Introduction to Artificial Intelligence

Search

CS 486/686

University of Waterloo

Introduction

Search was one of the first topics studied in AI

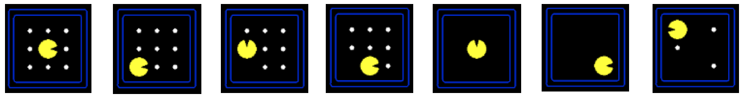
- Newell and Simon (1961) *General Problem Solver*

Central component to many AI systems

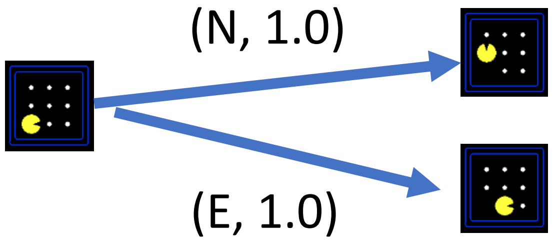
- Automated reasoning, theorem proving, robot navigation, scheduling, game playing, machine learning...

Search Problems

- A **search problem** consists of
  - a state space

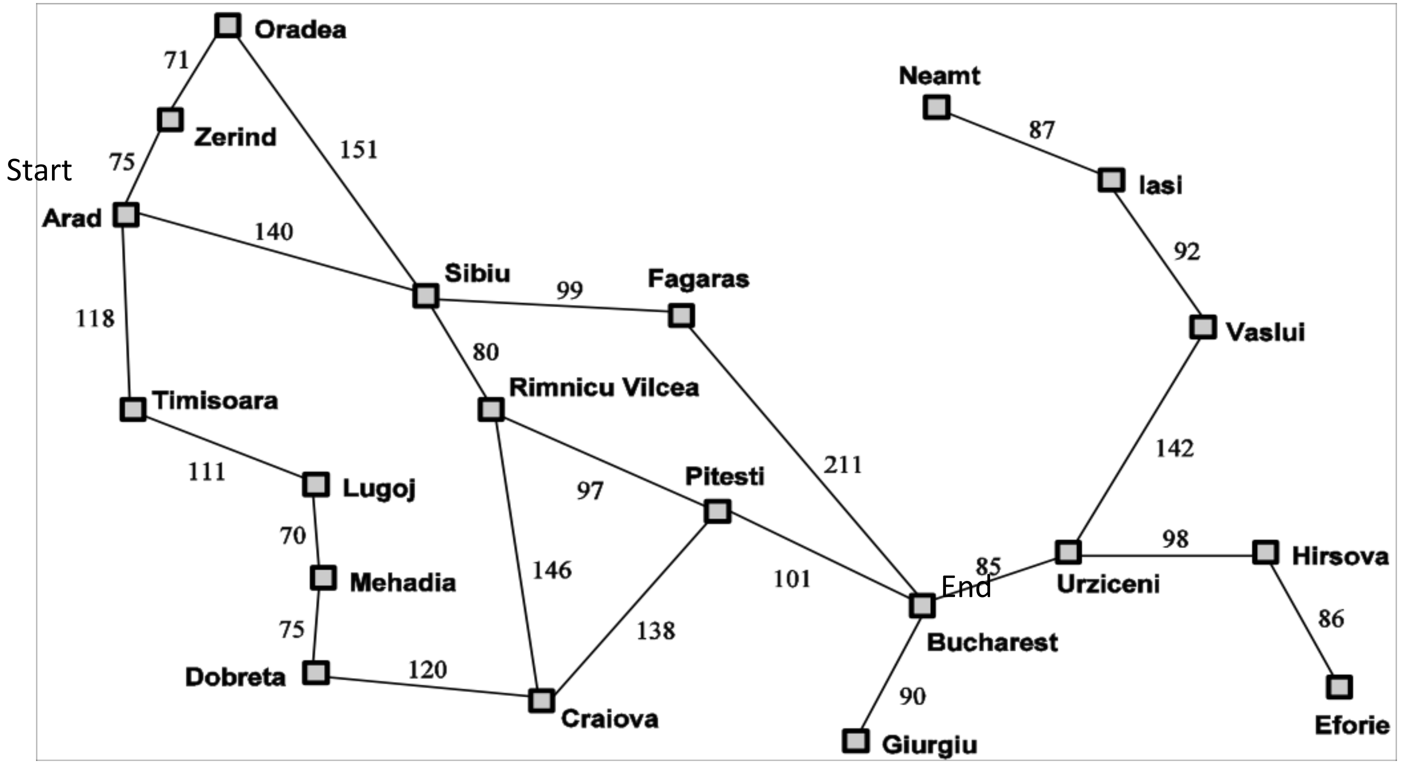


  - a successor function (actions, cost)



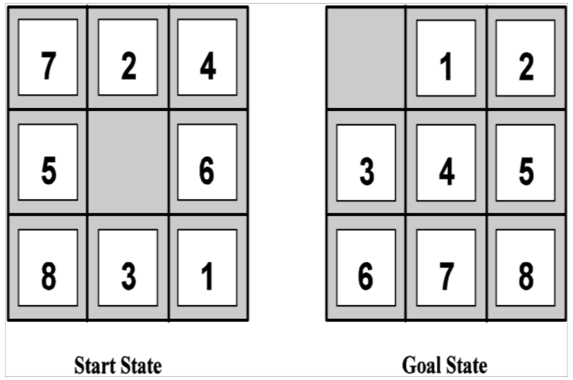
  - a start state and a goal test
- A **solution** is a sequence of actions (plan) from the start state to a goal state

Example: Traveling in Romania



- States:
- Initial State:
- Successor Function:
- Goal test:
- Solution:

Examples of Search Problems



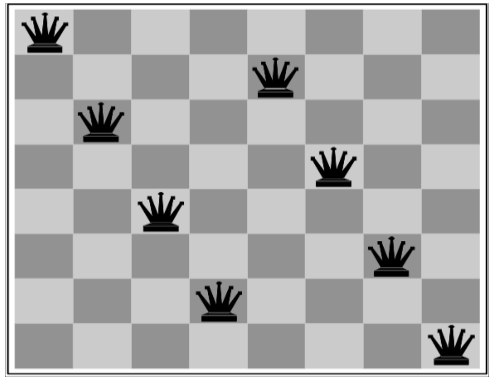
States:

Initial State:

Successor Function:

Goal test:

Solution:



States:

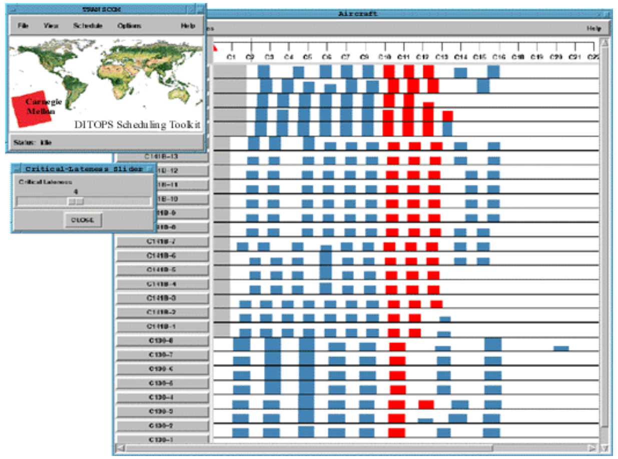
Initial State:

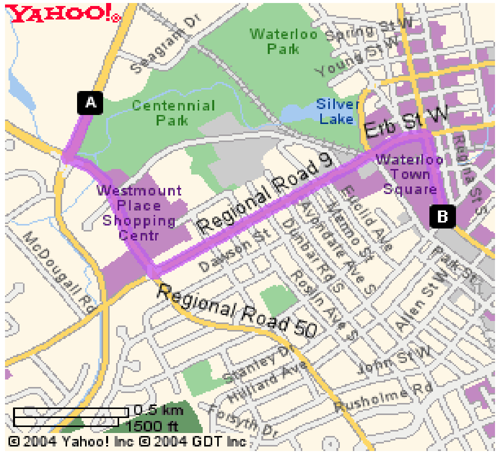
Successor Function:

Goal test:

Solution:

Examples of Search Problems





Our Definition Excludes...

