

# Perception

July 21, 2005  
CS 486/686  
University of Waterloo

# Outline

- Perception
  - Computational vision
- Reading: R&N Sect. 24.1-24.3

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# Perception

- Perception provides agents with information about the world
- Perception is initiated by sensors:
  - Microphones
  - Laser range finders
  - Sonars
  - Movement detectors
  - Video cameras (vision)
  - Etc.

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# Computational Vision

- Vision: very rich perception mode
- Computational vision:
  - Set of algorithmic/computational approaches to perceive the world from images
  - Focus on image analysis (more than image capture)
  - Inspired by the human vision system

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# Vision vs Graphics

- Image formation:
  - $f(\text{world}) \rightarrow \text{image}$
  - Field of graphics
- Image analysis:
  - $f^{-1}(\text{image}) \rightarrow \text{world}$
  - Field of computational vision

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# Image analysis

- Analysis of the information in a scene

- For instance, what are the
  - objects?
  - object properties?
  - object relations?



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## Video sequence analysis

- Info analysis in a frame sequence

- For instance, what are the
  - events?
  - object movements?



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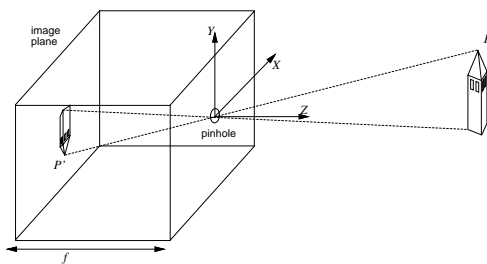
## Image Formation

- Vision gathers light scattered from objects in a scene and creates a two-dimensional image
- Image plane:
  - Coated with photosensitive material
- Digital image:
  - Rectangular grid of a few million pixels

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## Pin-hole camera



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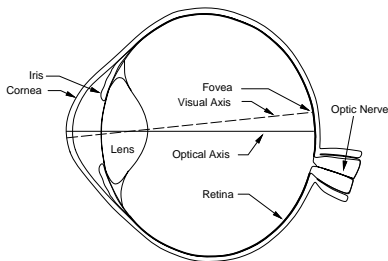
## Pin-hole camera

- $P=(X,Y,Z)$  in scene  $\rightarrow P'=(x',y',f)$  in image
- Distance equations:
  - $-x/f = X/Z \rightarrow x = -fX/Z$
  - $-y/f = Y/Z \rightarrow y = -fY/Z$
- Proportions are preserved
- Minus sign means that image is inverted

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## Human eye



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## Lens systems

- Pin-hole system is a rough approximation of lens system
- With lens
  - let in more light than a pin-hole
  - But image may be out of focus

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## Photometry

- **Photometry** is the study of light
- Light is crucial for vision
- Pixel brightness measures **light intensity**  $I(x,y)$
- But light is emitted/reflected by many objects
  - This complicates image analysis!

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## Spectrophotometry

- Light comes in different colors
- Colors correspond to different wave lengths
- All colors perceived by human eyes correspond to linear combinations of
  - Red (700 nm)
  - Green (546 nm)
  - Blue (436 nm)
- Pixel often an **RGB** measurement

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## Model-based vision

- Since  $\text{image} = f(\text{world})$ ,
  - Understand  $f$ 
    - Photometry, spectrophotometry, physics, camera engineering, etc.
  - Compute  $\text{world} = f^{-1}(\text{image})$ 
    - But  $f$  is not completely understood
    - $f$  is often noisy
    - So how can we compute  $f^{-1}$ ?

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## Statistical vision

- To model uncertainty, let
  - $f: \text{world} \rightarrow \text{image}$  becomes  $P(\text{image}|\text{world})$
  - $f^{-1}: \text{image} \rightarrow \text{world}$  becomes  $P(\text{world}|\text{image})$
- Image analysis: compute most likely world for a given image
  - $\text{world}^* = \text{argmax}_{\text{world}} P(\text{world}|\text{image})$
  - but where do we get  $P(\text{world}|\text{image})$ ?

