

# You Just Want Attention

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CS886: Deep Learning and NLP  
Winter 2020

# Charlie Puth Vs. Google Research

- Charlie Puth released his hit “You Just Want Attention” in April 2017 (1B+ views)
- Google Research did not publish “Attention Is All You Need” until June 2017 (5K+ citations)
- Coincidence??



2014

Memory Networks  
Weston >>

RNNSearch  
Bahdanau >>

2015

End-to-End Memory Networks  
Sukhbaatar >>

+ token-level  
Attentive Reader  
Impatient Reader  
Hermann >>

Memory Network on CBT  
Hill >>

Agreement-based Joint Training for Bidirectional Attention-based NMT  
Cheng >>

Grammar as a Foreign Language  
Vinyals >>

Local/Global Input feeding  
Luong >>

Reasoning About Entailment With Neural Attention  
Rocktaschel >>

ABCNN for Modeling Sentence Pairs  
Yin >>

Attention-Based Summarization  
Rush >>

2016

Chen's Attentive Reader  
Chen >>

Q(A)LSTM  
Tan >>

Iterative Alternating Attention  
Sordani >>

Long Short-Term Memory-Networks for Machine Reading  
Cheng >>

Attention Sum Reader  
Kadlec >>

Attention-over-Attention Reader  
Cui >>

Gated Attention reader  
Dhingra >>

Dynamic Coattention networks  
Xiong >>

BiDAF  
Seo >>

NMT with Recurrent Attention Modeling  
Yang >>

Multi-Way, Multilingual Neural Machine Translation with a Shared Attention Mechanism  
Firat >>

Match-LSTM  
Wang, Jiang >>

CSE: Conceptual Sentence Embeddings based on Attention Model  
Wang >>

Attention-Based Summarization  
Chopra >>

Hierarchical Attention Networks for Document Classification  
Yang >>

2017

IARNN  
Wang >>

ReasoNet  
Shen >>

(Reinforced) Mnemonic Reader  
Hu >>

+ gating + multi-pass  
Ruminating Reader  
Gong >>

Transformer  
Vaswani >>

Gated Self-Matching Networks (r-net)  
Wang >>

Structured Attention Networks  
Kim >>

A Structured Self-attentive Sentence Embedding  
Lin >>

Multilingual -|-  
Pappas >>

QA    Summarization    MT    Inference, Entailment

General    multi-pass    Classification

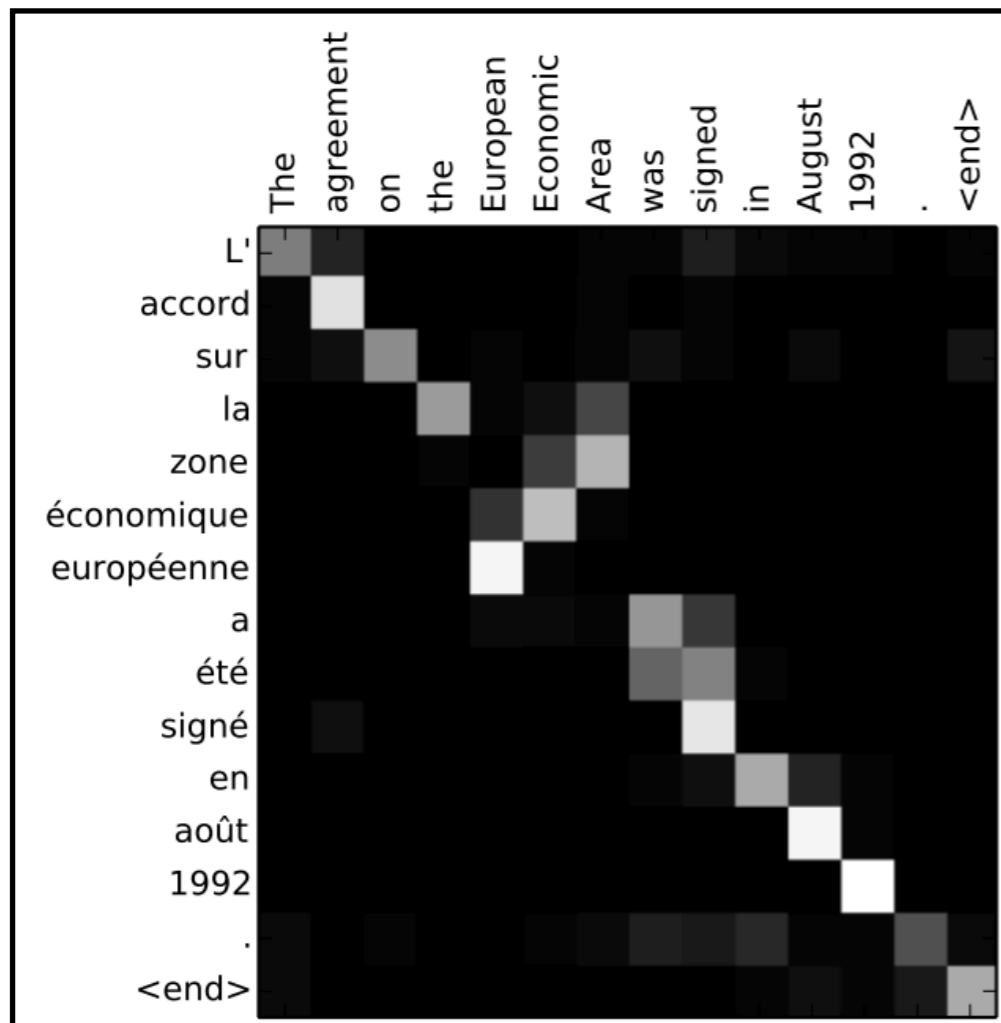
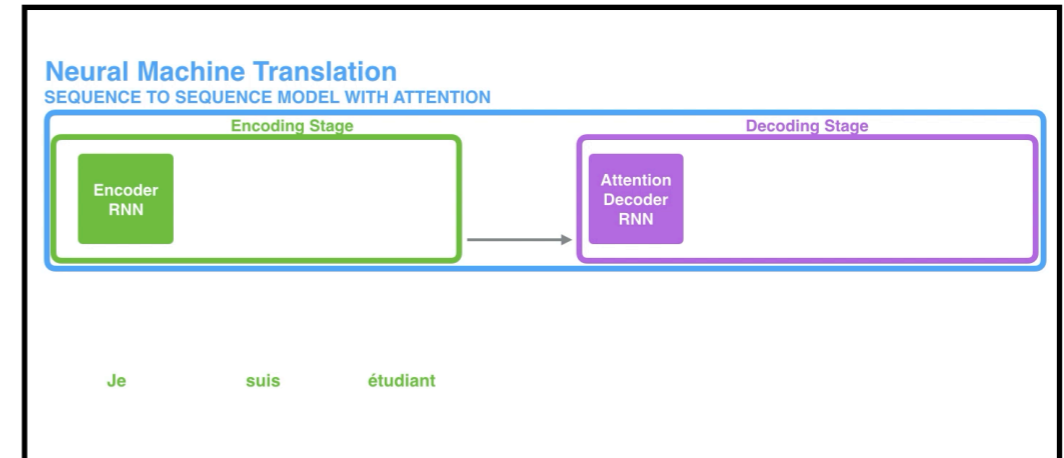
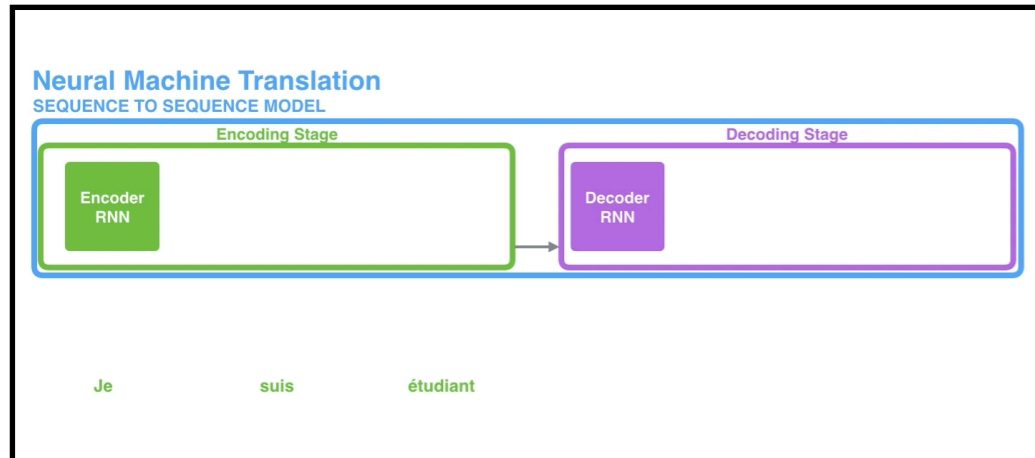
generalization on multiple hops