Chance

Adversaries

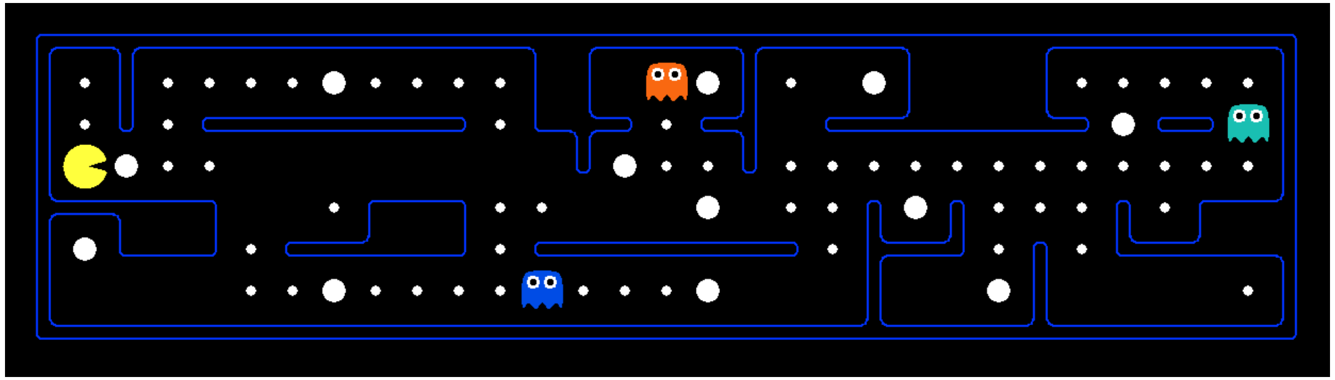
Continuous states

Partial Observability

All of the above

What is is a state space?

The **world state** includes every last detail of the environment



A **search state** keeps only the details needed for planning (abstraction)

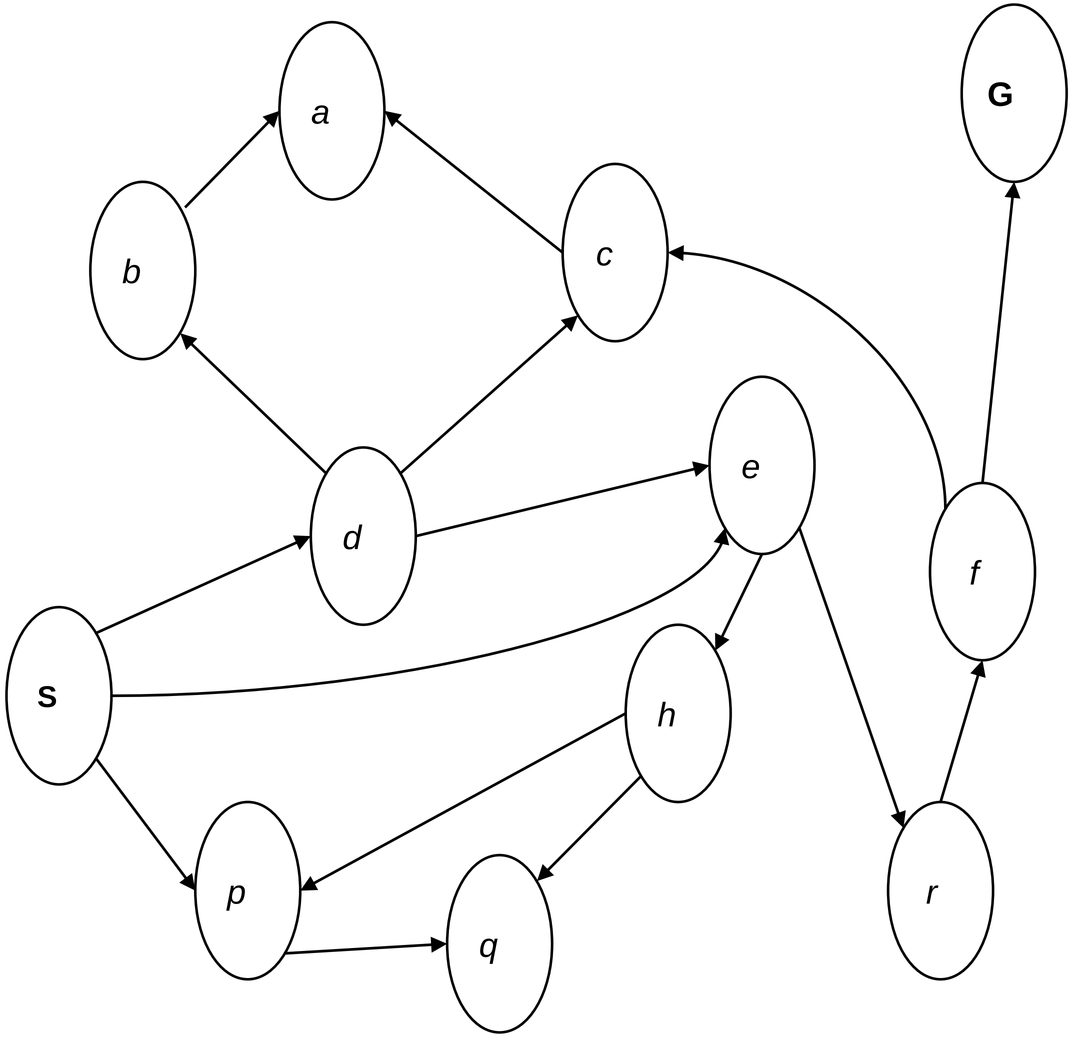
- Problem: Pathing
  - States: (x,y) location
  - Actions: NSEW
  - Successor: update location only
  - Goal test: is (x,y)=END

- Problem: Eat-All-Dots
  - States: {(x,y), dot booleans}
  - Actions: NSEW
  - Successor: update location and possibly a dot boolean
  - Goal test: dots all false

