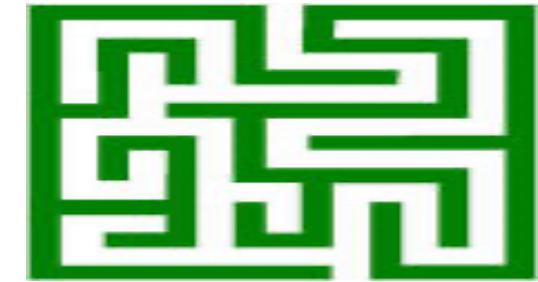
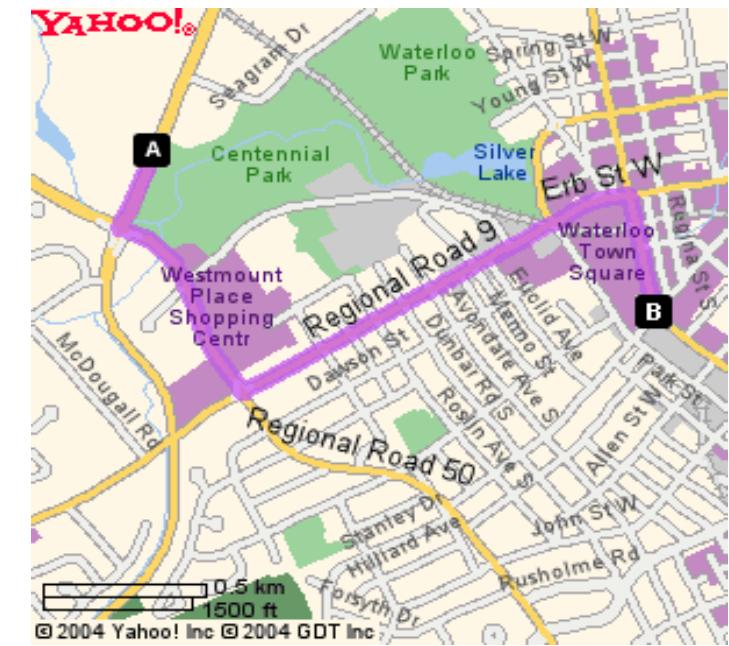
**Initial State:** No queens on the board

**Succ Func:** Add a queen to an empty space

**Goal test:** 8 queens on board, none attacked

**Path cost:** none

# More Examples



# Common Characteristics

- All of those examples are
  - Fully observable
  - Deterministic
  - Sequential
  - Static
  - Discrete
  - Single agent
- Can be tackled by **simple** search techniques