+ local attention + generalization, simplification for global + alignment decisions based on past alignment information

# Agenda:

- Motivation
- What Is Attention?
- How to Compute Attention?
- Attention Functions
- The Cost of Attention
- Attention in NLP
- BERT Attention Analysis

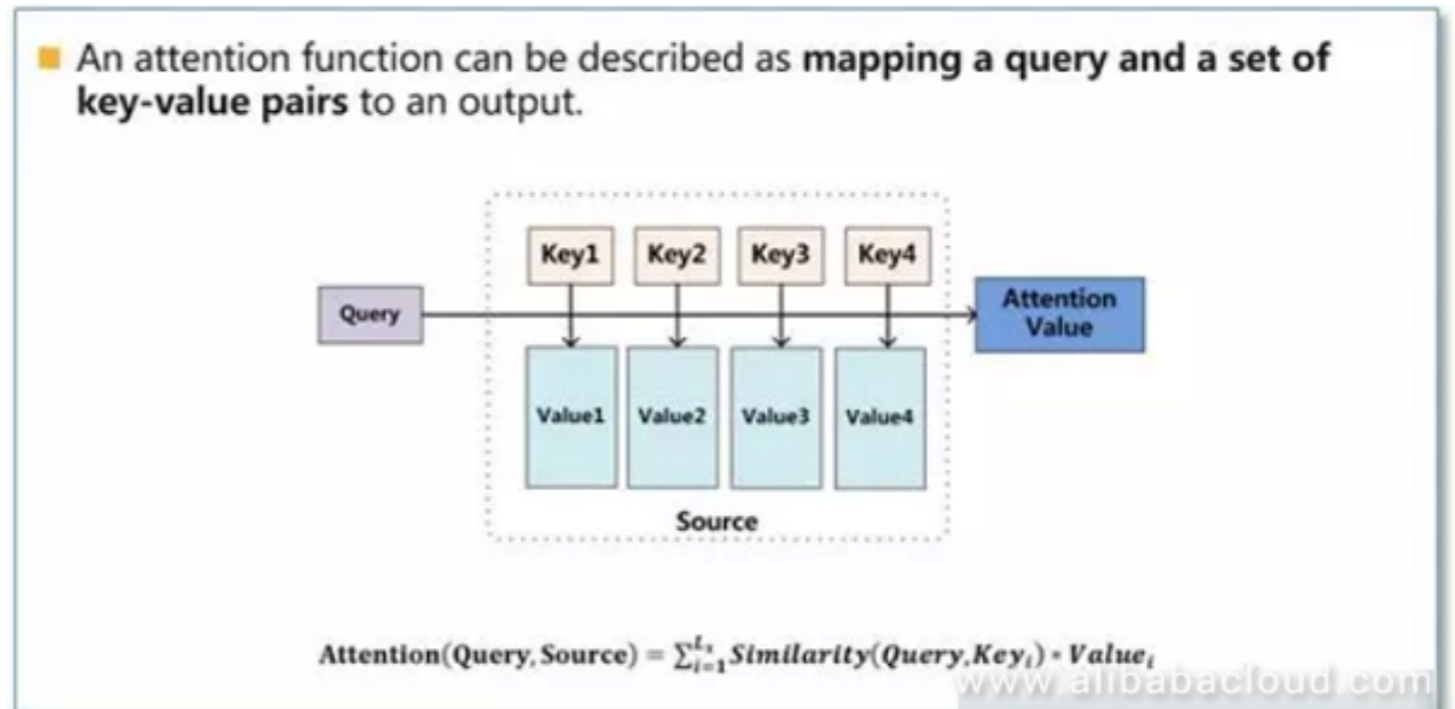
# Motivation



- First proposed in [Bahdanau et al., 2014](#) as an alignment mechanism.
- Basically, Attention allows the model to focus on the relevant parts of the input sequence as needed (Think of how humans pay attention to only most relevant parts of a scene)

# What Is Attention?

- Attention can be described as mapping a query (Q) and a set of key-value pairs (<K, V>) to an output (Z), where the query, keys, values, and output are all vectors.
- The output is computed as a weighted sum of the values, where the weight assigned to each value is computed by a compatibility function (f) of the query with the corresponding key.