Adapted from UC Berkeley's CS188 Course

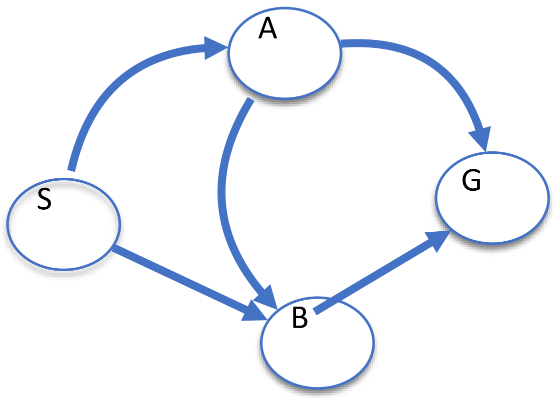
Representing Search

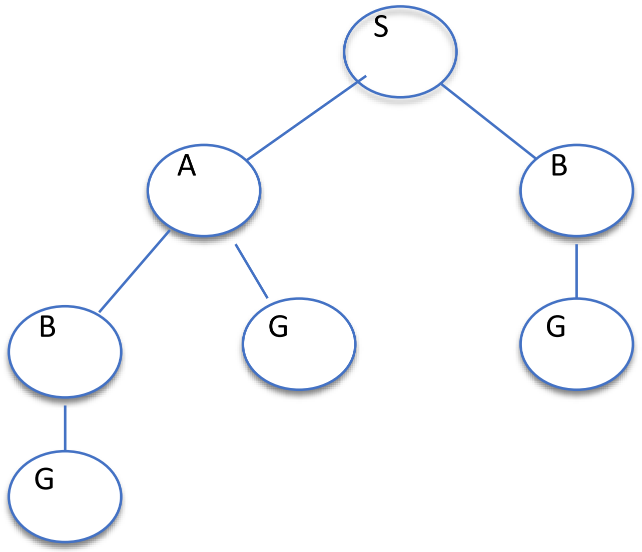
- **State space graph**
  - Vertices correspond to states (one vertex for each state)
  - Edges correspond to successors
  - Goal test is a set of goal nodes
- We search for a solution by building **a search tree** and traversing it to find a goal state



Search Tree

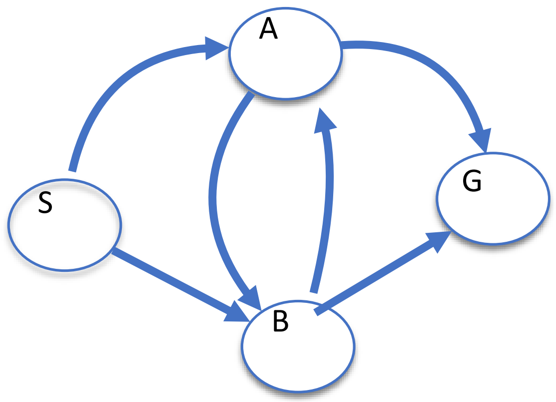
- **A search tree**:
  - Start state is the root of the tree
  - Children are successors
  - A plan is a path in the tree. A solution is a path from the root to a goal node.
  - For most problems we do not actually generate the entire tree





Quiz

- Given this state graph, how large is the search tree?



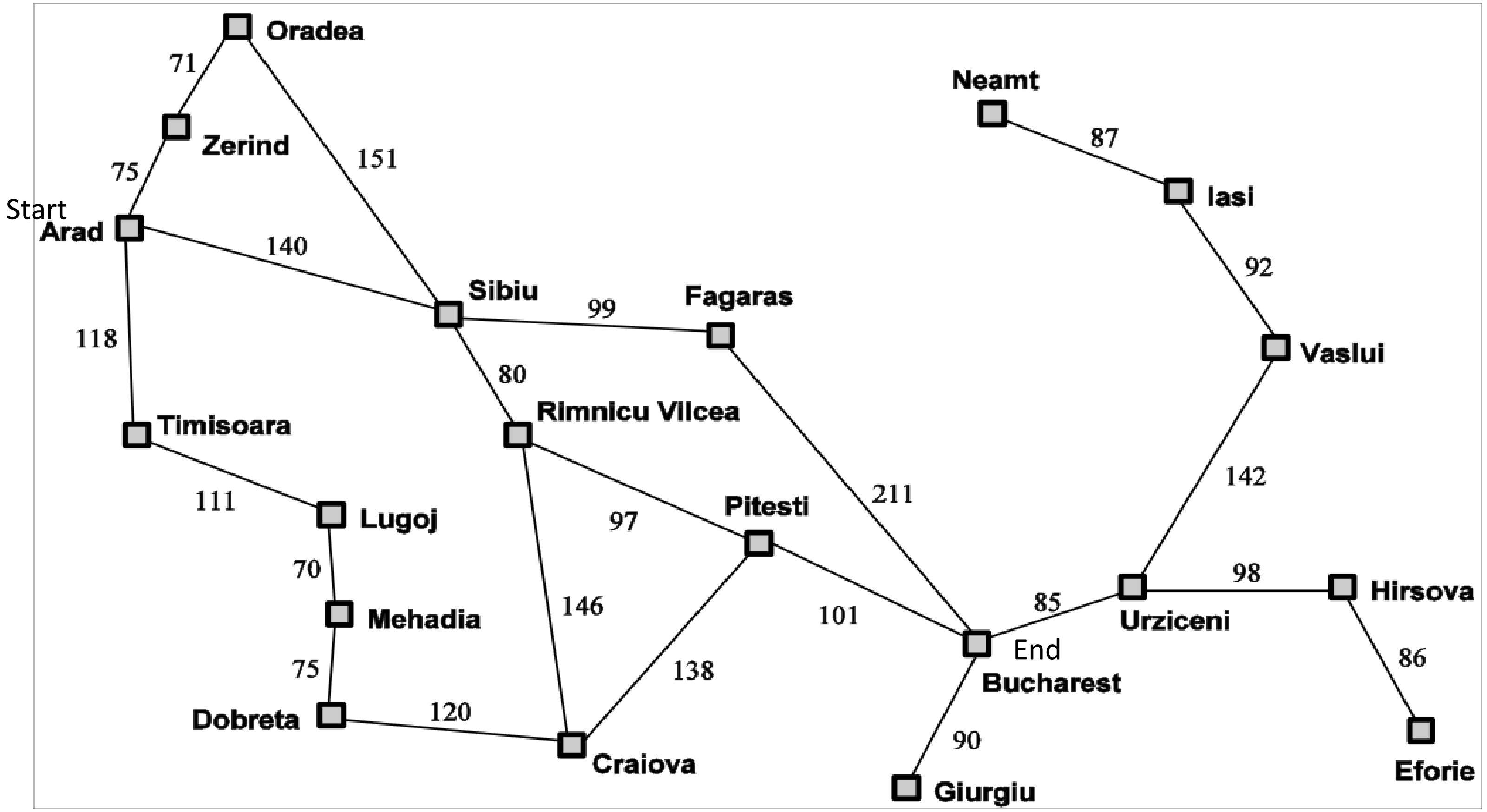
Expanding Nodes

Expanding a node:

Applying all legal operators to the state contained in the node

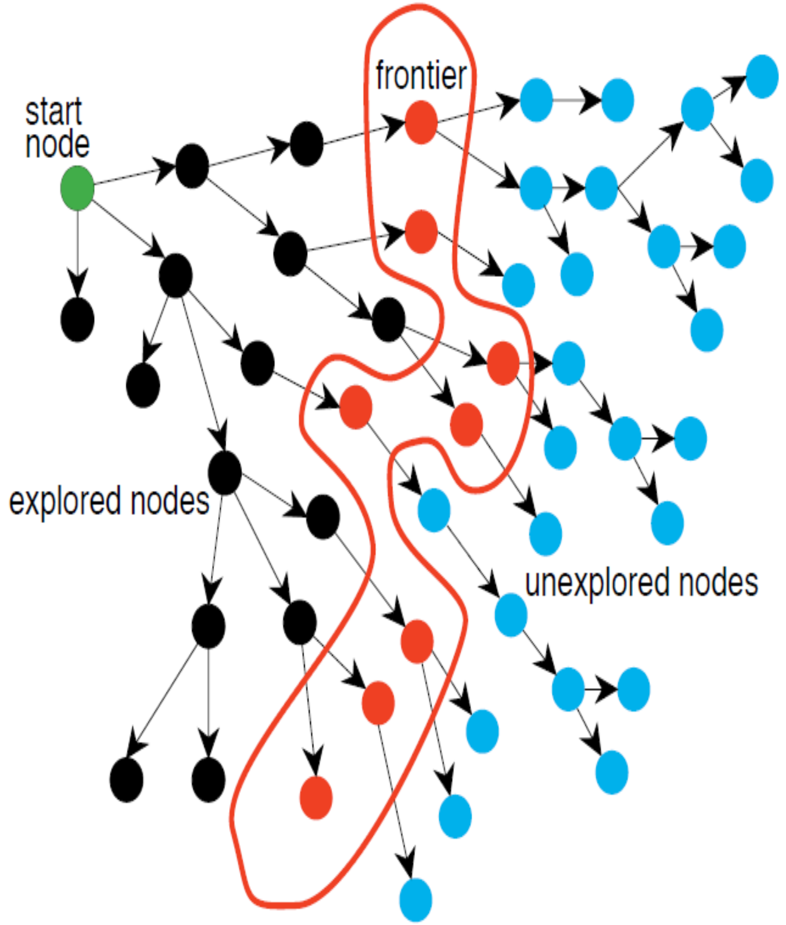
Generating nodes for all corresponding successor states

