

CS 489 / 698: Software and Systems Security

Module: Common Vulnerabilities

Lecture: race conditions

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Outline

- 1 Concepts: race condition vs data race
- 2 Introductory examples
- 3 More complex examples
- 4 Atomicity violations
- 5 A formal way to model concurrency
- 6 Other form of races

What is a race condition?

Wikipedia's definition

A race condition is the condition of a software system where the system's substantive behavior is dependent on the sequence or timing of other uncontrollable events, leading to unexpected or inconsistent results.

It becomes a bug when one or more of the possible behaviors is undesirable.

Wikipedia's definition

A *race condition* is the condition of a software system where the system's substantive behavior is dependent on the sequence or timing of other uncontrollable events, leading to unexpected or *inconsistent* results.

It becomes a *bug* when one or more of the possible behaviors is *undesirable*.

What is a data race?

Data race definition in C++ standard

When

- an evaluation of an expression writes to a memory location **and**
- another evaluation reads or modifies *the same memory location*,
the expressions are said to *conflict*.

A program that has two *conflicting evaluations* has a *data race* unless:

- both evaluations execute on *the same thread*, **or**
- both conflicting evaluations are *atomic operations*, **or**
- one of the conflicting evaluations *happens-before* another.

Adapted from [a community-backed C++ reference site](#). For the full version, please refer to the related sections in [C++ working draft](#).

An intuitive definition

Intuitively, a *data race* happens when:

- 1 There are two memory accesses from **different threads**.
- 2 Both accesses target the **same memory location**.
- 3 At least one of them is a **write** operation.

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- 1 There are two memory accesses from **different threads**.
- 2 Both accesses target the **same memory location**.
- 3 At least one of them is a **write** operation.
- 4 Both accesses could **interleave** freely without restrictions such as **synchronization primitives** or **causality relations**.

Test of your understanding

Q: Based on the definition of race condition and data race, what do you think are the relationship between them?

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Introductory case

global var `count` = 0

```
for(i = 0; i < x; i++) {  
    /* do sth critical */  
    .....  
    count++;  
}
```

Thread 1

```
for(i = 0; i < y; i++) {  
    /* do sth critical */  
    .....  
    count++;  
}
```

Thread 2

Q: What is the value of `count` when both threads terminate?

Introductory case

global var `count` = 0

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for(i = 0; i < x; i++) {  
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Thread 1

```
for(i = 0; i < y; i++) {  
    /* do sth critical */  
    .....  
    count++;  
}
```

Thread 2

Q: What is the value of `count` when both threads terminate?

Introductory case

```
global var count = 0  
global var mutex = ⊥
```

```
for(i = 0; i < x; i++) {  
    /* do sth critical */  
    .....  
    lock(mutex);  
    count++;  
    unlock(mutex);  
}
```

Thread 1

```
for(i = 0; i < y; i++) {  
    /* do sth critical */  
    .....  
    lock(mutex);  
    count++;  
    unlock(mutex);  
}
```

Thread 2

Q: What is the value of `count` when both threads terminate?

Race conditions in other settings

Race conditions are not tied to a specific programming language, instead, they are tied to **data sharing in concurrent execution**.

Race conditions in other settings

Race conditions are not tied to a specific programming language, instead, they are tied to **data sharing in concurrent execution**.

For example, in the database context:

Q: If two database clients send the following requests concurrently, what will be the result (both try to withdraw \$100 from Alice)?

Client 1

```
SELECT @balance = Balance
  FROM Ledger WHERE Name = "Alice";

UPDATE Ledger SET Balance =
  @balance - 100 WHERE Name = "Alice";
```

Client 2

```
SELECT @balance = Balance
  FROM Ledger WHERE Name = "Alice";

UPDATE Ledger SET Balance =
  @balance - 100 WHERE Name = "Alice";
```


Race conditions in a database setting

One possible interleaving (that messes up the states)

```
SELECT @balance = Balance FROM Ledger WHERE Name = "Alice";
SELECT @balance = Balance FROM Ledger WHERE Name = "Alice";
UPDATE Ledger SET Balance = @balance - 100 WHERE Name = "Alice";
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```

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Q: How to prevent the race condition in this case?

Race conditions in a database setting

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SELECT @balance = Balance FROM Ledger WHERE Name = "Alice";
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UPDATE Ledger SET Balance = @balance - 100 WHERE Name = "Alice";
```

Q: How to prevent the race condition in this case?

