# Lecture 8: Causal Inference CS486/686 Intro to Artificial Intelligence

2023-6-6

Pascal Poupart
David R. Cheriton School of Computer Science



## **Outline**

- Models
  - Causal Bayesian Networks
  - Structural Causal Models
- Causal inference
  - Interventions
  - Counterfactuals



## Causality

 Causality is the study of how things influence one other, how causes lead to effects.

- Causal dependence: X causes Y iff changes to X induce changes to Y
  - Example: Diseases cause symptoms, but symptoms do not cause diseases

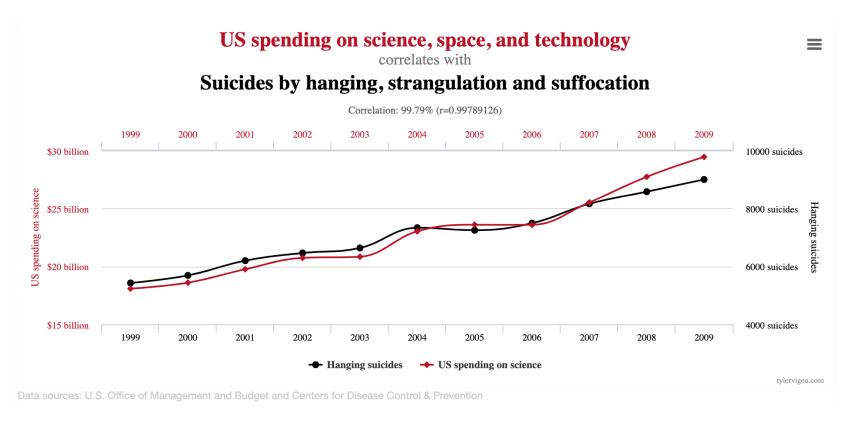


#### **Causal and Non-Causal Correlations**

- A **joint distribution** P(X,Y) **captures correlations** between X and Y, but does not indicate whether a causal relation exists between X and Y nor the direction of the causal relation when it exists.
- A conditional distribution P(Y|X) does not necessarily indicate X causes Y
  - Recall Bayes' rule:  $P(Y|X) = \frac{\Pr(X|Y)P(Y)}{P(X)}$
  - Since we can transform P(X|Y) into P(Y|X), conditional distributions do not always indicate causal dependences, otherwise Y would cause X and X would cause Y



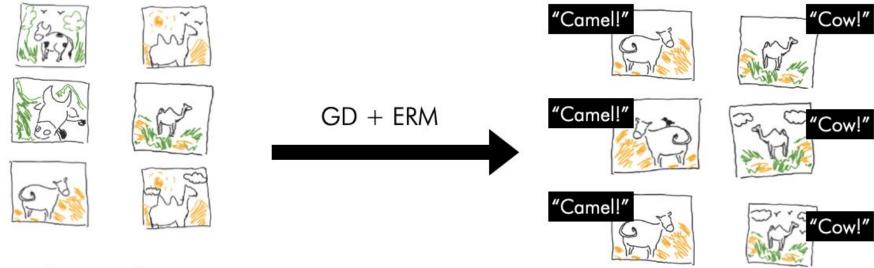
# **Spurious Correlations**



From https://www.tylervigen.com/spurious-correlations



## **Spurious Correlations**



Training domain

Cows: 90% green background

Camels: 90% yellow background

Cows: 0% green background

Test domain

Camels: 0% yellow background

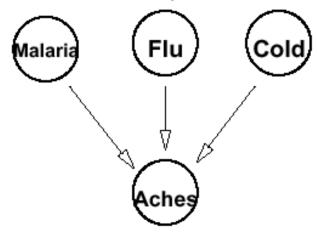
Standard example (Beery et al., '18 Arjovsky et al., '19)



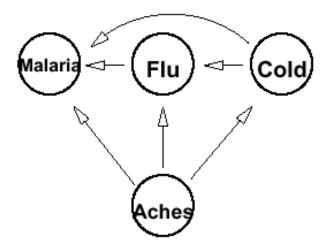
## **Causal Bayesian Network**

Definition: Bayesian network where all edges indicate direct causal effects.

Causal Bayes net



Probabilistic Inference Causal Inference Non-causal Bayes net



**Probabilistic Inference** 



#### **Causal Inference**

**Intervention:** What is the effect of an action?

E.g., What is the effect of a treatment?

Causal networks can easily support intervention queries, but not non-causal networks do not.



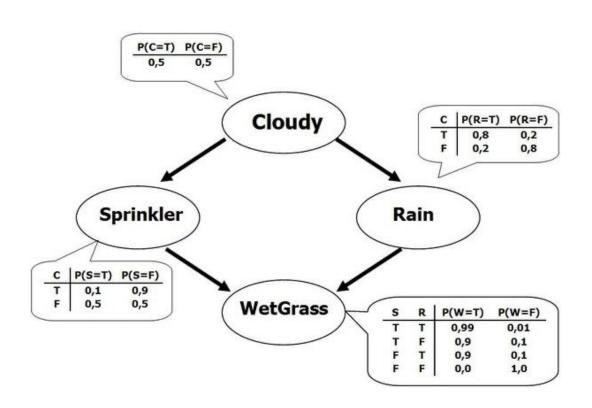
#### **Observation versus Intervention**

**Observation:** What is the likelihood that the grass is wet when the sprinkler is observed to be on?

$$P(WG|S = true)$$
?

