## Summary of Natural Deduction $(\vdash_{\tiny{ND}})$ for Predicate Logic CS 745 Fall 2004

These rules are in addition to the rules already given for propositional logic.

	INTRODUCTION	ELIMINATION
Α	$ \begin{array}{c}     \begin{bmatrix}       x_g \\       \vdots \\       P[x_g/x] \\       \hline       \forall x \bullet P \end{array} $	$\frac{\forall x \bullet P}{P[t/x]} \forall \bot \mathbf{E}$
3	$\frac{P[t/x]}{\exists x \bullet P} \exists \bot I$	$\exists x \bullet P$ $\begin{bmatrix} x_u & P[x_u/x] & \text{assumption} \\ & \vdots & \\ Q & \\ & & \\ \hline Q & \\ & & \\ x_u & \text{does not appear in } Q. \end{bmatrix}$