Interleavings with transactions

```
BEGIN TRANSACTION;
  SELECT @balance = Balance FROM Ledger WHERE Name = "Alice";
  UPDATE Ledger SET Balance = @balance - 100 WHERE Name = "Alice";
COMMIT TRANSACTION;
BEGIN TRANSACTION;
  SELECT @balance = Balance FROM Ledger WHERE Name = "Alice";
  UPDATE Ledger SET Balance = @balance - 100 WHERE Name = "Alice";
COMMIT TRANSACTION;
```

Revisit the example

global var **count** = 0

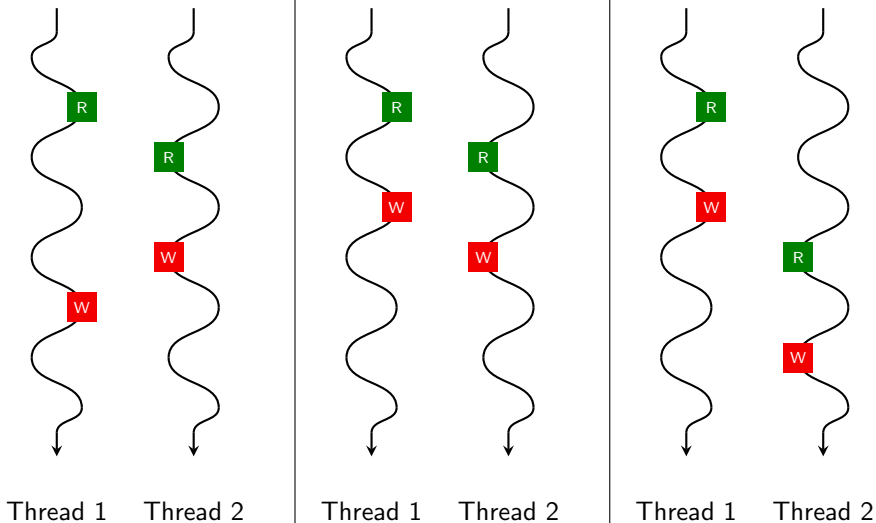
```
for(i = 0; i < x; i++) {  
    count++;  
}
```

Thread 1

```
for(i = 0; i < y; i++) {  
    count++;  
}
```

Thread 2

Free interleavings without locking



Revisit the example

global var `count` = 0

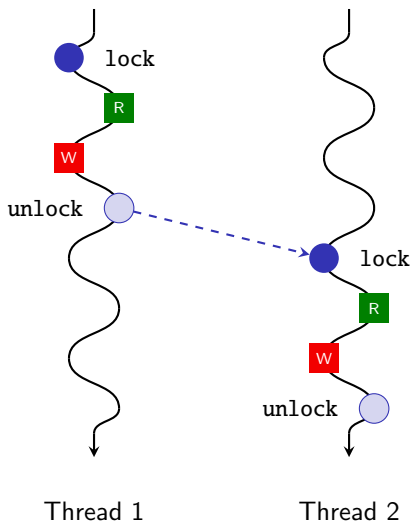
```
for(i = 0; i < x; i++) {  
    lock(mutex);  
    count++;  
    unlock(mutex);  
}
```

Thread 1

```
for(i = 0; i < y; i++) {  
    lock(mutex);  
    count++;  
    unlock(mutex);  
}
```

Thread 2

Limited interleavings with locking



Revisiting the definition

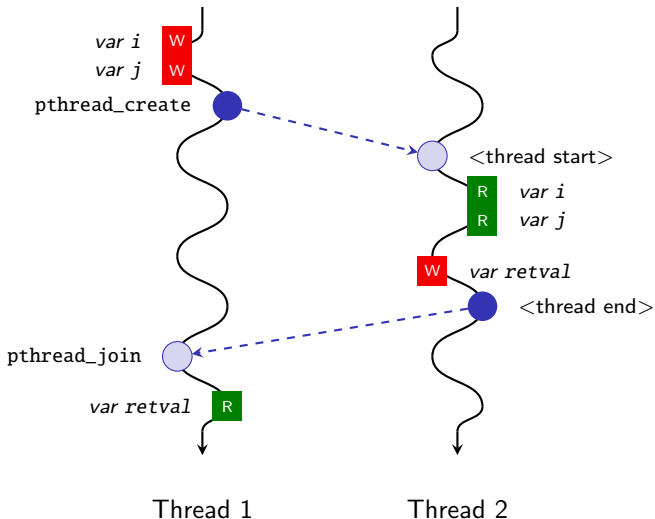
Intuitively, a *data race* happens when:

- 1 There are two memory accesses from **different threads**.
- 2 Both accesses target the **same memory location**.
- 3 At least one of them is a **write** operation.
- 4 Both accesses could **interleave** freely without restrictions such as **synchronization primitives** ~~or **causality relations**~~.