# Cannot tackle these problems yet...

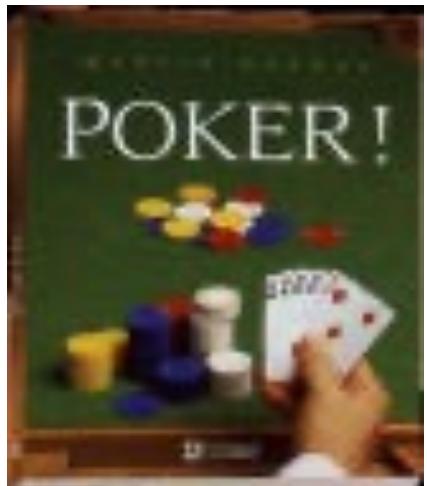
Chance



Infinite number of states



Games against  
an adversary



Hidden states

All of the  
above

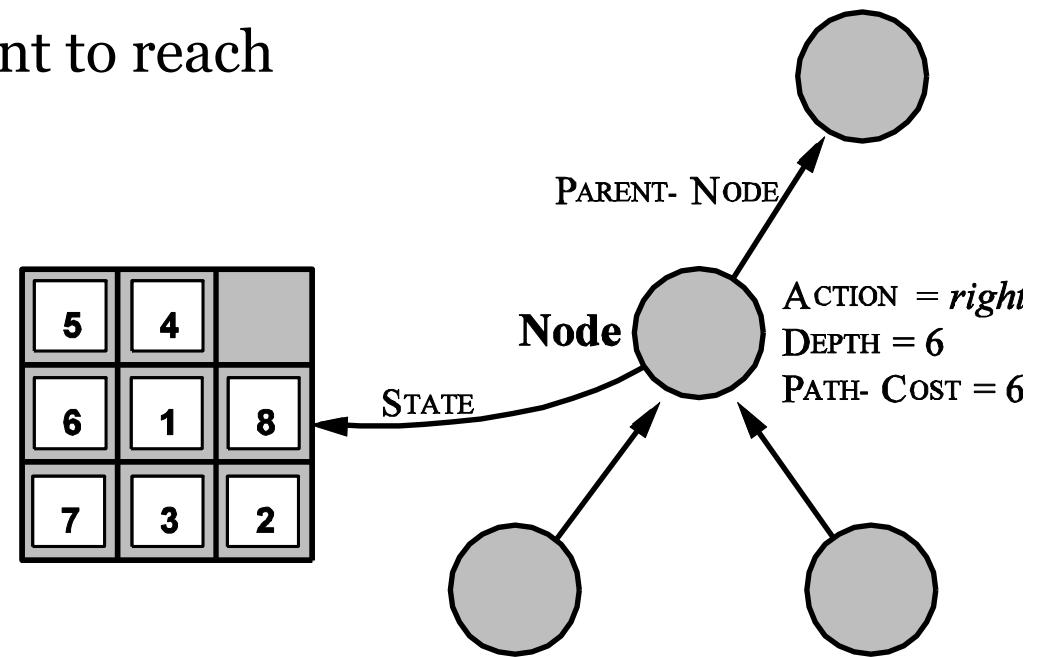


# Searching

- We can formulate a search problem
  - Now need to find the solution
- We can visualize a state space search in terms of trees or graphs
  - Nodes correspond to states
  - Edges correspond to taking actions
- We will be studying **search trees**
  - These trees are constructed “on the fly” by our algorithms