Example: Traveling in Romania



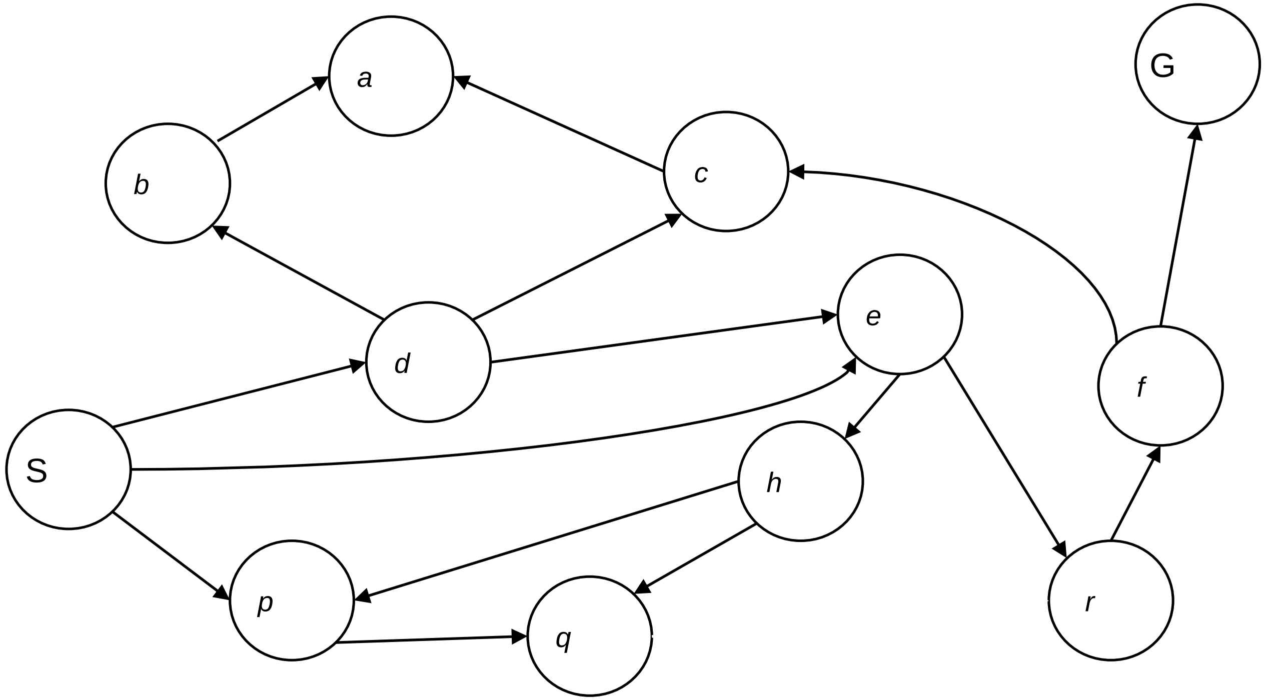
Generic Search Algorithm

- Initialize with initial state of the problem
- Repeat
  - If no candidate nodes can be expanded **return failure**
  - Choose leaf node for expansion, according to **search strategy**
  - If node contains goal state, **return solution**
  - Otherwise, expand the node. Add resulting nodes to the tree