Causality relations: an example

```
1 #include <stdio.h>
2 #include <pthread.h>
3
4 int i;
5 int retval;
6
7 void* foo(void* p){
8     printf("Value of i: %d\n", i);
9     printf("Value of j: %d\n", *(int *)p);
10    pthread_exit(&retval);
11 }
12
13 int main(void){
14     int i = 1;
15     int j = 2;
16
17     pthread_t id;
18     pthread_create(&id, NULL, foo, &j);
19     pthread_join(id, NULL);
20
21     printf("Return value from thread: %d\n", retval);
22 }
```

Causality relations



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Revisiting the definition

If we can find, statically or dynamically, a pair of memory access instructions (A_1, A_2) such that

- they originate from **different threads**,
- both A_1 and A_2 target the **same memory location**, **AND**
- at least one of them is a **write** operation,

then we conclude that (A_1, A_2) must be one of the following cases:

- 1 A_1 **strictly happens before** A_2 or vice versa due to causality, **OR**
- 2 A_1 and A_2 can only occur when **a common lock** is held, **OR**
- 3 (A_1, A_2) is a **data race**.

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If we can find, statically or dynamically, a pair of memory access instructions (A_1, A_2) such that

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- 2 A_1 and A_2 can only occur when **a common lock** is held, **OR**
- 3 (A_1, A_2) is a **data race**.

Q: Wait... how are locks implemented?

Common synchronization primitives

Common synchronization primitives

- Lock / Mutex / Critical section
- Read-write lock
- Barrier
- Semaphore

How are synchronization primitives implemented?

- Hardware support
 - Atomic swap
 - Atomic read-modify-write
 - * compare-and-swap
 - * test-and-set
 - * fetch-and-add
 - *

How are synchronization primitives implemented?

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 - Atomic swap
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 - * compare-and-swap
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 - * fetch-and-add
 - *

- Software algorithms
 - Dekker's algorithm

Spinlock with atomic swap (xchg)

```
1 locked: ; The lock variable. 1 = locked, 0 = unlocked.
2     dd     0
3
4 spin_lock:
5     mov    eax, 1 ; Set the EAX register to 1.
6     xchg   eax, [locked] ; Atomically swap the EAX register with
7                       ; the lock variable.
8                       ; This will always store 1 to the lock, leaving
9                       ; the previous value in the EAX register.
0     test   eax, eax ; Test EAX with itself. Among other things, this
1                       ; will set the processor's Zero Flag if EAX is 0.
2                       ; If EAX is 0, then the lock was unlocked and
3                       ; we just locked it.
4                       ; Otherwise, EAX is 1 and we didn't acquire the lock.
5     jnz    spin_lock ; Jump back to the MOV instruction if the Zero Flag is
6                       ; not set; the lock was previously locked, and so
7                       ; we need to spin until it becomes unlocked.
8     ret    ; The lock has been acquired, return to the caller.
9
0 spin_unlock:
1     xor    eax, eax ; Set the EAX register to 0.
2     xchg   eax, [locked] ; Atomically swap the EAX register with
3                       ; the lock variable.
4     ret    ; The lock has been released.
```

Spinlock with atomic swap (xchg)

Q: Are there data races or race conditions in spinlock implementation?

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Q: Are there data races or race conditions in spinlock implementation?

A: By looking at the code

- Data race: Yes, but hardware guarantees atomicity
- Race condition: No

Dekker's algorithm

```
1 bool wants_to_enter[2] = {false, false};  
2 int turn = 0; /* or turn = 1 */
```

```
1 // lock  
2 wants_to_enter[0] = true;  
3 while (wants_to_enter[1]) {  
4     if (turn != 0) {  
5         wants_to_enter[0] = false;  
6         // busy wait  
7         while (turn != 0) {}  
8         wants_to_enter[0] = true;  
9     }  
10 }  
11  
12 /* ... critical section ... */  
13  
14 // unlock  
15 turn = 1;  
16 wants_to_enter[0] = false;
```

Thread 1

```
1 // lock  
2 wants_to_enter[1] = true;  
3 while (wants_to_enter[0]) {  
4     if (turn != 1) {  
5         wants_to_enter[1] = false;  
6         // busy wait  
7         while (turn != 1) {}  
8         wants_to_enter[1] = true;  
9     }  
10 }  
11  
12 /* ... critical section ... */  
13  
14 // unlock  
15 turn = 0;  
16 wants_to_enter[1] = false;
```

Thread 2

Dekker's algorithm

Q: Are there data races or race conditions in Dekker's algorithm?