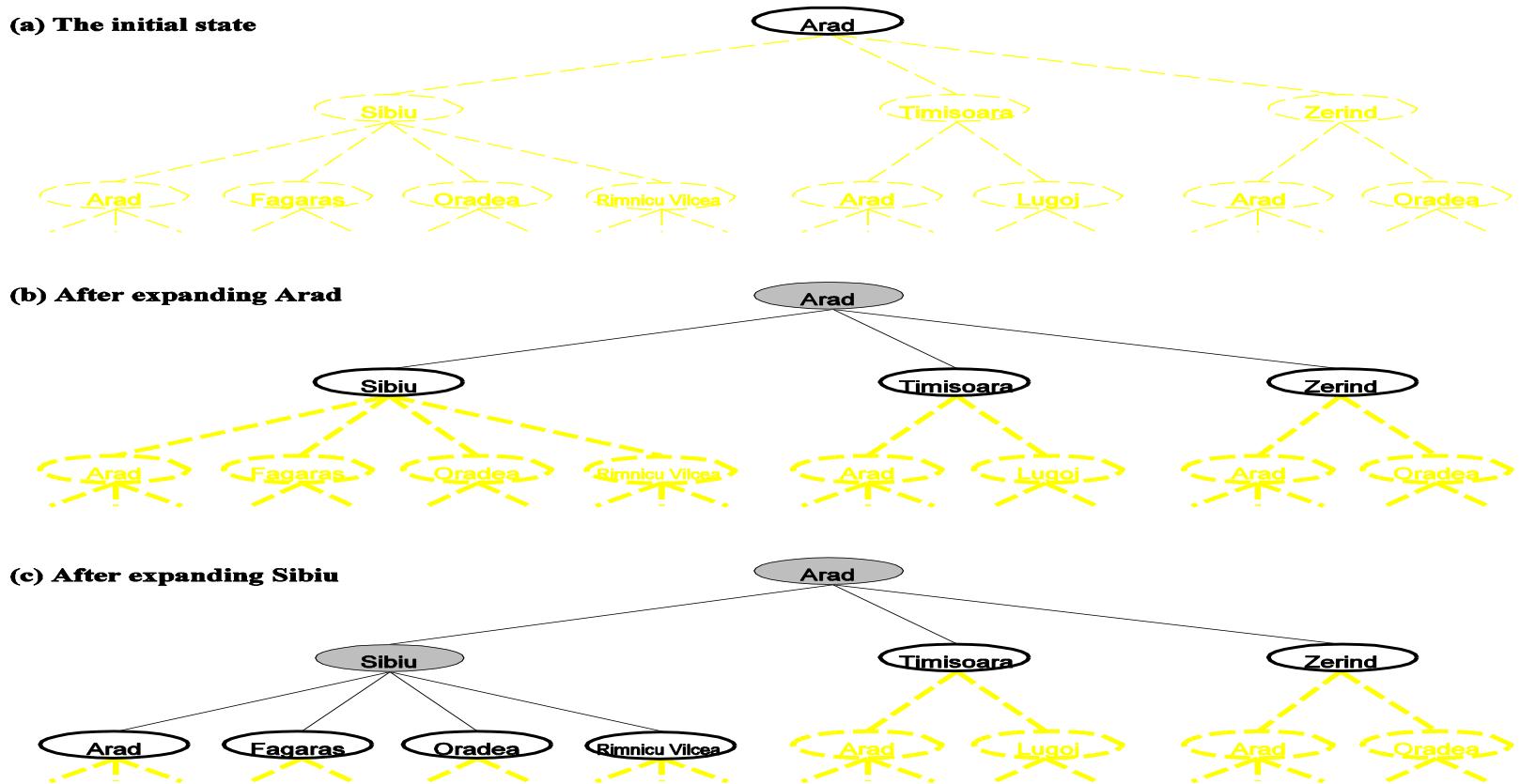
# Data Structures for Search

- Basic data structure: **Search Node**
  - State
  - Parent node and operator applied to parent to reach current node
  - Cost of the path so far
  - Depth of the node



# Expanding Nodes

- Expanding a node
  - Applying all legal operators to the state contained in the node and generating nodes for all corresponding successor states



# Generic Search Algorithm

1. Initialize search algorithm with initial state of the problem
2. **Repeat**
  1. If no candidate nodes can be expanded, **return failure**
  2. Choose leaf node for expansion, according to **search strategy**
  3. If node contains a goal state, **return solution**
  4. Otherwise, expand the node, by applying legal operators to the state within the node. Add resulting nodes to the tree

# Implementation Details

- We need to keep track only of nodes that need to be expanded (**fringe**)
  - Done by using a (prioritized) **queue**

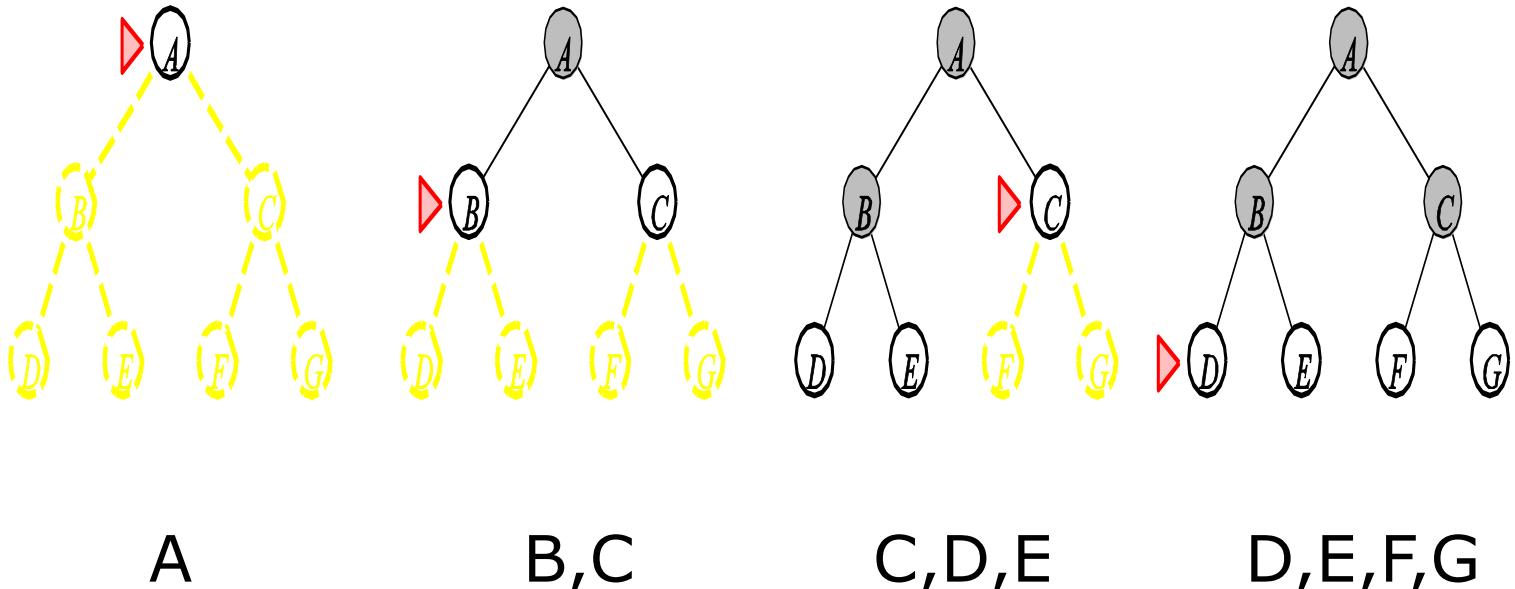
1. Initialize queue by inserting the node corresponding to the initial state of the problem
2. Repeat
  1. If queue is empty, **return failure**
  2. Dequeue a node
  3. If the node contains a goal state, **return solution**
  4. Otherwise, expand node by applying legal operators to the state within. Insert resulting nodes into queue

**Search algorithms differ in their queuing function!**

# Breadth-first search

All nodes on a given level are expanded before any node on the next level is expanded.