The K, V, Q notation is inspired by the information retrieval literature.

# How to Compute Attention?

- Calculating Attention:

1. Similarity between the query and each key to obtain scalar scores.
2. Use a Softmax function to normalize these scores into weights.
3. Apply weighted sum of the values.

- Major components in attention mechanisms:

1. Define  $\langle K, V \rangle$  and  $Q$
2. Choose a similarity function

In a lot of NLP work, the key and value are often the same, therefore  $\text{key}=\text{value}=\text{word-embeddings}$

$$\text{Attention}(Q, K_i, V_i) = \frac{e^{\text{Similarity}(Q, K_i)}}{\sum e^{\text{Similarity}(Q, K_i)}} V_i$$

# Attention Functions

- Additive Attention:
- The attention scores are computed using a Perceptron.
- Example:  
LSTM + Attention

- Multiplicative Attention:
- The attention scores are computed using (scaled/general) dot products.
- Example:  
Transformer

- Additive attention outperforms Multiplicative attention without scaling for larger dimensions, because the dot products grow large in magnitude, pushing the softmax function into regions where it has extremely small gradients.

$$f(Q, K_i) = \begin{cases} Q^T K_i & \text{dot} \\ Q^T W_a K_i & \text{general} \\ W_a [Q; K_i] & \text{concat} \\ v_a^T \tanh(W_a Q + U_a K_i) & \text{perceptron} \end{cases}$$

$$a_i = \text{soft max}(f(Q, K_i)) = \frac{\exp(f(Q, K_i))}{\sum_j \exp(f(Q, K_j))}$$

$$\text{Attention}(Q, K, V) = \sum_i a_i V_i$$



# The Cost of Attention

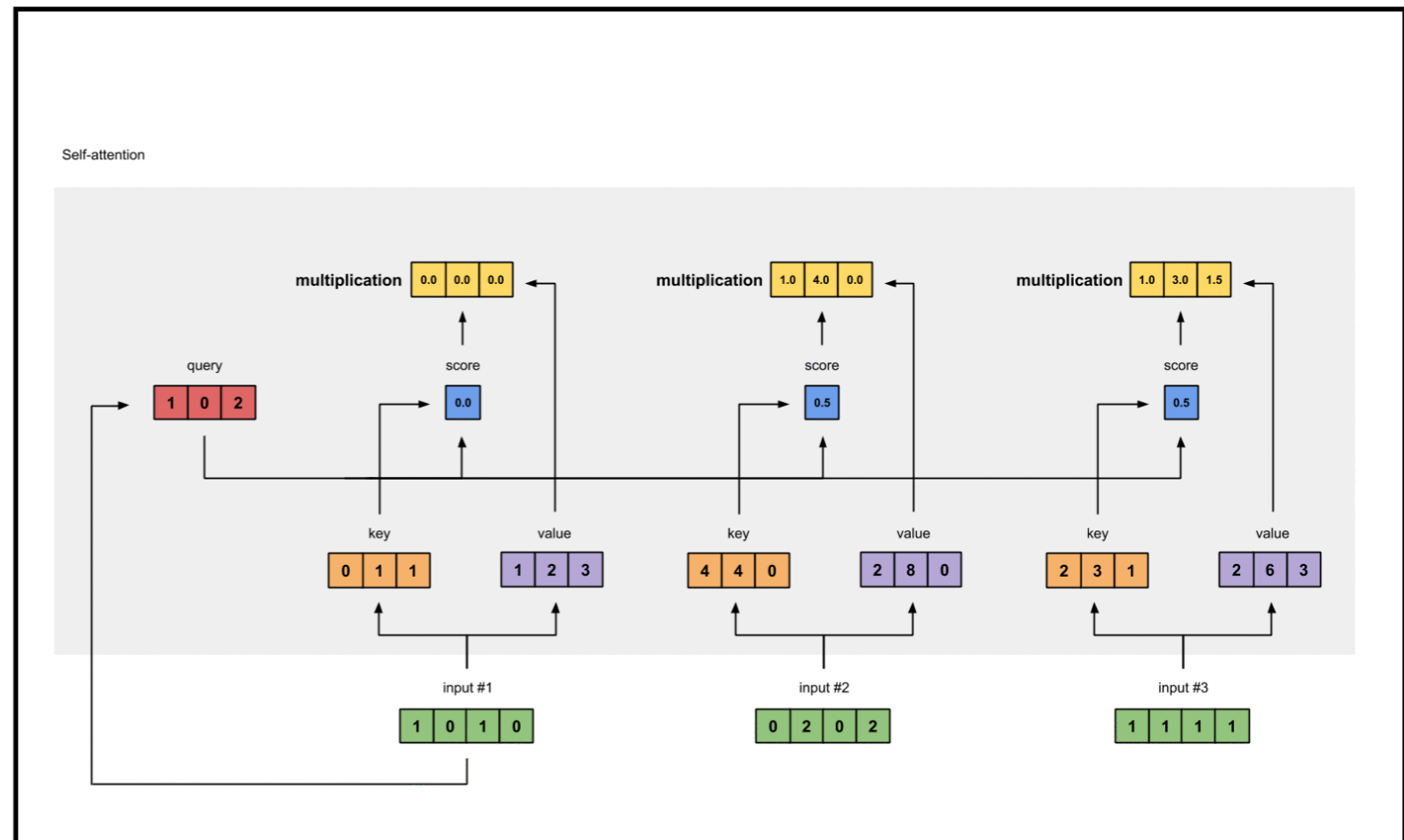
- Human attention is something that's supposed to **save** computational resources. By focusing on one thing, we can neglect many other things.
- However, we need to calculate an attention value for each combination of input and output objects (for long sequences, it could become prohibitively expensive).
- Essentially looks at everything in detail before deciding what to attend to.
- Intuitively that's equivalent outputting a translated word, and then going back through *all* of your internal memory of the text to decide which word to produce next. That seems like a waste, and not at all what humans are doing.
- In fact, it's more akin to memory access (Information Retrieval), not attention.