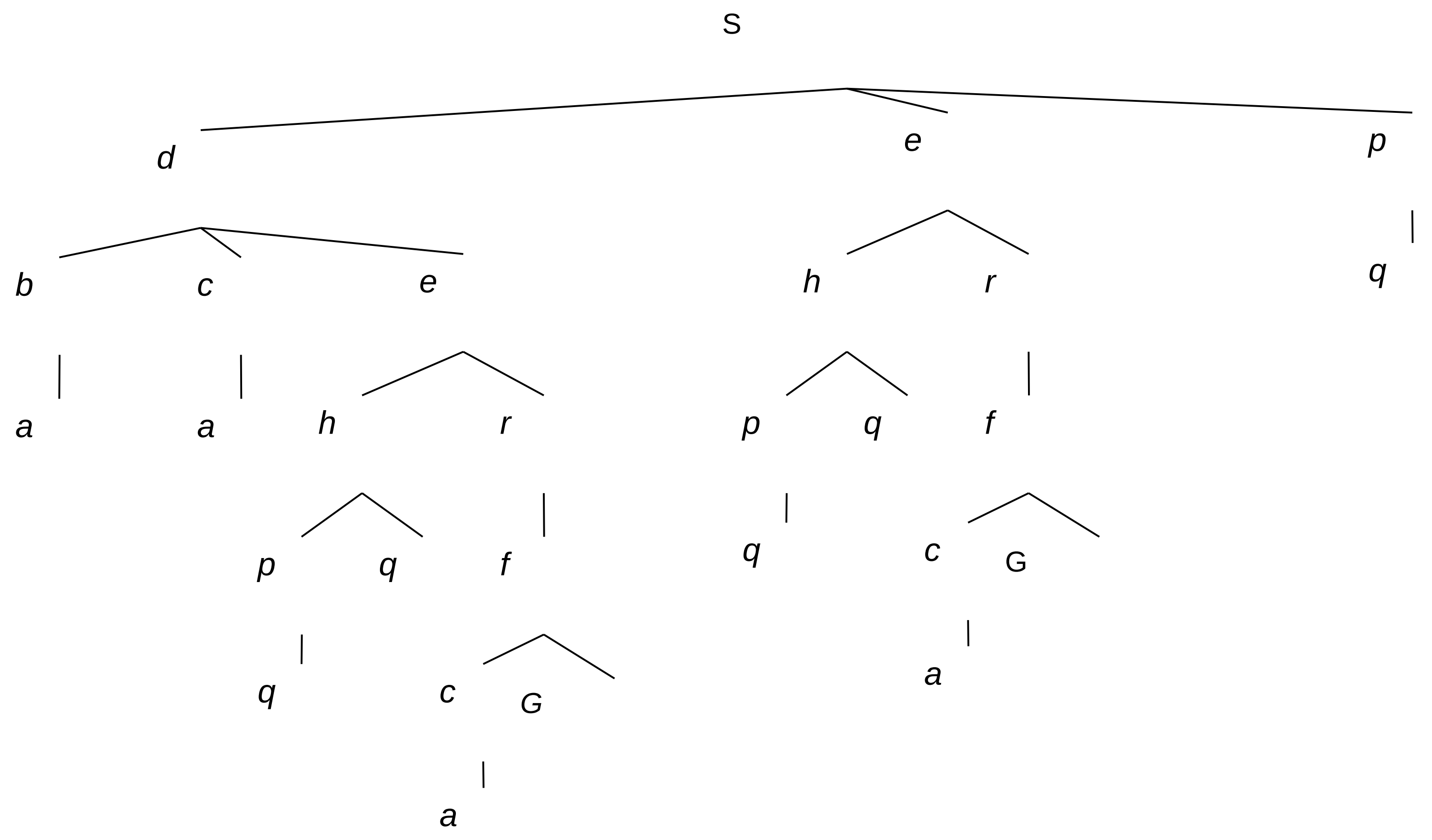
Implementation Details

Search Strategies



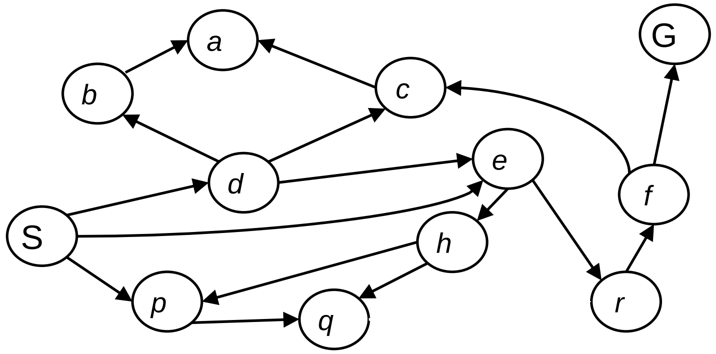
Adapted from UC Berkeley's CS188 Course

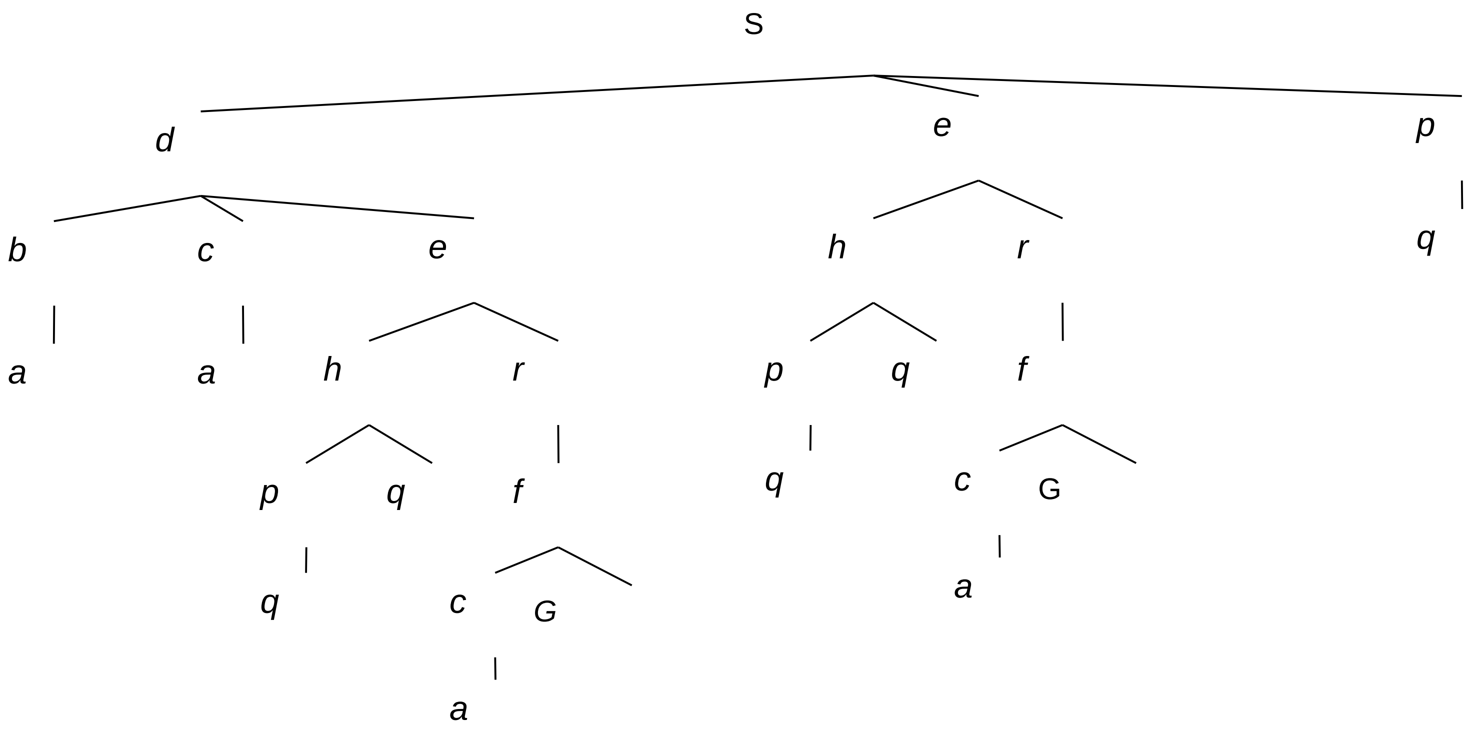
Search Strategies



Depth-First Search

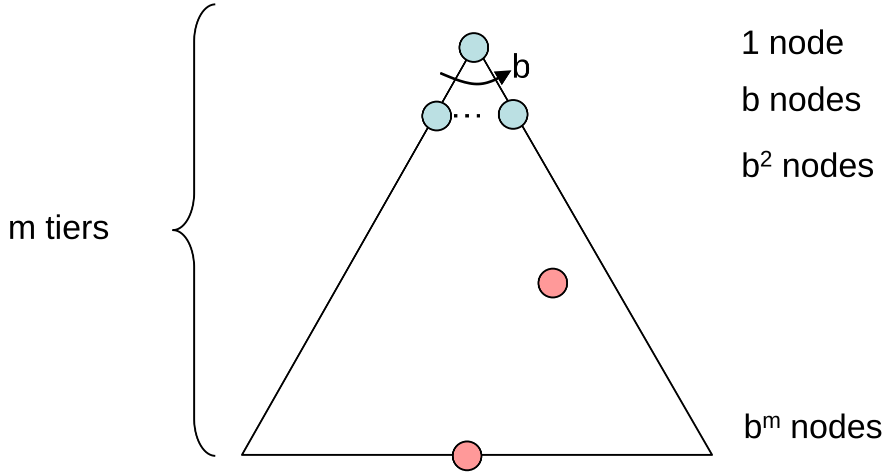
Strategy: Expand deepest node first
Implementation: LIFO stack