Implemented with a FIFO queue



# Evaluating search algorithms

- **Completeness:** Is the algorithm guaranteed to find a solution if a solution exists?
- **Optimality:** Does the algorithm find the optimal solution (lowest path cost of all solutions)?
- **Time complexity**
- **Space complexity**

Variables	
b	Branching factor
d	Depth of shallowest goal node
m	Maximum length of any path in the state space

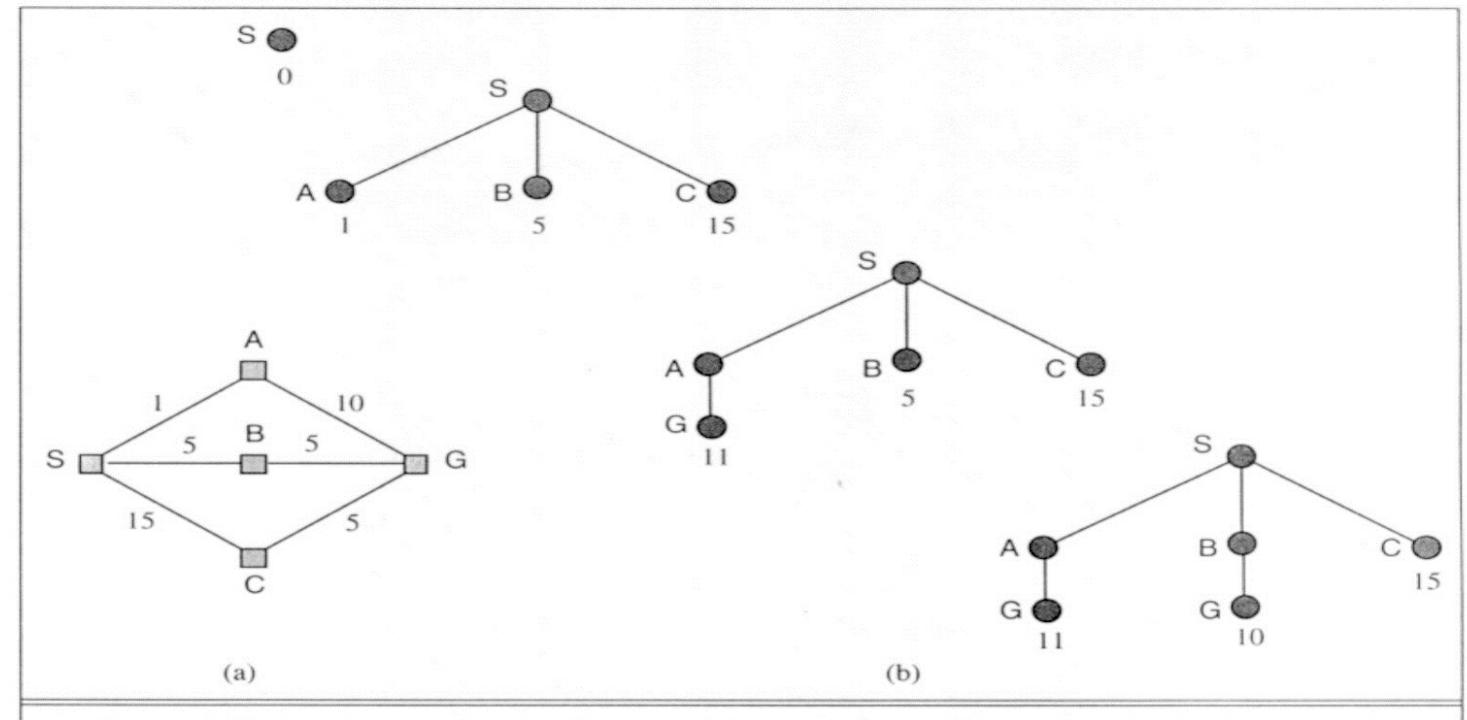
# Judging BFS

- **Complete:** Yes, if  $b$  is finite
- **Optimal:** Yes, if all costs are the same
- **Time:**  $1+b+b^2+b^3+\dots+b^d = O(b^d)$
- **Space:**  $O(b^d)$

All uninformed search methods will have exponential time complexity ☹

# Uniform Cost Search

- Variation of breadth-first search
  - Instead of expanding shallowest node, it expands the node with lowest path cost
  - Implemented using a priority queue



**Figure 3.13** A route-finding problem. (a) The state space, showing the cost for each operator. (b) Progression of the search. Each node is labelled with  $g(n)$ . At the next step, the goal node with  $g = 10$  will be selected.