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Q: Are there data races or race conditions in Dekker's algorithm?

A: By looking at the code

- Data race: Yes, but hardware guarantees atomicity
- Race condition: No

Is this a data race or a race condition or neither?

```
1 int x = 0;
2 bool flag = false;
3 lock mutex = unlocked;
```

```
1 x++;
2 lock(mutex);
3 flag = true;
4 unlock(mutex);
```

Thread 1

```
1 while(true) {
2     lock(mutex);
3     if (flag) {
4         unlock(mutex);
5         break;
6     }
7     unlock(mutex);
8 }
9 x--;
```

Thread 2

Is this a data race or a race condition or neither?

```
1 int x = 0;  
2 bool flag = false;
```

```
1 x++;  
2 flag = true;
```

Thread 1

```
1 while (!flag) {};  
2 x--;
```

Thread 2

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Revisit the example

global var `count` = 0

```
for(i = 0; i < x; i++) {  
    lock(mutex);  
    t = count;  
    unlock(mutex);  
  
    t++;  
  
    lock(mutex);  
    count = t;  
    unlock(mutex);  
}
```

Thread 1

```
for(i = 0; i < y; i++) {  
    lock(mutex);  
    t = count;  
    unlock(mutex);  
  
    t++;  
  
    lock(mutex);  
    count = t;  
    unlock(mutex);  
}
```

Thread 2

Revisit the example

Q: In this modified example, is there a data race?

Revisit the example

Q: In this modified example, is there a data race?

A: No

Revisit the example

Q: In this modified example, is there a data race?

A: No

Q: But the results are the same with all locks removed?

global var `count` = 0

```
for(i = 0; i < x; i++) {  
    t = count;  
    t++;  
    count = t;  
}
```

```
for(i = 0; i < y; i++) {  
    t = count;  
    t++;  
    count = t;  
}
```

Revisit the example

Q: In this modified example, is there a data race?

A: No

Q: But the results are the same with all locks removed?

global var **count** = 0

```
for(i = 0; i < x; i++) {  
    t = count;  
    t++;  
    count = t;  
}
```

```
for(i = 0; i < y; i++) {  
    t = count;  
    t++;  
    count = t;  
}
```

A: No, depending on how hardware works (e.g., per-bit conflict)

Extract the commonalities of the two variants

Q: What is common in developers' expectations in the two variants?

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A: States do not change **for a critical section** during execution.

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Q: What is common in developers' expectations in the two variants?

A: States do not change **for a critical section** during execution.

A: Generalization: states remain **integral for a critical section** during execution. No change of states is just one way of remaining integral (assuming state is integral before the critical section).

State integrity example

```
1 struct R { x: int, y: int } g;  
2 [invariant] g.x + g.y == 100;
```

```
1 int add_x(v: int) {  
2   g.x += v;  
3   g.y -= v;  
4 }
```

Thread 1

```
1 int add_y(v: int) {  
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Thread 2

State integrity example

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1 struct R { x: int, y: int } g;  
2 [invariant] g.x + g.y == 100;  
3 lock mutex = unlocked;
```

```
1 int add_x(v: int) {  
2   lock(mutex);  
3   g.x += v;  
4   unlock(mutex);  
5   lock(mutex);  
6   g.y -= v;  
7   unlock(mutex);  
8 }
```

Thread 1

```
1 int add_y(v: int) {  
2   lock(mutex);  
3   g.y += v;  
4   unlock(mutex);  
5   lock(mutex);  
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7   unlock(mutex);  
8 }
```

Thread 2

Q: Is this the right way of adding locks?

State integrity example

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Thread 1

```
1 int add_y(v: int) {  
2   lock(mutex);  
3   g.y += v;  
4   unlock(mutex);  
5   lock(mutex);  
6   g.x -= v;  
7   unlock(mutex);  
8 }
```

Thread 2

Q: Is this the right way of adding locks?

