# Lecture 11

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## Outline

- Decision Networks
  Aka Influence diagrams
  Value of information
- Russell and Norvig: Sect 16.5-16.6



- add decision variables variables that you "control"
- add utility variables how good different states are

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- i.e., for any instantiation of parents, value of Drug is fixed by policy  $\delta_D$
- this means we can solve for optimal policy for BT just as before
- only uninstantiated vars are random vars (once we fix *its* parents)

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# Optimizing Policies: Key Points When a decision D node is optimized, it can be treated as a random variable for each instantiation of its parents we now know what value the decision should take

- just treat policy as a new CPT: for a given parent instantiation x, D gets d(x) with probability 1 (all other decisions get probability zero)
- If we optimize from last decision to first, at each point we can optimize a specific decision by (a bunch of) simple VE calculations
  - it's successor decisions (optimized) are just normal nodes in the BNs (with CPTs)

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- Decision networks commonly used by decision analysts to help structure decision problems
- Much work put into computationally effective techniques to solve these
  - common trick: replace the decision nodes with random variables at outset and solve a plain Bayes net (a subtle but useful transformation)
- Complexity much greater than BN inference
  - we need to solve a number of BN inference problems
    one BN problem for each setting of decision node
  - one BN problem for each setting of decision node parents and decision node value

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- Setting: you want to buy a used car, but there's a good chance it is a "lemon" (i.e., prone to breakdown). Before deciding to buy it, you can take it to a mechanic for inspection. S/he will give you a report on the car, labeling it either "good" or "bad". A good report is positively correlated with the car being sound, while a bad report is positively correlated with the car being a lemon.
- The report costs \$50 however. So you could risk it, and buy the car without the report.
- Owning a sound car is better than having no car, which is better than owning a lemon. 19











## Alternatively

- N.B.: variable elimination for decision networks computes unscaled expected utility...
- Can still pick best action, since utility scale is not important (relative magnitude is what matters)
- If we want exact expected utility:
  - Let X = parents(U)
  - EU(dec|evidence) =  $\Sigma_X Pr(X|dec,evidence) U(X)$
  - Compute  $\Pr(\mathbf{X} | \text{dec,evidence})$  by variable elimination

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- Multiply Pr(X | dec, evidence) by U(X)
- Summout X

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## Evaluate First Decision: Inspect

- $EU(I) = \Sigma_{L,R} P(L,R|i) U(L,i, \delta_{Buy} (I,R))$ 
  - where P(R,L|i) = P(R|L,i)P(L|i)
  - EU(i) = (.1)(-650)+(.4)(-350)+(.45)(950)+(.05)(-350) = 187.5
  - EU(~i) = P(n,||~i) U(l,~i,buy) + P(n,~l|~i) U(~l,~i,buy) = .5\*-600 + .5\*1000 = 200
  - So optimal δ<sub>Inspect</sub> () = ~inspect

		P(R,L   i)	$\delta_{Buy}$	U(L, i, <i>δ<sub>Buy</sub></i> )	
7	g,l	0.1	buy	-600 - 50 = -650	
	b,I	0.4	~buy	-300 - 50 = -350	1
	g,~I	0.45	buy	1000 - 50 = 950	1
	b,~l	0.05	~buy	-300 - 50 = -350	2