$C^*$  is cost of optimal solution  
 $\varepsilon$  is minimum action cost

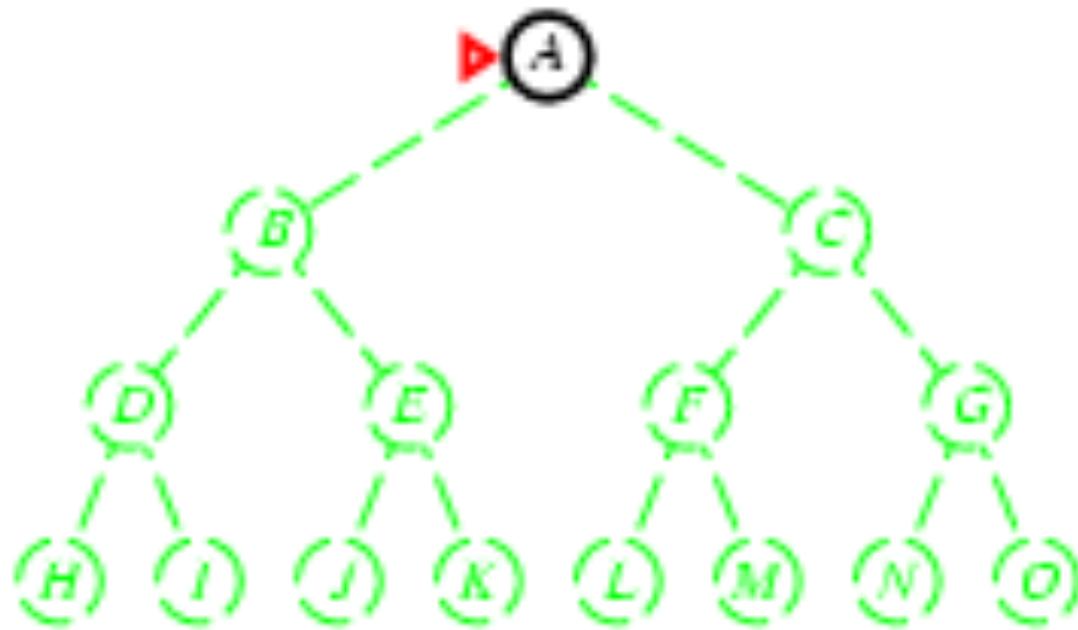
**Optimal:** Yes  
**Complete:** if  $\varepsilon > 0$

**Time:**  $O(b^{\lceil C^*/\varepsilon \rceil})$   
**Space:**  $O(b^{\lceil C^*/\varepsilon \rceil})$

# Depth-first search

The deepest node in the current fringe of the search tree is expanded first.

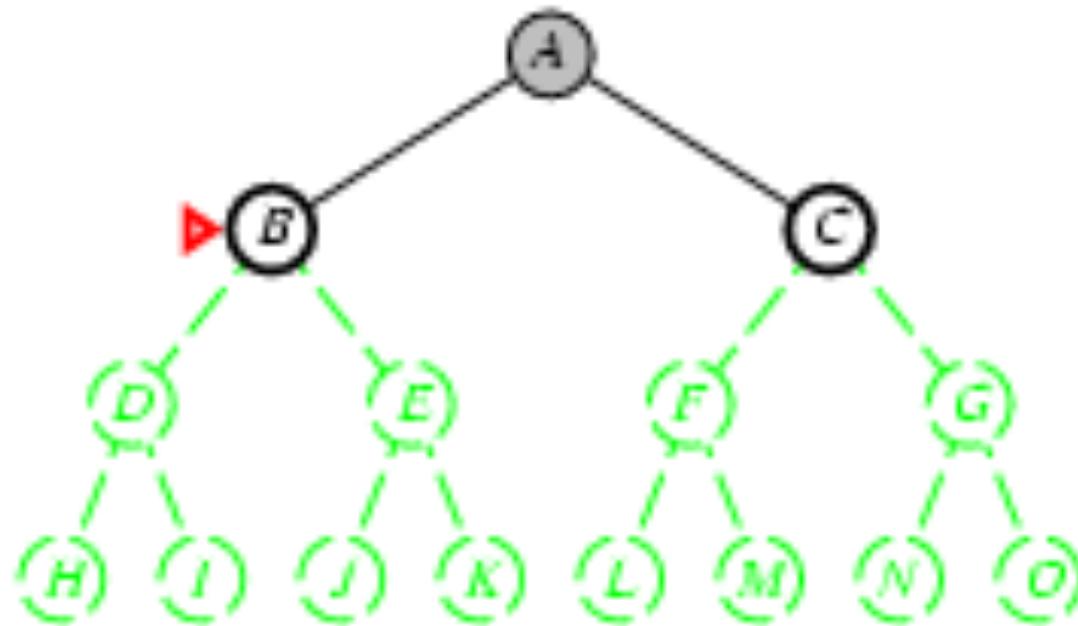
Implemented with a stack (LIFO queue)



# Depth-first search

The deepest node in the current fringe of the search tree is expanded first.