# Agenda:

- Motivation
- ~~What Is Attention?~~
- ~~How to Compute Attention?~~
- ~~The Cost of Attention~~
- ~~Attention Functions~~
- Attention in NLP:
  - Self Attention
  - Multi-Head Attention
  - Hierarchical Attention
  - Co-Attention
  - Two-Way Attention
  - Key-Value-Predict Attention
- BERT Attention Analysis

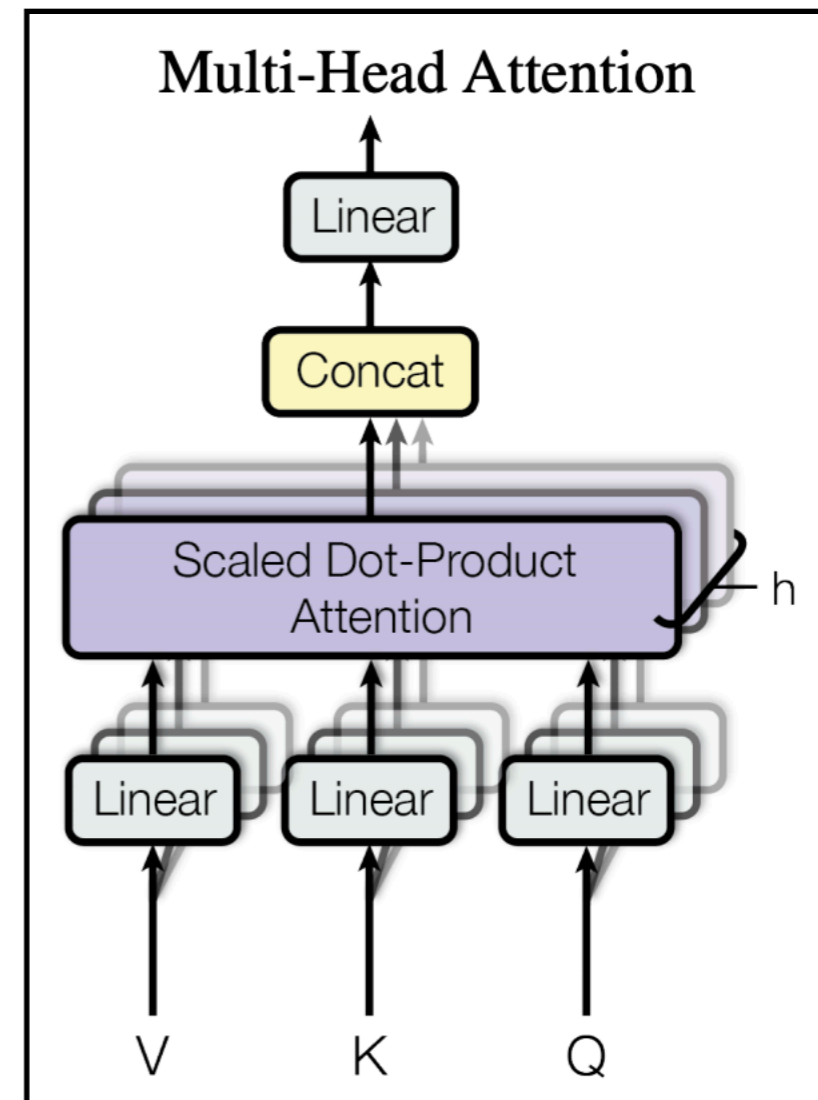
# Self Attention

- Application:  
Representation Learning +  
Machine Translation  
(Transformer, BERT, GPT)
- Intuition: When there is no  
external information  
available, relate different  
positions of the  
same sequence to compute  
its internal representation  
(i.e.  $Q = K = V$ )
- Seems to learn  
sophisticated syntactic  
patterns! (More on that later)



# Multi-Head Attention

- Application:  
Representation Learning  
+ Machine Translation  
(Transformer, BERT, GPT)
- Intuition : The more the merrier! Allow the model to jointly attend to information from different representation subspaces at different positions.



$$\text{MultiHead}(Q, K, V) = \text{Concat}(\text{head}_1, \dots, \text{head}_h)W^O$$

where  $\text{head}_i = \text{Attention}(QW_i^Q, KW_i^K, VW_i^V)$

# Hierarchical Attention

- Application:  
Document Classification
- Intuition: Employ two levels of attention: one at the word level and one at the sentence level, to capture and utilize the hierarchical nature of documents (words  $\rightarrow$  sentences  $\rightarrow$  document)

## Word Level:

$$\begin{aligned}x_{it} &= W_e w_{it}, t \in [1, T], \\ \vec{h}_{it} &= \overrightarrow{\text{GRU}}(x_{it}), t \in [1, T], \\ \overleftarrow{h}_{it} &= \overleftarrow{\text{GRU}}(x_{it}), t \in [T, 1].\end{aligned}$$

1

$$\begin{aligned}u_{it} &= \tanh(W_w h_{it} + b_w) \\ \alpha_{it} &= \frac{\exp(u_{it}^\top u_w)}{\sum_t \exp(u_{it}^\top u_w)} \\ s_i &= \sum_t \alpha_{it} h_{it}.\end{aligned}$$

2

## Sentence Level:

$$\begin{aligned}\vec{h}_i &= \overrightarrow{\text{GRU}}(s_i), i \in [1, L], \\ \overleftarrow{h}_i &= \overleftarrow{\text{GRU}}(s_i), i \in [L, 1].\end{aligned}$$

1

$$\begin{aligned}u_i &= \tanh(W_s h_i + b_s), \\ \alpha_i &= \frac{\exp(u_i^\top u_s)}{\sum_i \exp(u_i^\top u_s)}, \\ v &= \sum_i \alpha_i h_i,\end{aligned}$$