Key Properties

- **Completeness**: Is the alg. guaranteed to find a solution if the solution exists?
- **Optimality:** Does the alg. find the optimal solution?
- **Time complexity**
- **Space complexity** (size of the fringe)



b: branching factor
m: maximum depth
d: depth of shallowest goal node

Number of nodes in tree? $1+b+b^2+\ldots+b^m=O(b^m)$

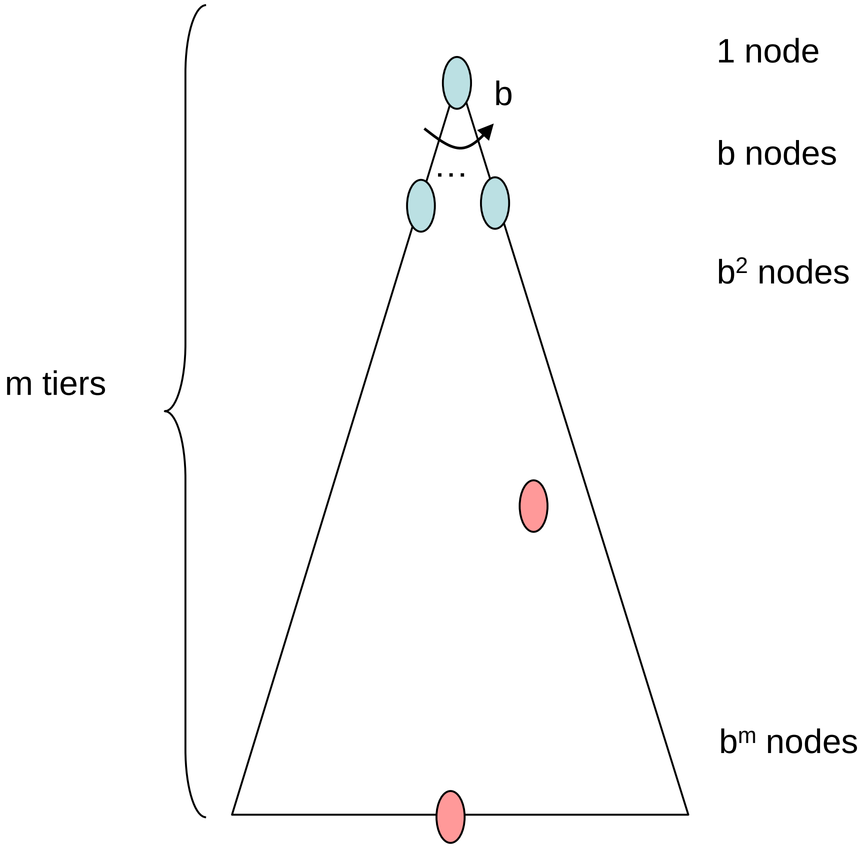
DFS Properties

Complete?

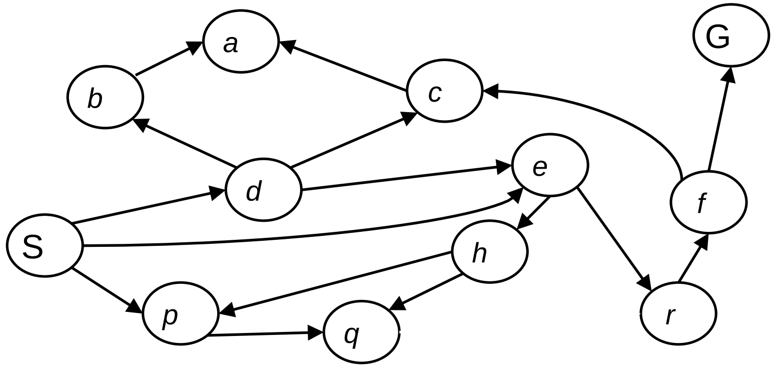
Optimal?