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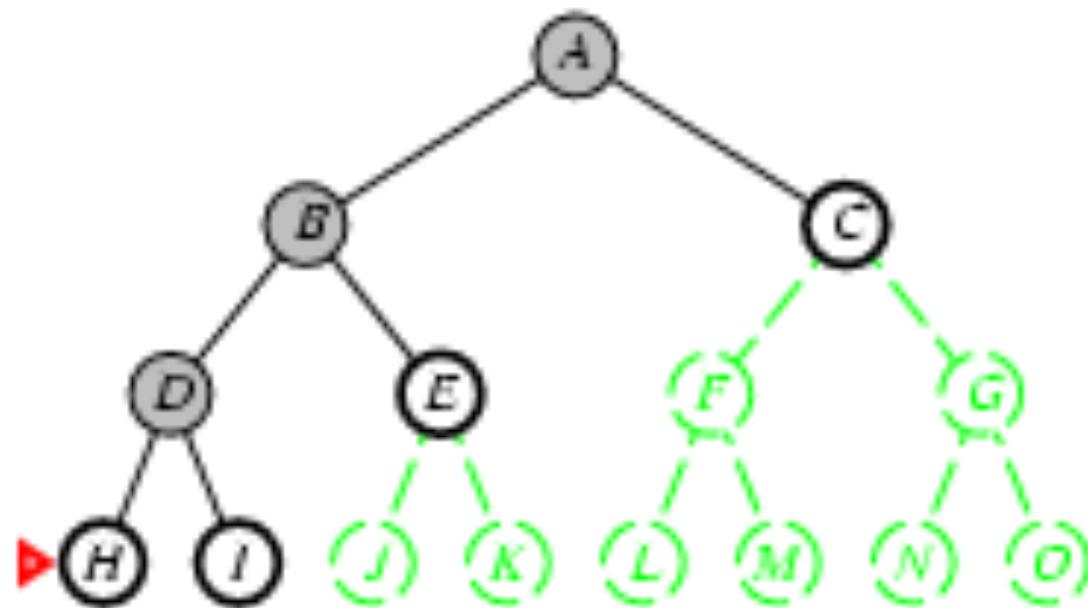
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# Depth-first search

The deepest node in the current fringe of the search tree is expanded first.

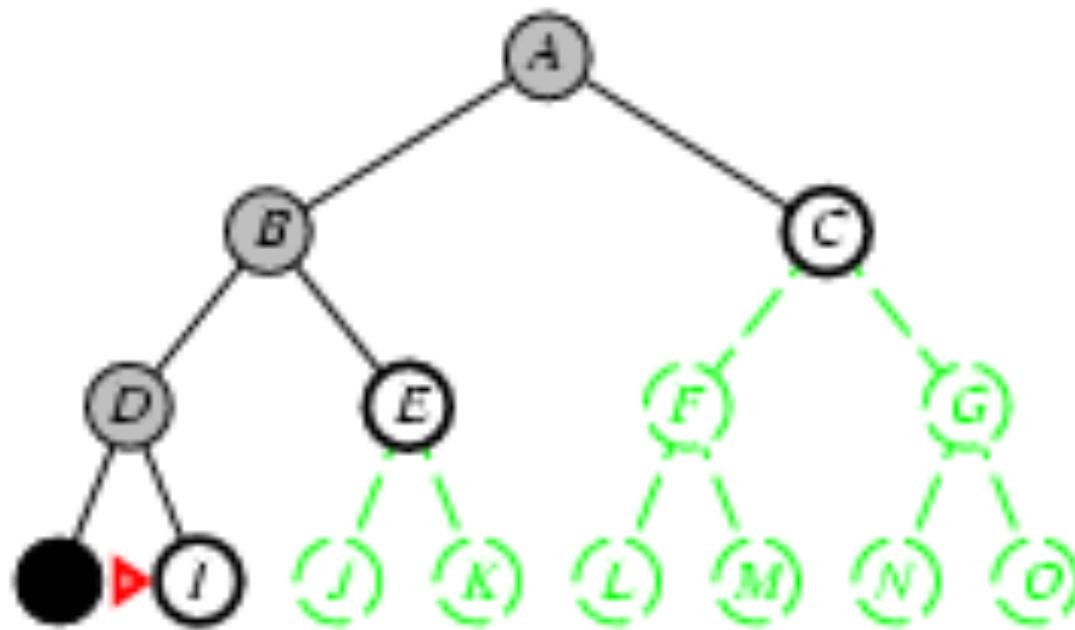
Implemented with a stack (LIFO queue)



# Depth-first search

The deepest node in the current fringe of the search tree is expanded first.