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## Statistical Vision

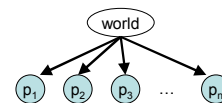
- Could use **Bayes Theorem**:
  - $\text{world}^* = \text{argmax}_{\text{world}} P(\text{world}|\text{image})$
  - =  $\text{argmax}_{\text{world}} P(\text{image}|\text{world})P(\text{world})$
  - Called the generative approach
- Could use **machine learning**
  - Learn  $f^{-1}$  or  $P(\text{world}|\text{image})$  from data
  - E.g. neural networks

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## Generative Approach

- One random variable per pixel
- Assume pixels generated independently
  - $P(\text{image}|\text{world}) = \prod_i P(\text{pixel}_i|\text{world})$
  - Naive Bayes model

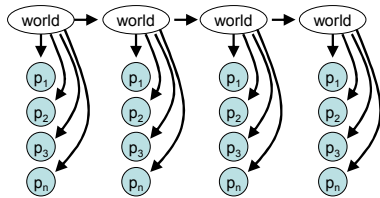


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## Generative Approach

- For video sequences:
  - Hidden Markov model



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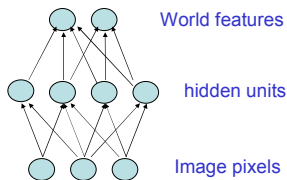
## Generative Approach

- It is a **principled approach**
- **But often intractable...**
  - "world" is too complex and must be decomposed
  - Too many pixels

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## Neural Networks



- Problems:
  - Too many pixels
  - Difficult to capture invariance

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## Image Processing

- Images contain millions of pixels
  - But many pixels may be uninformative
  - Extract **relevant features**
- Image processing
  - Extract all kinds of low level features
    - E.g., edges, corners
  - Then extract higher level information

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## Smoothing

- To handle pixel noise, smooth the image:
  - Pixel intensity  $\leftarrow$  (weighted) average of neighbors' intensity
- Gaussian filter
  - Assign weights proportional to Gaussian distribution
  - E.g.  $I(x_0, y_0) = \sum_{x,y} I(x,y) G_\sigma(d)$ 
    - Where  $d$  is the distance between  $(x_0, y_0)$  and  $(x,y)$
    - And  $G_\sigma(d) = e^{-d^2/2\sigma^2} / [\text{sqrt}(2\pi)\sigma^2]$

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## Convolution

- Convolution  $h = f * g$ 
  - $h(x) = \sum_u f(u) g(x-u)$
- Hence, **smoothing is a convolution** of  $I$  with  $G_\sigma$ 
  - i.e.,  $I * G_\sigma$

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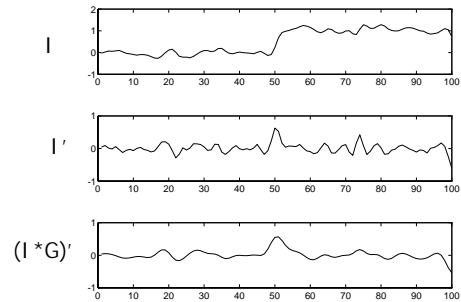
## Edge Detection

- Edges:
  - Sharp change in intensity  $I$
  - Idea: compute derivative of intensity  $I'$
- Noise:
  - But noise could cause sharp intensity changes
  - Solution: smooth before edge detection
  - Hence compute  $(I * G)'$

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## 1D edge detection



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## Optimized edge detection

- Smoothed edge detection:  $(I * G)'$
- Theorem:  $(f * g)' = f * g'$
- Proof:
  - $(f * g)' = \partial[\sum_u f(u) g(x-u)] / \partial x$
  - $= \sum_u f(u) \partial g(x-u) / \partial x$
  - $= \sum_u f(u) g'(x-u)$
  - $= f * g'$
- Hence  $(I * G)' = I * G'$

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## 2D Edge Detection

- Edges can have any orientation
- Can we avoid differentiating in all directions?
  - Yes: differentiate w.r.t  $x$  and  $y$  separately
- Compute:
  - $R_V(x,y) = I(x,y) * [G'_\sigma(x)G_\sigma(y)]$
  - $R_H(x,y) = I(x,y) * [G'_\sigma(y)G_\sigma(x)]$
  - $R(x,y) = R_H(x,y)^2 + R_V(x,y)^2$

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## Next Class

- Next Class:
  - Robotics
  - Russell and Norvig Ch. 25

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