A: No, as the invariant is not guaranteed

State integrity example

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1 struct R { x: int, y: int } g;  
2 [invariant] g.x + g.y == 100;  
3 lock mutex = unlocked;
```

```
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Thread 1

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Thread 2

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6 }
```

Thread 1

```
1 int add_y(v: int) {  
2   lock(mutex);  
3   g.y += v;  
4   g.x -= v;  
5   unlock(mutex);  
6 }
```

Thread 2

Q: Is this the right way of adding locks?

A: Yes, the invariant is guaranteed at each entry and exit of the critical section in both threads

State integrity is hard to capture

However, in practice, the invariant often exists in

- some architectural design documents (which no one reads)
- code comments in a different file (which no one notices)
- folklore knowledge among the dev team
- the mind of the developer who has resigned a few years ago...

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How to model concurrency mathematically?

How to model concurrency mathematically?

- Lamport clock
- Vector clock

Lamport clock algorithm

Each thread has its own clock variable t

- On initialization:
 - $t \leftarrow 0$
- On write to shared memory $*ptr = val$:
 - $t \leftarrow t + 1$
 - store t alongside val at memory location ptr
- On read from shared memory $val = *ptr$:
 - retrieve the stored clock t' at memory location ptr
 - $t \leftarrow \max(t, t') + 1$

Lamport clock algorithm

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- On read from shared memory $val = *ptr$:
 - retrieve the stored clock t' at memory location ptr
 - $t \leftarrow \max(t, t') + 1$

Properties of Lamport clock:

- $a \rightarrow b \implies L(a) < L(b)$
- $L(a) < L(b) \not\implies a \rightarrow b$

Vector clock algorithm

Each thread i has its own clock vector t

- On initialization:
 - $T \leftarrow \langle 0, 0, \dots, 0 \rangle_N$, assuming N threads
- On write to shared memory $*ptr = val$:
 - $T[i] \leftarrow T[i] + 1$
 - store T alongside val at memory location ptr
- On read from shared memory $val = *ptr$:
 - retrieve the stored clock T' at memory location ptr
 - $\forall k \in [0, N) : T[k] = \max(T[k], T'[k])$
 - $T[i] \leftarrow T[i] + 1$

Properties of the vector clock algorithm

With the following definition on the timestamp ordering:

- $T = T' \iff \forall i \in [0, N) : T[i] = T'[i]$
- $T \leq T' \iff \forall i \in [0, N) : T[i] \leq T'[i]$
- $T < T' \iff T \leq T' \wedge T \neq T'$
- $T \parallel T' \iff T \not\leq T' \wedge T' \not\leq T$

We have:

- $a \rightarrow b \iff V(a) < V(b)$
- $a = b \iff V(a) = V(b)$
- $a \parallel b \iff V(a) \parallel V(b)$

Practice exercise (vector clock)

```
1 int x = 0;  
2 atomic_bool flag = false;
```

```
1 x++;  
2 flag = true;
```

Thread 1

```
1 while (!flag) {};  
2 x--;
```

Thread 2

Prove: the write of `x` at `x--` in thread 2 can **never happen before** the read of `x` in `x++` in thread 1.

Practice exercise (vector clock)

```
1 int x = 0;  
2 bool r = false;
```

```
1 v = load(&x);  
2 store(&x, v + 1);  
3 store(&r, true);
```

Thread 1

```
1 loop:  
2   c = load(&r);  
3   jump_if_false(c, loop);  
4   v = load(&x);  
5   store(&x, v - 1);
```

Thread 2

Prove: line 5 at thread 2 can **never happen before** line 1 at thread 1.

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A more abstract view of race conditions

Q: Why do race conditions happen in the first place?

A more abstract view of race conditions

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A: Because two threads in the same process **share memory**

A more abstract view of race conditions

Q: Why do race conditions happen in the first place?

A: Because two threads in the same process **share memory**

We can further generalize this concept by asking:

Q: What else do they share?

Q: What about other entities that may run concurrently?

Example: race over the filesystem

```
1 #include <...>
2
3 int main(int argc, char *argv[]) {
4     FILE *fd;
5     struct stat buf;
6
7     if (stat("/some_file", &buf)) {
8         exit(1); // cannot read stat message
9     }
10
11    if (buf.st_uid != getuid()) {
12        exit(2); // permission denied
13    }
14
15    fd = fopen("/some_file", "wb+");
16    if (fd == NULL) {
17        exit(3); // unable to open the file
18    }
19
20    fprintf(f, "<some-secret-value>");
21    fclose(fd);
22    return 0;
23 }
```

Example: the Dirty COW exploit

CVE-2016-5195

Allows local privilege escalation: `user(1000) → root(0)`.

Existed in the kernel for nine years before finally patched.

Details on the [Website](#).

⟨ **End** ⟩