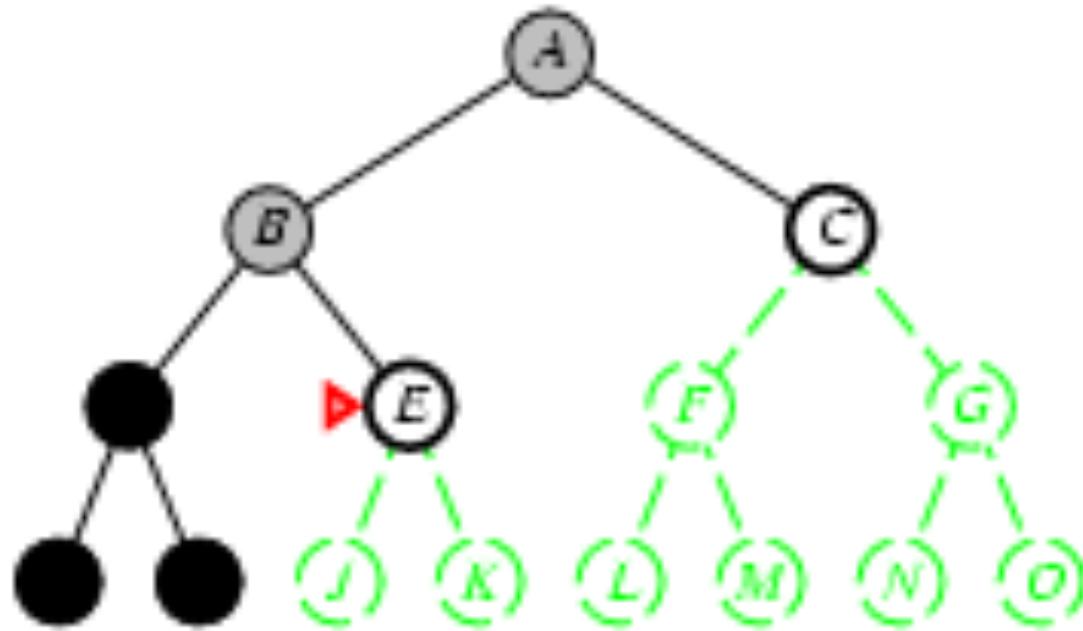
Implemented with a stack (LIFO queue)



# Depth-first search

The deepest node in the current fringe of the search tree is expanded first.

Implemented with a stack (LIFO queue)



# Judging DFS

- **Complete?** No, might get stuck going down a long path
- **Optimal?** No, might return a solution which is deeper (i.e. more costly) than another solution
- **Time:**  $O(b^m)$ ,  $m$  might be larger than  $d$
- **Space:**  $O(bm)$  ☺