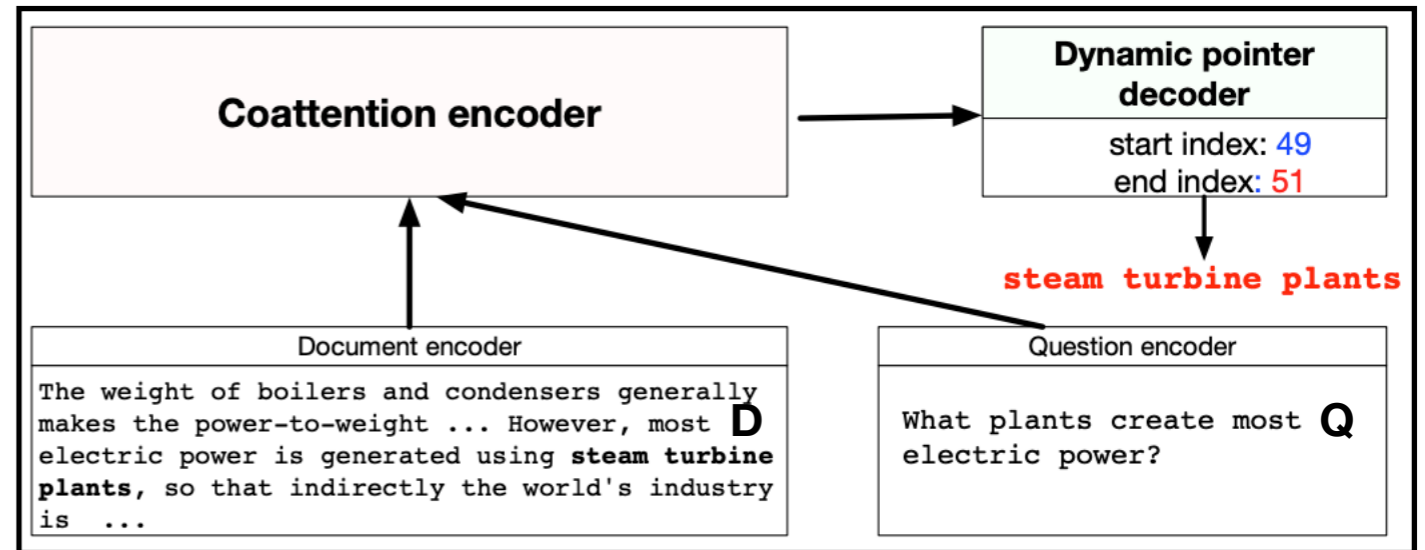
2

## Classification:

$$p = \text{softmax}(W_c v + b_c).$$

# Co-Attention

- Application: Question Answering
- Intuition: Co-attention is computed as an alignment matrix on *all* pairs of document and query words.
- Extra: Use an iterative procedure to select an answer span by alternating between predicting the start point and predicting the end point. This allows for recovering from initial local maxima corresponding to incorrect answer spans.



$$D = [d_1 \dots d_m d_\emptyset]$$

$$Q' = [q_1 \dots q_n q_\emptyset]$$

$$Q = \tanh(W^{(Q)}Q' + b^{(Q)}) \in \mathbb{R}^{\ell \times (n+1)}$$

$$L = D^T Q \in \mathbb{R}^{(m+1) \times (n+1)}$$

$$A^D = \text{softmax}(L^T) \in \mathbb{R}^{(n+1) \times (m+1)}$$

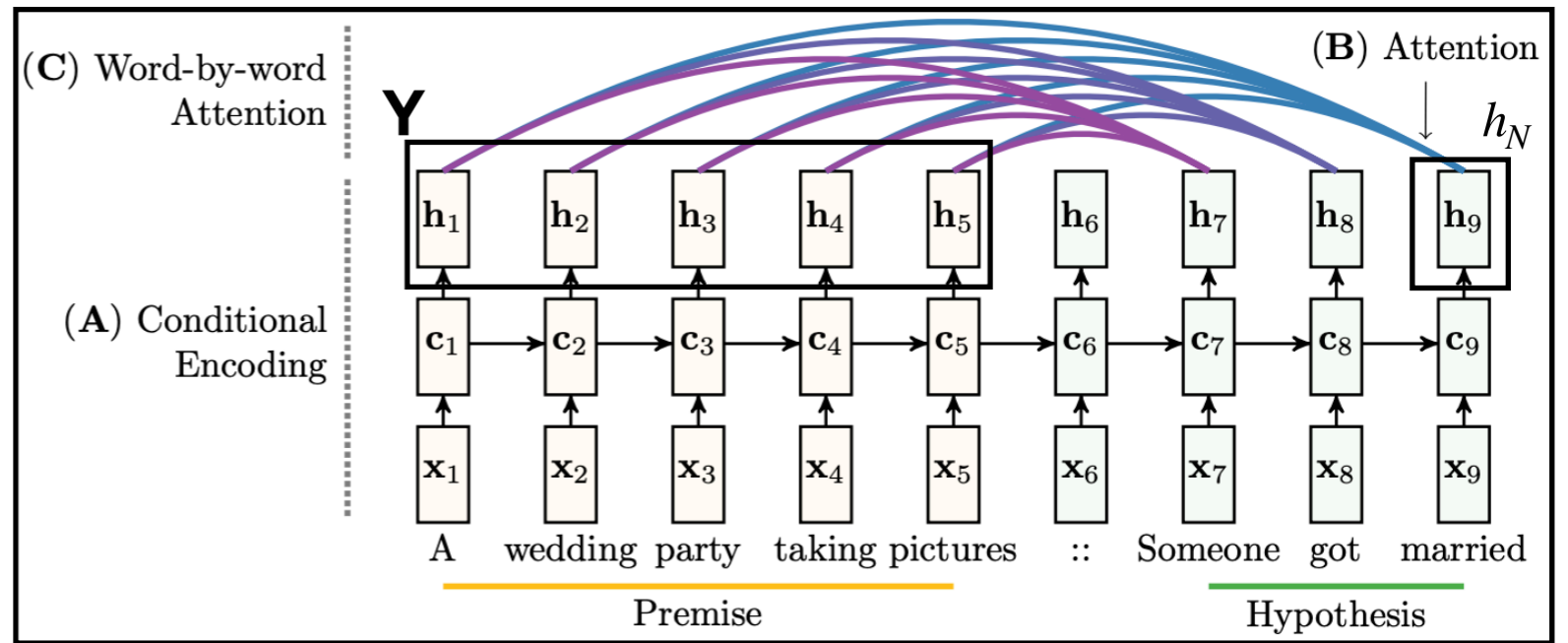
$$A^Q = \text{softmax}(L) \in \mathbb{R}^{(m+1) \times (n+1)}$$

$$C^Q = DA^Q \in \mathbb{R}^{\ell \times (n+1)}$$

$$C^D = [Q; C^Q] A^D \in \mathbb{R}^{2\ell \times (m+1)}$$

# Two-Way Attention

- Application: Textual Entailment
- Intuition: Use the same model to attend over the premise conditioned on the hypothesis, as well as to attend over the hypothesis conditioned on the premise, by simply swapping the two sequences. This produces two sentence-pair representations that we concatenate for classification.