**Intervention:** How does turning on the sprinkler affect the grass?

$$P(WG|do(S = true))$$
?





## **Do Operator**

#### **Observational query:**

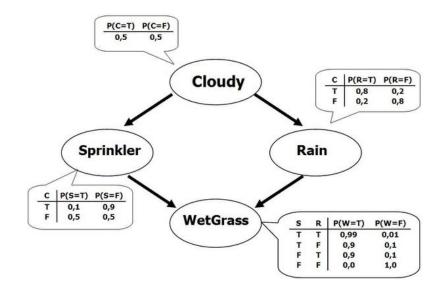
P(WG|S = true)?

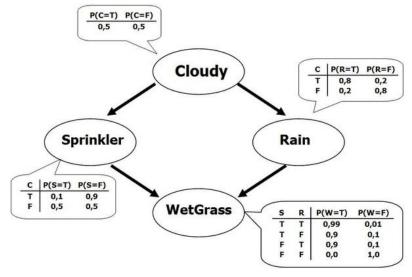
- Factors:
- Evidence:
- Eliminate:

#### **Intervention query:**

P(WG|do(S = true))?

- Factors:
- Evidence:
- Eliminate:







## Inference with Do Operator

$$P(X|do(Y = y), Z = z)$$

#### In a causal graph:

- 1) Remove edges pointing to Y and P(Y|parents(Y))
- 2) Perform variable elimination on remaining graph:
  - a) Restrict factors to evidence: Y = y and Z = z
  - b) Eliminate variables
  - e) Multiply remaining factors and normalize



## **Non-Causal Graph**

#### **Observational query:**

$$P(WG|S = true)$$
?

- Factors:
- Evidence:
- Eliminate:

#### **Intervention query:**

$$P(WG|do(S = true))$$
?

- Factors:
- Evidence:
- Eliminate:



## **Counterfactual Analysis**

**Intervention:** What is the effect of an action?

E.g., What is the effect of a treatment?

Counterfactual analysis (or counterfactual thinking): explores outcomes that did not actually occur, but which could have occurred under different conditions. It's a kind of what if? analysis and is a useful way for testing cause-and-effect relationships.

E.g., Would the patient have died if he was not treated?

E.g., Would a goal be scored had the player not tripped?



## **Counterfactual Analysis**

How can we answer counterfactual questions with a causal Bayes net?

Treatment → Dead

Fact: patient was treated and then died

**Counterfactual question:** Had the patient not been treated, would the patient have survived?

Can't answer this question since we can't revive the patient to try no treatment...



#### **Structural Causal Models**

Idea: separate causal relations from noise

#### Structural Causal Model contains:

- X: endogenous variables (domain variables)
- U: exogenous variables (noise)
- Only deterministic relations given by equations
  - $X_i = f(parents(X_i), U_i)$



## **Conversion**

 Structural Causal Models (SCMs) can be converted into equivalent Causal Bayesian Network, but not the other way around

 SCMs separate causal relations from the noise and therefore provide more information

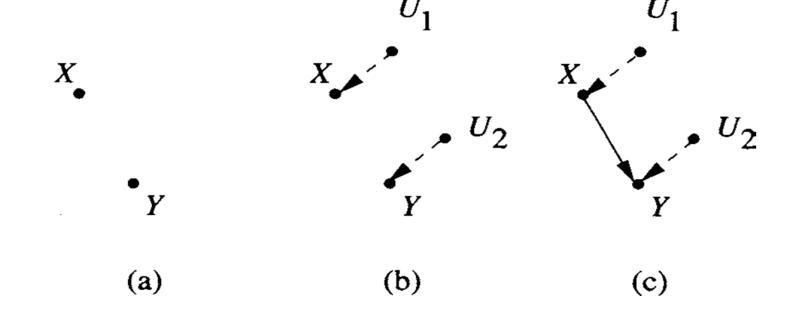


## **Example**

Let P(X,Y) be uniformly distributed i.e.,  $P(X=x,Y=y)=0.25 \ \forall x,y$ 

*X*: treatment

Y: dead



# **Example**

Model B	$u_2=0$		$u_2=1$		Marginal	
	x = 1	x = 0	x = 1	x = 0	x = 1	x = 0
y = 1 (death)	0	0	0.25	0.25	0.25	0.25
y = 0 (recovery)	0.25	0.25	0	0	0.25	0.25
Model C	$u_2=0$		$u_2 = 1$		Marginal	
Model C	$u_2$	= 0	$u_2$	= 1	Mar	ginai
Model C	-	x = 0	_	x = 0	x = 1	x = 0
Model C $y = 1 \text{ (death)}$	-		_			_



## **Counterfactual Analysis**

These three steps can be generalized to any causal model M as follows. Given evidence e, to compute the probability of Y = y under the hypothetical condition X = x (where X is a subset of variables), apply the following three steps to M.

**Step 1 (abduction):** Update the probability P(u) to obtain  $P(u \mid e)$ .

**Step 2 (action):** Replace the equations corresponding to variables in set X by the equations X = x.

**Step 3 (prediction):** Use the modified model to compute the probability of Y = y.



# **Example**

Model b:

Model c:



# **DoWhy Library (Microsoft)**

https://github.com/py-why/dowhy

Case Studies using DoWhy: Hotel booking cancellations | Effect of customer loyalty programs | Optimizing article headlines | Effect of home visits on infant health (IHDP) | Causes of customer churn/attrition