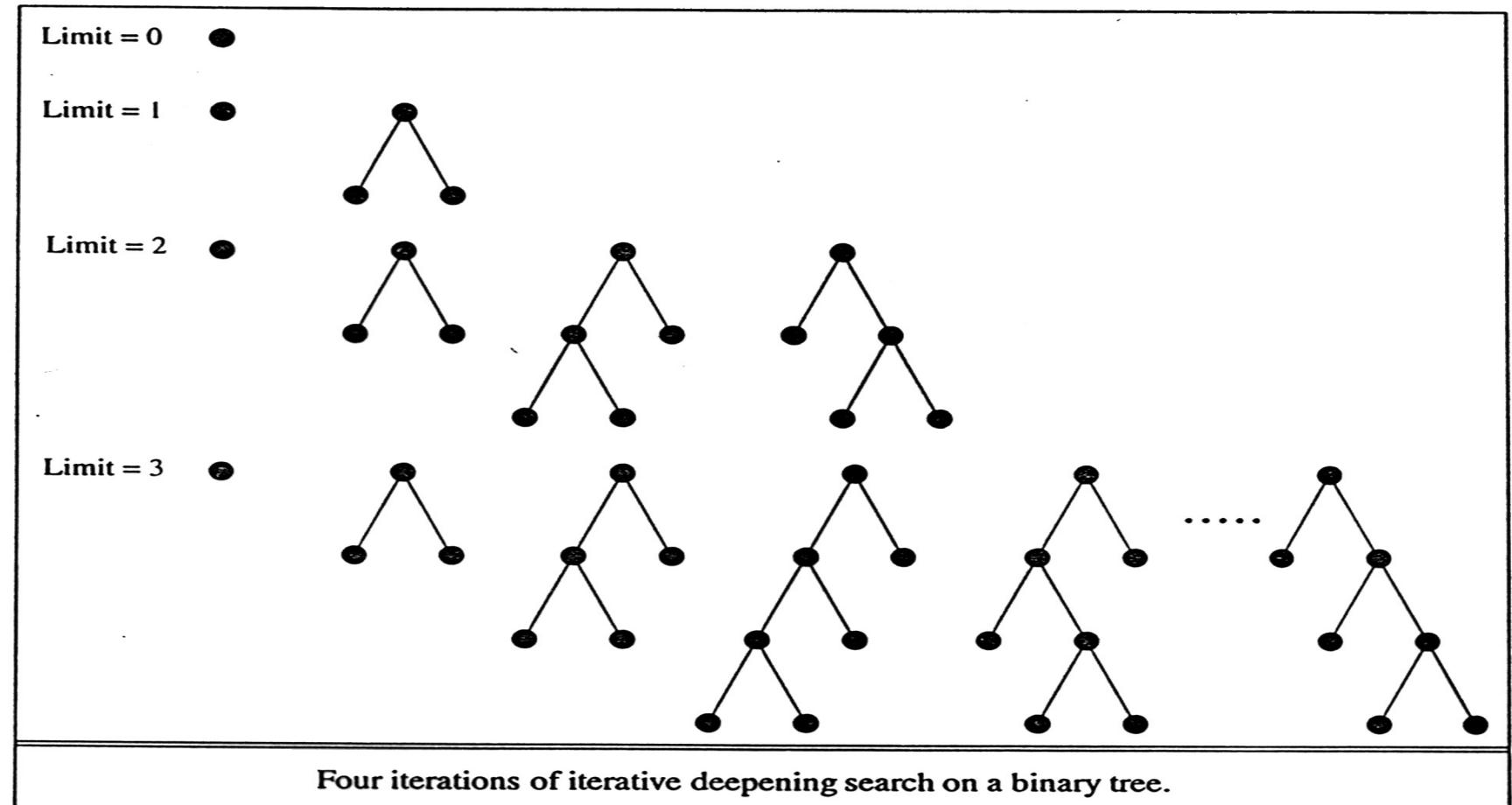
Do not use DFS if you suspect a large tree depth

# Depth-limited Search

- We can avoid the problem of unbounded trees by using a **depth limit**,  $l$ 
  - All nodes at depth  $l$  as though they have no successors
  - If possible, choose  $l$  based on knowledge of the problem
- **Time:**  $O(b^l)$
- **Space:**  $O(bl)$
- **Complete?** No
- **Optimal?** No

# Iterative-deepening

- General strategy that repeatedly does depth-limited search, but increases the limit each time



# Iterative-deepening

IDS is not as wasteful as one might think.

Note, most nodes in a tree are at the bottom level. It does not matter if nodes at a higher level are generated multiple times.

**Breadth first search :**

$$1 + b + b^2 + \dots + b^{d-1} + b^d$$

E.g.  $b=10, d=5: 1+10+100+1,000+10,000+100,000 = 111,111$

**Iterative deepening search :**

$$(d+1)*1 + (d)*b + (d-1)*b^2 + \dots + 2b^{d-1} + 1b^d$$

E.g.  $6+50+400+3000+20,000+100,000 = 123,456$

Complete, Optimal,  $O(b^d)$  time,  $O(bd)$  space

# Summary

- Problem formulation usually requires abstracting away real-world details to define a state space that can feasibly be explored
- Variety of uninformed search strategies
  - Assume no knowledge about the problem (general but expensive)
  - Mainly differ in the order in which they consider the states

Criteria	BFS	Uniform	DFS	DLS	IDS
<b>Complete</b>	Yes	Yes	No	No	Yes
<b>Time</b>	$O(b^d)$	$O(b^{\lceil C^*/\varepsilon \rceil})$	$O(b^m)$	$O(b^l)$	$O(b^d)$
<b>Space</b>	$O(b^d)$	$O(b^{\lceil C^*/\varepsilon \rceil})$	$O(bm)$	$O(bl)$	$O(bd)$
<b>Optimal</b>	Yes	Yes	No	No	Yes

# Summary

- Iterative deepening uses only **linear space** and not much more time than other uninformed search algorithms
  - Use IDS when there is a large state space and the maximum depth of the solution is unknown
- Things to think about:
  - What about searching graphs?
  - Repeated states?