$$\mathbf{M} = \tanh(\mathbf{W}^y \mathbf{Y} + \mathbf{W}^h \mathbf{h}_N \otimes \mathbf{e}_L) \quad \mathbf{M} \in \mathbb{R}^{k \times L}$$

$$\alpha = \text{softmax}(\mathbf{w}^T \mathbf{M}) \quad \alpha \in \mathbb{R}^L$$

$$\mathbf{r} = \mathbf{Y} \alpha^T \quad \mathbf{r} \in \mathbb{R}^k$$

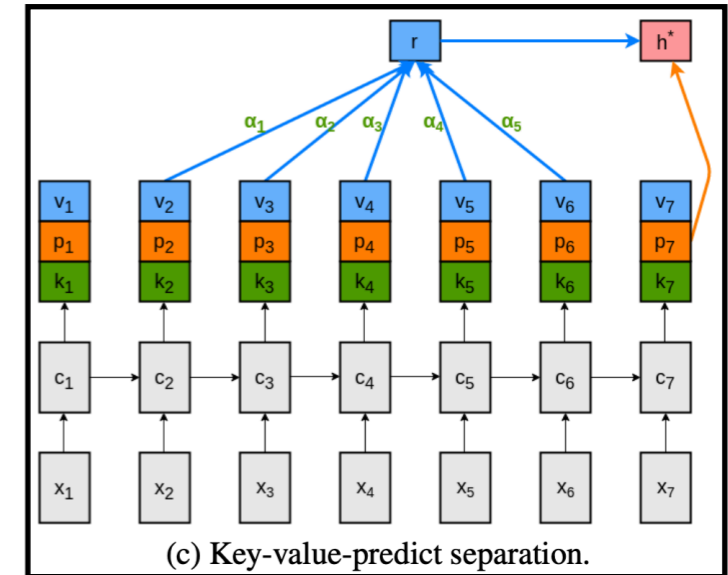
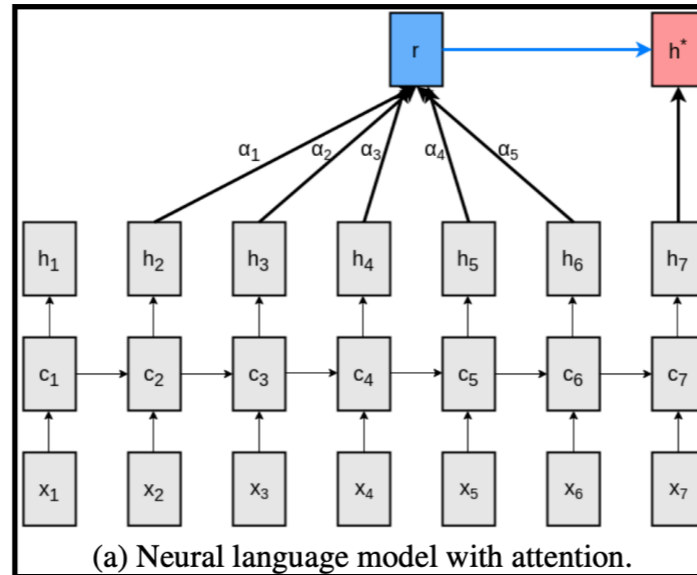
$$\mathbf{M}_t = \tanh(\mathbf{W}^y \mathbf{Y} + (\mathbf{W}^h \mathbf{h}_t + \mathbf{W}^r \mathbf{r}_{t-1}) \otimes \mathbf{e}_L) \quad \mathbf{M}_t \in \mathbb{R}^{k \times L}$$

$$\alpha_t = \text{softmax}(\mathbf{w}^T \mathbf{M}_t) \quad \alpha_t \in \mathbb{R}^L$$

$$\mathbf{r}_t = \mathbf{Y} \alpha_t^T + \tanh(\mathbf{W}^t \mathbf{r}_{t-1}) \quad \mathbf{r}_t \in \mathbb{R}^k$$

# Key-Value-Predict Attention

- Application:  
Language Modelling
- Intuition: Using  $K = V$  for all applications can make training difficult (K=V simultaneously store information for predicting the next word, computing the attention, and encode content relevant to future steps)



$$\begin{bmatrix} k_t \\ v_t \\ p_t \end{bmatrix} = h_t$$

$$\begin{aligned} M_t &= \tanh(\mathbf{W}^Y [k_{t-L} \cdots k_{t-1}] + (\mathbf{W}^h k_t) \mathbf{1}^T) \\ \alpha_t &= \text{softmax}(w^T M_t) \\ r_t &= [v_{t-L} \cdots v_{t-1}] \alpha^T \end{aligned}$$

