# CS480/680 Lecture 16: July 2, 2019

Convolutional Neural Networks [GBC] Chap. 9

# Large networks

 What kind of neural networks can be used for large or variable length input vectors (e.g., time series)?

- Common networks:
  - Convolutional networks
  - Recursive networks
  - Recurrent networks

### Convolution

• Convolution: mathematical operation on two functions x() and w() that produces a third function y() that can be viewed as a modified version of one of the original functions x()

$$y(i) = \int_{t} x(t)w(i-t)dt$$
$$y(i) = (x * w)(i)$$

Where \* is an operator denoting a convolution

# **Example Smoothing**

### Discrete convolution

Discrete convolution

$$y(i) = \sum_{t=-\infty}^{\infty} x(t)w(i-t)$$

Multidimensional convolution

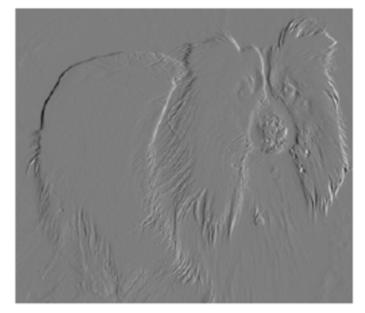
$$y(i,j) = \sum_{t_1 = -\infty}^{\infty} \sum_{t_2 = -\infty}^{\infty} x(t_1, t_2) w(i - t_1, j - t_2)$$

# Example: Edge Detection

- Consider a grey scale image
- Detect vertical edges: y(i,j) = x(i,j) x(i-1,j)

hence 
$$w(i - t_1, j - t_2) = \begin{cases} 1 & t_1 = i, t_2 = j \\ -1 & t_1 = i - 1, t_2 = j \\ 0 & \text{otherwise} \end{cases}$$





### Convolutions for feature extraction

- In neural networks
  - A convolution denotes the linear combination of a subset of units based on a specific pattern of weights.

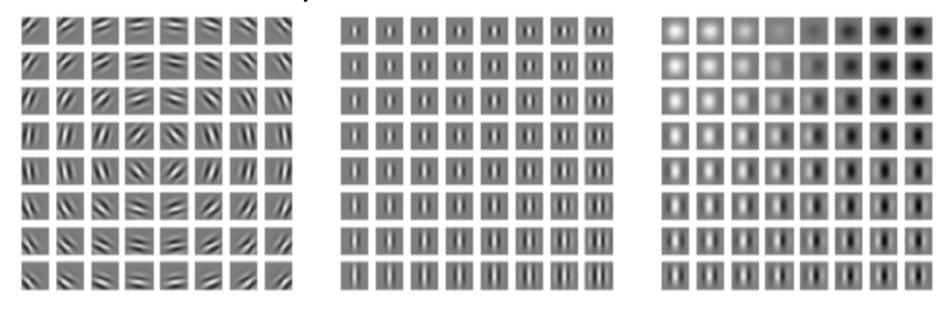
$$a_j = \sum_i w_{ji} z_i$$

Convolutions are often combined with an activation function to produce a feature

$$z_j = h(a_j) = h\left(\sum_i w_{ji} z_i\right)$$

### Gabor filters

 Gabor filters: common feature maps inspired by the human vision system



Weights:

Grey: zero White: positive Black: negative

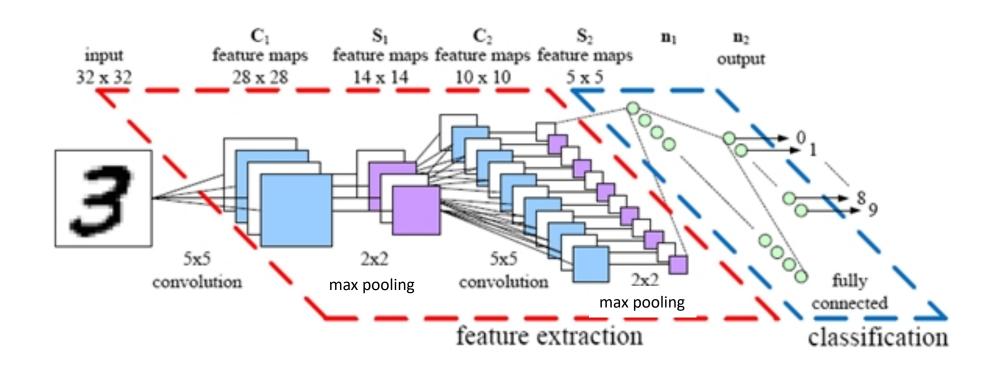
### **Convolution Neural Network**

- A convolutional neural network refers to any network that includes an alternation of convolution and pooling layers, where some of the convolution weights are shared.
- Architecture:

# Pooling

- Pooling: commutative mathematical operation that combines several units
- Examples:
  - max, sum, product, average, Euclidean norm, etc.
- Commutative property (order does not matter): max(a, b) = max(b, a)

## Example: Digit Recognition



### **Benefits**

- Sparse interactions
  - Fewer connections
- Parameter sharing
  - Fewer weights
- Locally equivariant representation
  - Locally invariant to translations
  - Handle inputs of varying length

#### **Parameters**

- # of filters: integer indicating the # of filters applied to each window.
- kernel size: tuple (width, height) indicating the size of the window.
- Stride: tuple (horizontal, vertical) indicating the horizontal and vertical shift between each window.
- **Padding:** "valid" or "same". Valid indicates no input padding. Same indicates that the input is padded with a border of zeros to ensure that the output has the same size as the input.

# Examples

### Training

- Convolutional neural networks are trained in the same way as other neural networks
  - E.g., backpropagation

- Weight sharing:
  - Combine gradients of shared weights into a single gradient

# Architecture design

- What is the preferred filter size?
- VGG (Visual Geometry Group at Oxford, 2014): stack of small filters is often preferred to single large filter
  - Fewer parameters
  - Deeper network
- Picture

### Residual Networks

- Problem: even with ReLU, very deep networks suffer from vanishing gradients
- Solution [He et al., 2015]: introduce residual connections (a.k.a. skip connections) to shorten paths
- Picture:

## **Applications**

- Image processing
- Data with sequential, spatial, or tensor patterns