Time complexity

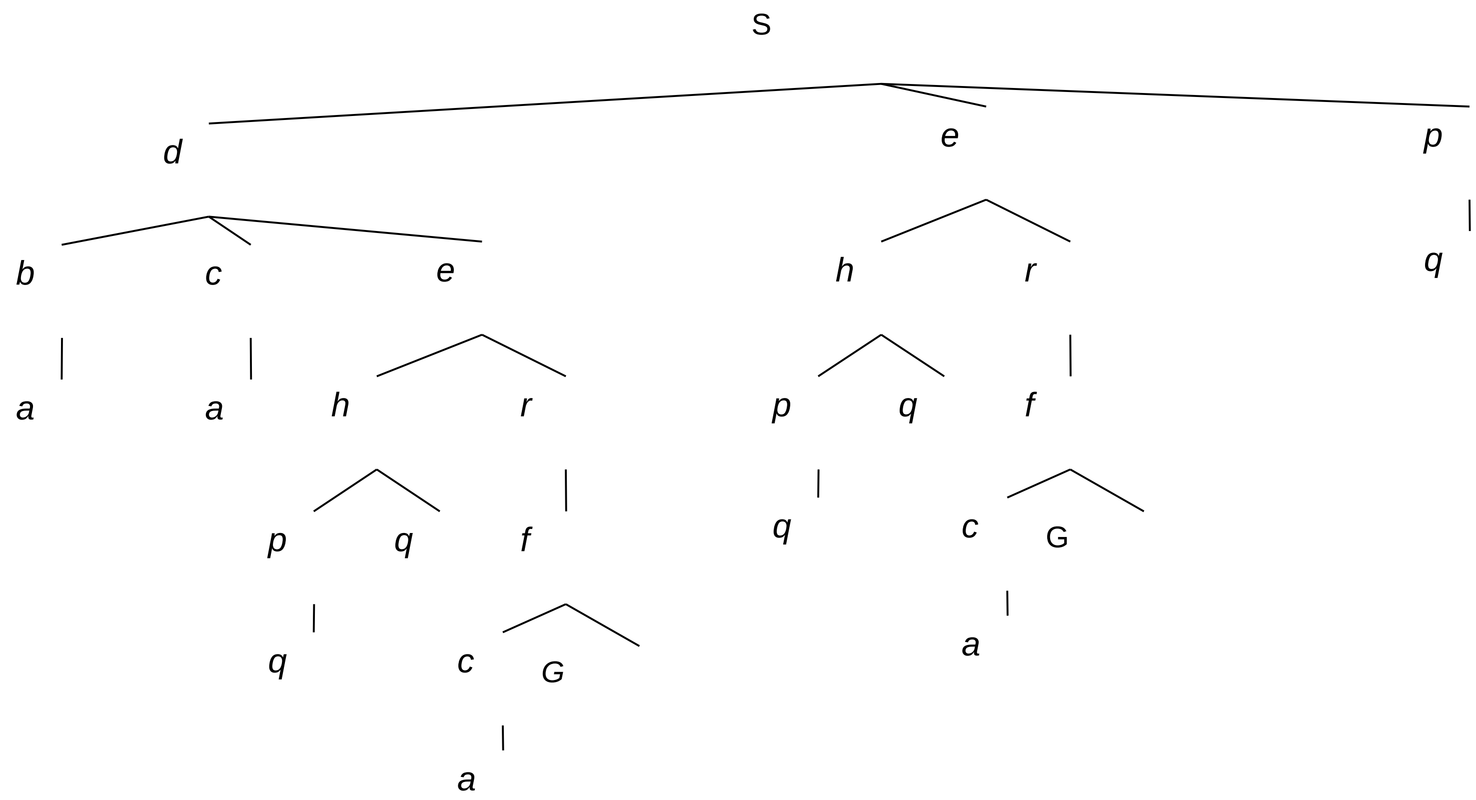
Space complexity



Breadth-First Search

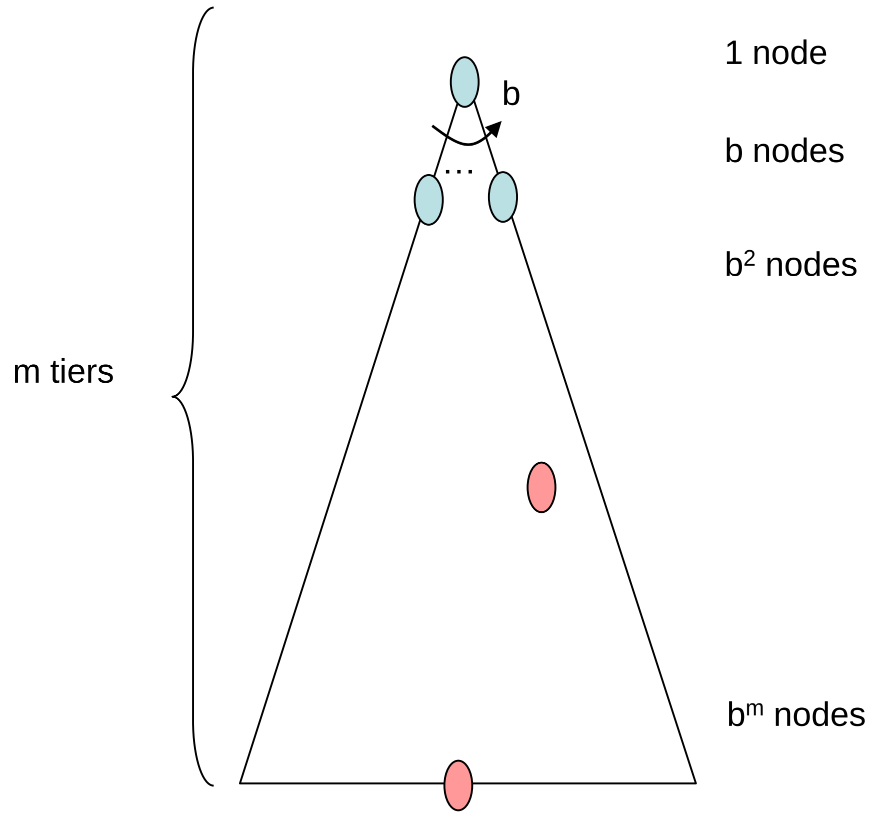


Strategy: Expand shallowest node first
Implementation: FIFO queue

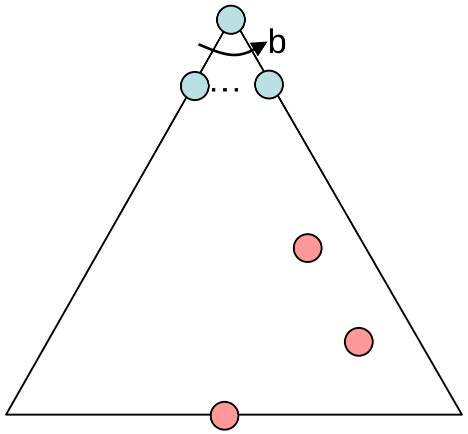


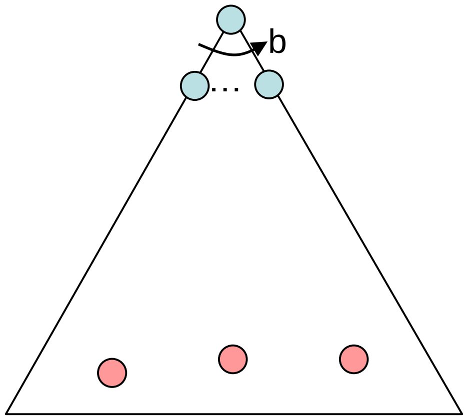
BFS Properties

- **Complete?**
- **Optimal?**
- **Time complexity**
- **Space complexity**



Quiz: DFS vs BFS





Iterative Deepening Search

- Can we combine search methods to take advantage of DFS space complexity and BFS completeness/shallow solution advantage?

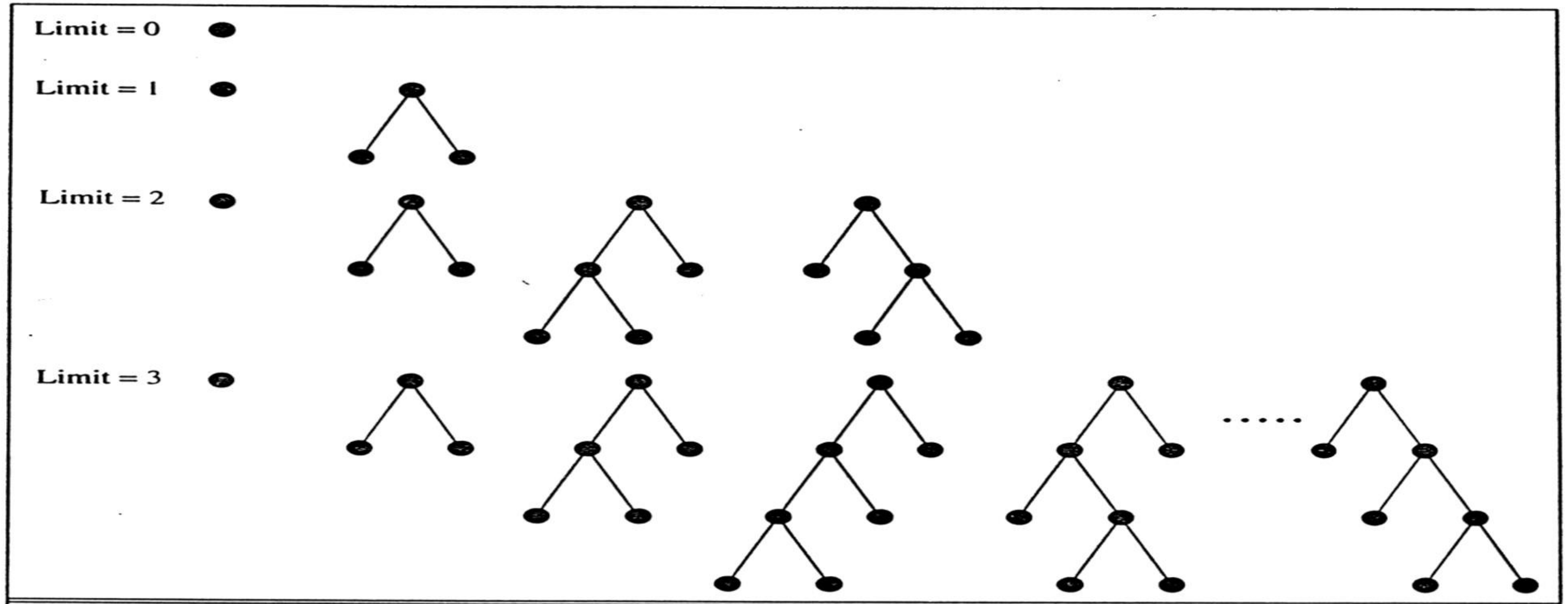
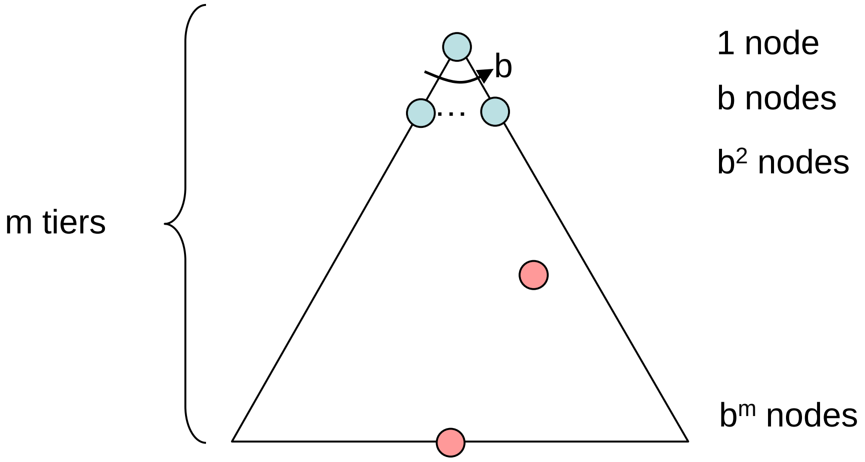


Figure 3.16 Four iterations of iterative deepening search on a binary tree.