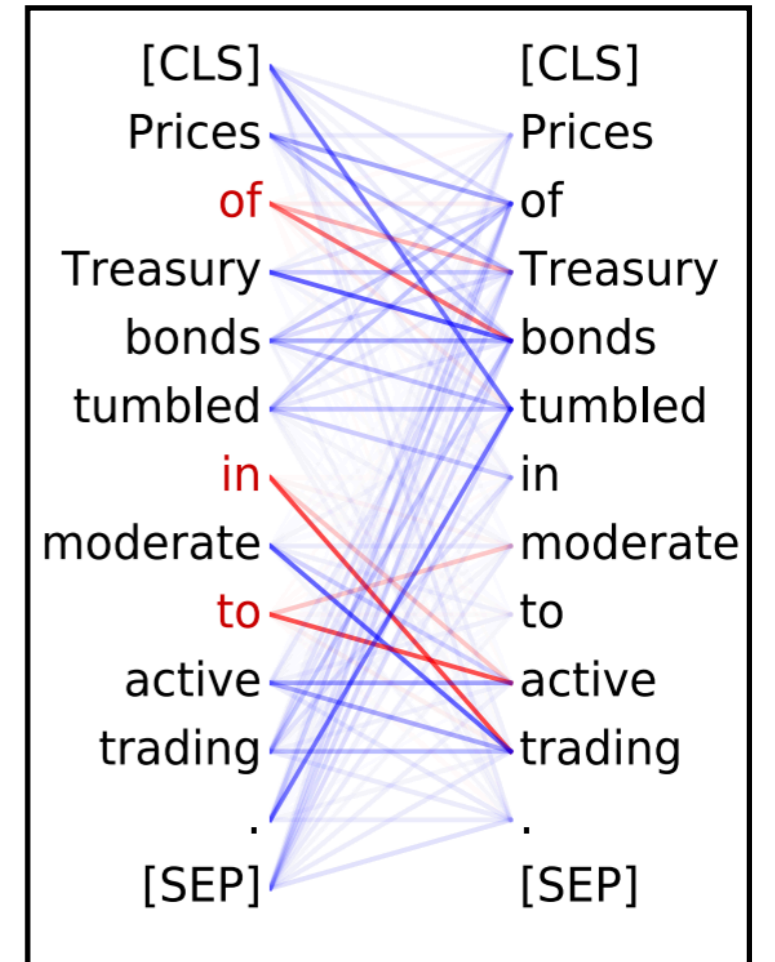
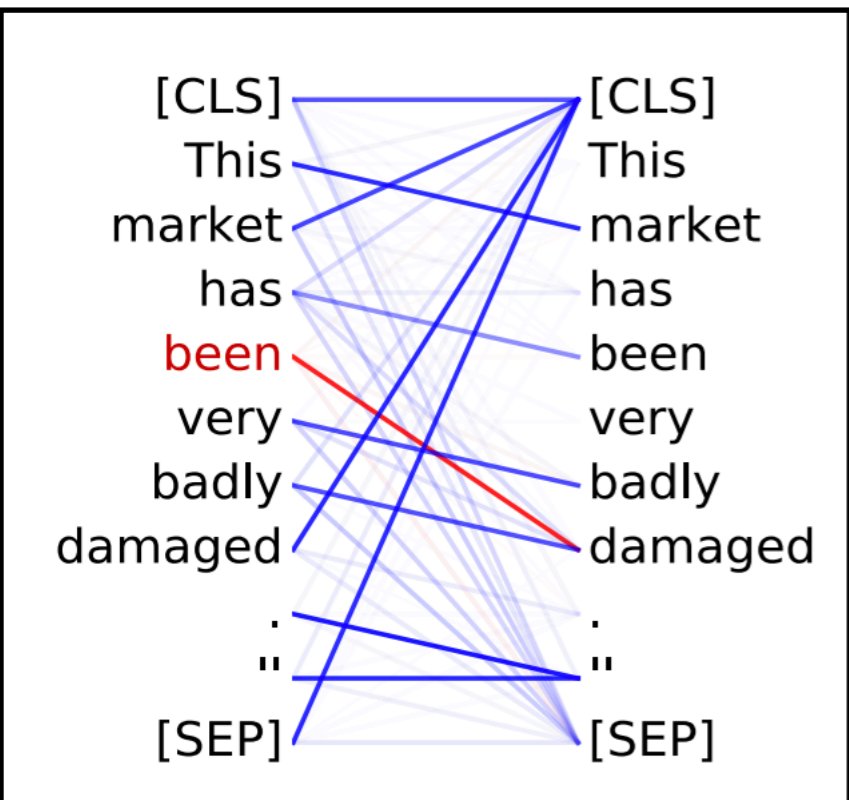
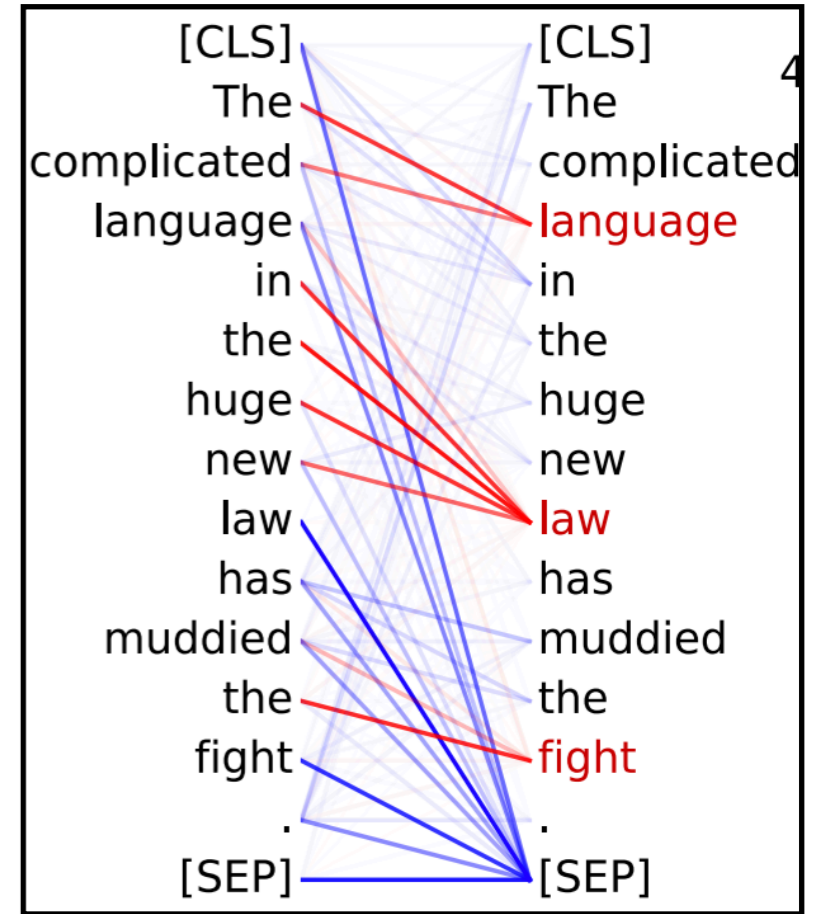
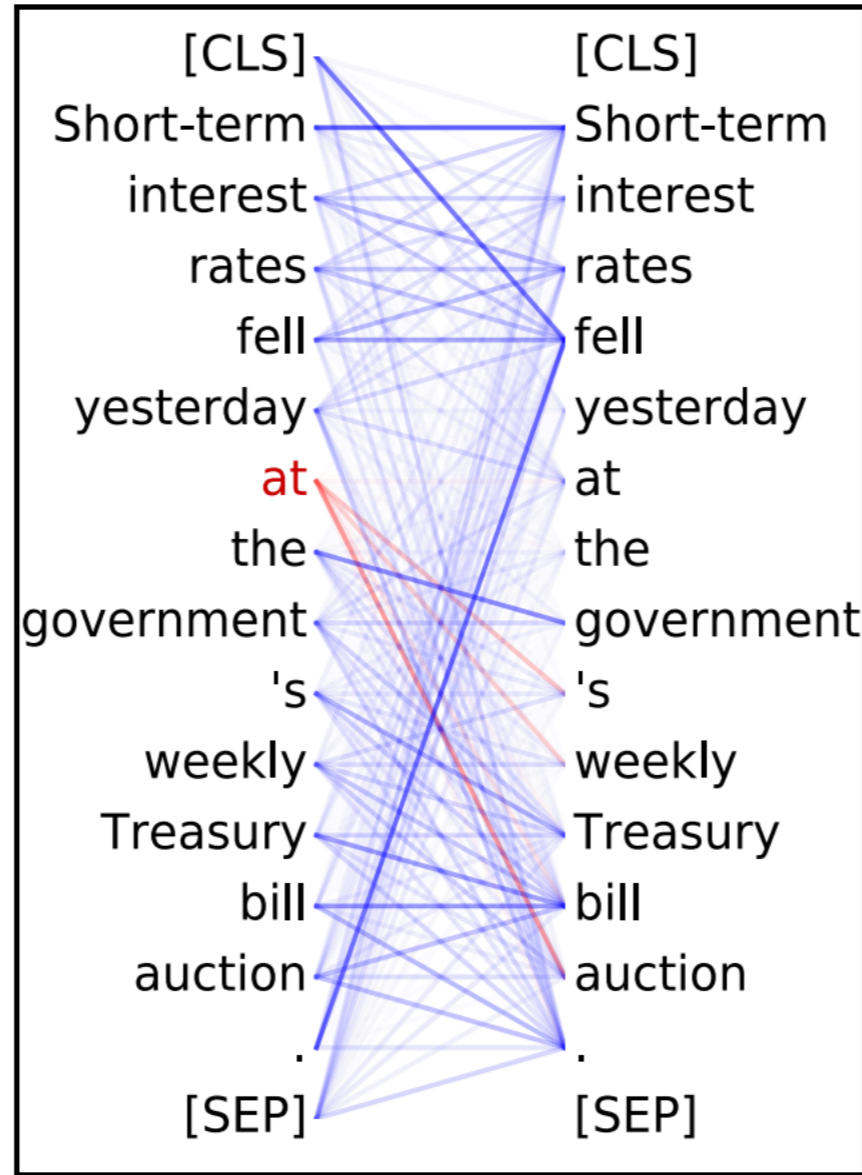
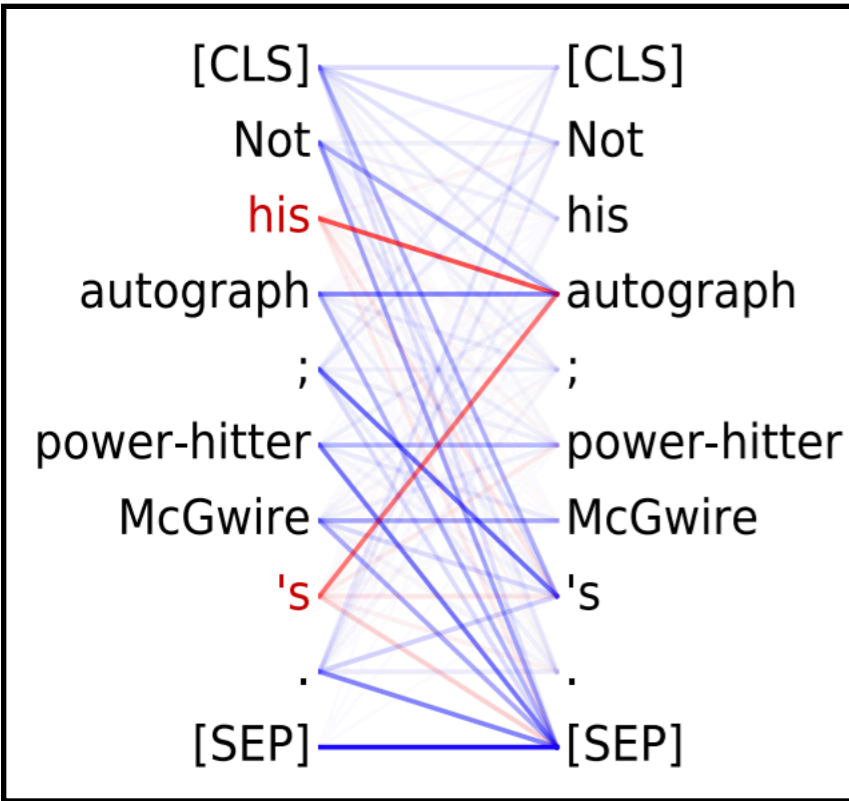
$$h_t^* = \tanh(\mathbf{W}^r r_t + \mathbf{W}^x p_t)$$



# BERT Attention Analysis

- The massive success of pre-trained attention-based models (even though these models are trained in a self-supervised fashion on unlabeled data, without explicit supervision for syntax or coreference) begs the question: What specific linguistic features do they learn?
- Methodology: Collect various statistics (e.g. average entropy, average attention weight per token) and study attention maps of BERT on different datasets.
- Some Findings:
  - Most heads put little attention on the current token. However, there are heads that specialize in attending heavily on the next or previous token, especially in earlier layers of the network.
  - Over half of BERT's attention in layers 6-10 focuses on the delimiter token [SEP], which could be used by the model as a sort of “no-op”.
  - Some attention heads, especially in lower layers, have very broad attention (at most 10% of their attention mass on any single word). The output of these heads is roughly a bag-of-vectors representation of the sentence.
  - Particular heads specialize to specific aspects of syntax. For example, there are heads that find direct objects of verbs, determiners of nouns, objects of prepositions, and objects of possessive pronouns with >75% accuracy.

# Examples:



# References:

- Attention in NLP: <https://medium.com/@joealato/attention-in-nlp-734c6fa9d983>
- Attention Is All You Need: <https://papers.nips.cc/paper/7181-attention-is-all-you-need.pdf>
- Attention and its Different Forms: <https://towardsdatascience.com/attention-and-its-different-forms-7fc3674d14dc>
- What Does BERT Look At? An Analysis of BERT's Attention: <https://arxiv.org/pdf/1906.04341.pdf>
- Visualizing Attention for Seq2Seq models: <https://jalammar.github.io/visualizing-neural-machine-translation-mechanics-of-seq2seq-models-with-attention/>
- Attention and Memory in Deep Learning and NLP: <http://www.wildml.com/2016/01/attention-and-memory-in-deep-learning-and-nlp/>
- An Introductory Survey on Attention Mechanisms in NLP Problems: <https://arxiv.org/pdf/1811.05544.pdf>
- Hierarchical Attention Networks for Document Classification: <http://www.cs.cmu.edu/~./hovv/papers/16HLT-hierarchical-attention-networks.pdf>
- REASONING ABOUT ENTAILMENT WITH NEURAL ATTENTION: <https://arxiv.org/pdf/1509.06664.pdf>
- DYNAMIC COATTENTION NETWORKS FOR QUESTION ANSWERING: <https://arxiv.org/pdf/1611.01604.pdf>
- Neural Machine Translation by Jointly Learning to Align and Translate: <https://arxiv.org/abs/1409.0473>
- FRUSTRATINGLY SHORT ATTENTION SPANS IN NEURAL LANGUAGE MODELING: <https://arxiv.org/pdf/1702.04521.pdf>
- Illustrated: Self-Attention: <https://towardsdatascience.com/illustrated-self-attention-2d627e33b20a>