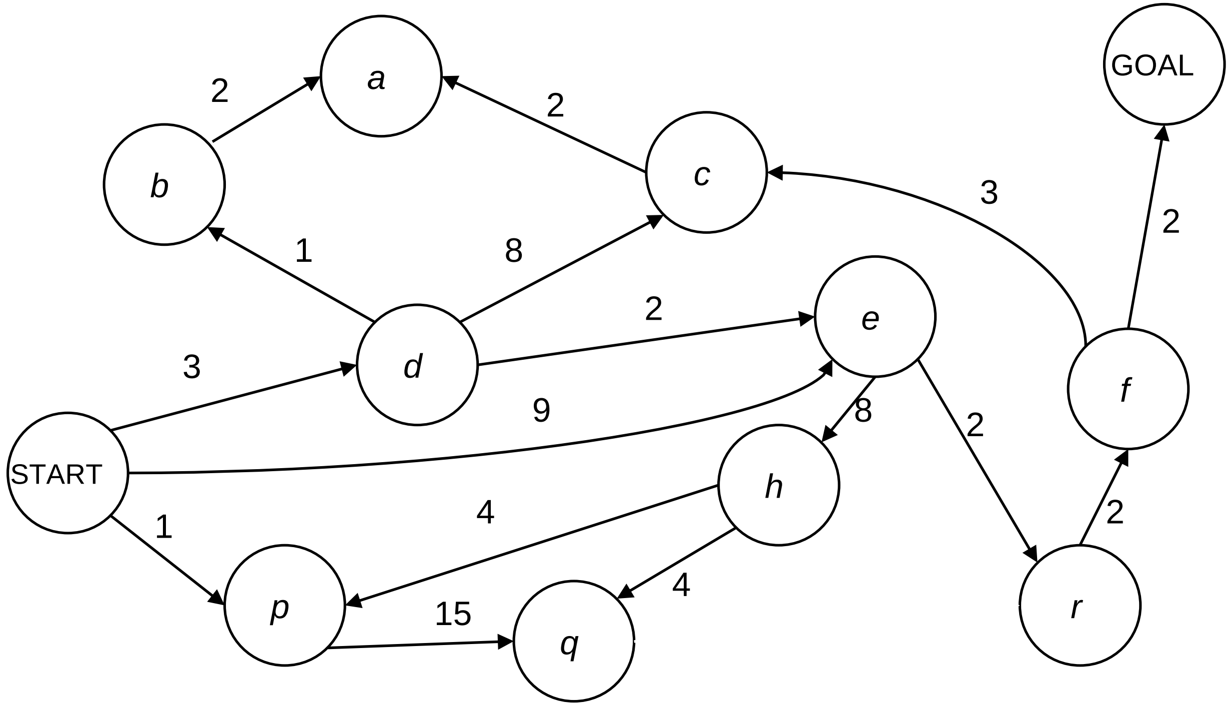
IDS Properties

- **Complete?**
- **Optimal?**
- **Time complexity**
- **Space complexity**



Wasteful? Most nodes found in lowest level of search so not too bad

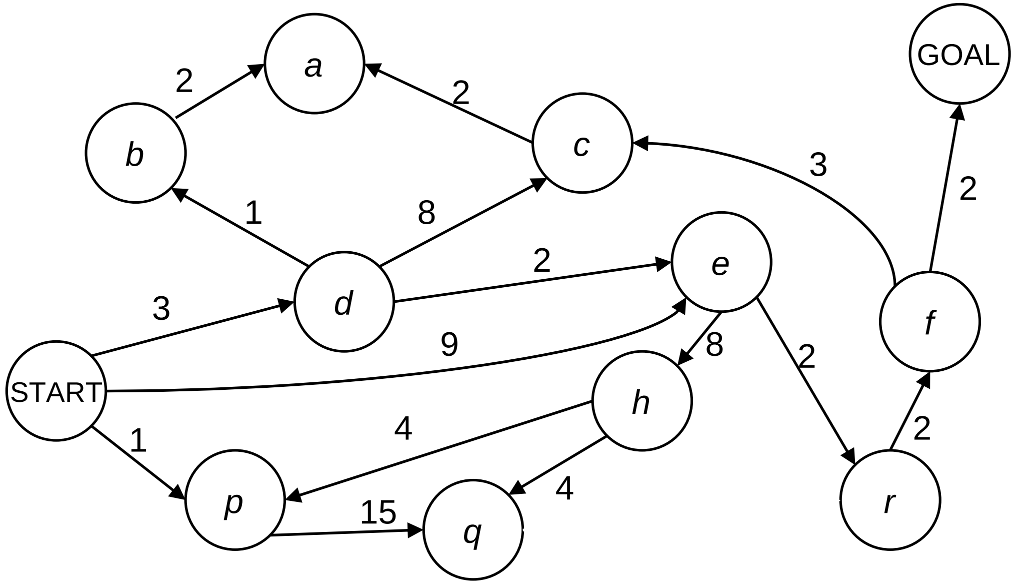
Cost-Sensitive Search



Recall that BFS was only optimal under some conditions (i.e. we only cared about number of actions taken). What can we do if actions have different costs?

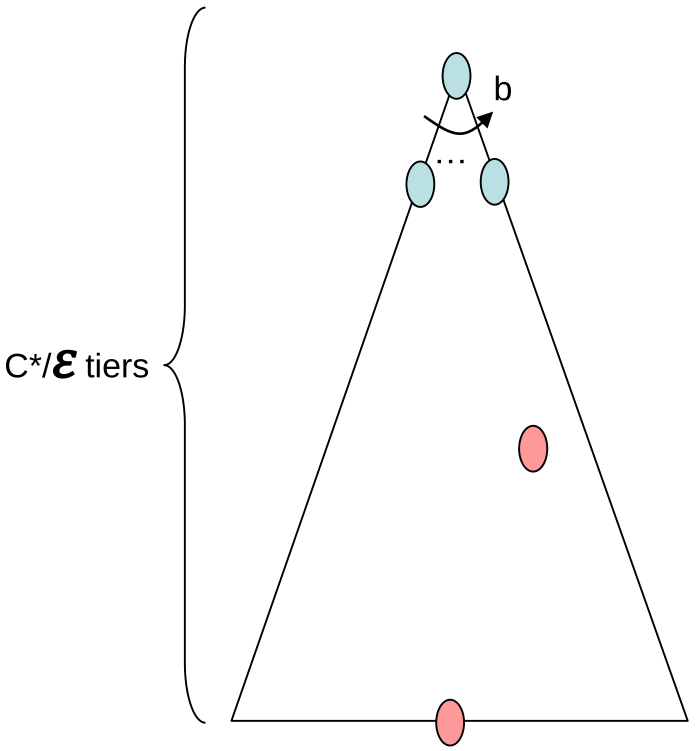
Uniform Cost Search

Strategy: Expand cheapest node first
Implementation: Priority queue



UCS Properties

- **Complete?**
- **Optimal?**
- **Time complexity**
- **Space complexity**



Summary

- These algorithms are basically the same except for the order in which they expand nodes
    - Basically all priority queues with different ways to determining priorities

- How successful the search is depends heavily on your model!

Questions?

- Next class: Informed search