

Useful Maple Functions and Hints

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Commands

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|-------------------------------|--|
| <code>with(numtheory)</code> | loads the Maple number theory package |
| <code>ifactors(n)</code> | factors the integer n into primes |
| <code>igcd(m,n)</code> | finds the greatest common denominator of integers m and n |
| <code>order(a,n)</code> | finds the order of a modulo n |
| <code>isprime(n)</code> | returns “true” if n is prime |
| <code>nextprime(n)</code> | finds the smallest prime greater than n |
| <code>phi(n)</code> | computes $\phi(n)$, where $\phi(\cdot)$ is the Euler phi-function |
| <code>primroot(g,n)</code> | finds the smallest primitive root of n greater than g |
| <code>msqrt(a,n)</code> | finds a square root of a modulo n (if it exists) |
| <code>a mod n</code> | reduces a modulo n , returning a value between 0 and $n - 1$ |
| <code>1/a mod n</code> | computes a^{-1} modulo n (if it exists) |
| <code>Power(a,b) mod n</code> | computes a^b modulo n using the square-and-multiply algorithm |
| <code>a &^ b mod n</code> | equivalent to <code>Power(a,b) mod n</code> |

Functions

Chinese Remainder Theorem

The function `chrem` uses the Chinese remainder theorem to solve a system of linear equations. That is, `chrem([a1,a2,a3],[m1,m2,m3])` finds x such that $x \equiv a_j$ modulo m_j , $j = 1, 2, 3$. For example,

`chrem([5,3,10],[7,11,13])`

returns 894.

Lagrange Interpolation

`interp([x1,x2,x3],[y1,y2,y3],x) mod n` uses Lagrange interpolation to find the polynomial $f(x)$ such that $f(x_j) \equiv y_j$ modulo n , $j = 1, 2, 3$. For example,

```
interp([1,3,5],[8,10,11],x) mod 17
```

returns $2x^2 + 10x + 13$.

Solving Equations

The function `solve(eq, var)` will find all solutions to the equation `eq` in the variable `var`. For example,

```
solve(x^2 - 10*x + 24 = 0, x);
```

yields the two solution 6, 4. If we execute the command

```
soln := solve(x^2 - 10*x + 24 = 0, x);,
```

then `soln[1] = 6` and `soln[2] = 4`.

Factoring Integers

The command

```
L:=ifactors(123456);
```

yields the result

```
L := [1, [[2, 6], [3, 1], [643, 1]]].
```

Here `L[1] = 1`; this indicates that the number being factored is positive. The list `L[2]` is

```
[[2, 6], [3, 1], [643, 1]],
```

which means that the factorization is $123456 = 2^6 3^1 643^1$. The distinct prime factors of 123 are specified by `L[2, 1, 1] = 2`, `L[2, 2, 1] = 3` and `L[2, 3, 1] = 643`.

Continued Fractions

The continued fraction expansion of a number m is obtained from the command `cfrac(m, 'quotients')`. For example, the command

```
M:=cfrac(60728973/160523347, 'quotients');
```

yields the result

```
M := [0, 2, 1, 1, 1, 4, 12, 102, 1, 1, 2, 3, 2, 2, 36].
```

The n th convergent of M is obtained from the command `nthconver(M,n)`; For example, the command `C:=nthconver(M,6)`; yields `C := 171/452`. The numerator of this fraction (171) can be obtained as `op(1,C)`; and the denominator (452) is `op(2,C)`;

Checking Running Times

To check the running time of a series of operations in Maple, use the following commands:

```
printlevel := -1;
start_time:= time();
perform desired operations
elapsed_time := (time() - start_time)*seconds;
print(elapsed_time);
printlevel := 1;
```

Random Number Generation

To generate a random integer in the range from `lower_bound` to `upper_bound`, use the following commands:

```
with(RandomTools);
seed := any desired value;
SetState( state = seed );
lower_bound := any desired value;
upper_bound := any desired value;
Generate(integer(range = lower_bound..upperbound));
```

Loops

Maple supports various types of loop structures, if-then-else constructs, etc. For example:

```
while condition do
statements
end do;
```

and

```
if condition then
statements
else
more statements
end if;
```

Procedures

Procedures have the following format:

```
Proc_name := proc( parameter list )
local local variables ;
procedure statements
return a,b,c
end proc;
```

To invoke a procedure and assign the outputs, use the following commands:

```
Out_params := Proc_name( parameter list )  
a1:= Out_params[1];  
b1:= Out_params[2];  
c1:= Out_params[3];
```

Printing

The variable `printlevel` controls how much output is produced by a Maple program. The default value of `printlevel` is 1; this causes all variables at the “top” level to be printed. To automatically print variables in (nested) loops, set `printlevel := 2` (or a higher level, if desired). To turn off all output except for user-defined print statements, set `printlevel := 0`.

Miscellaneous

To include an inline comment in a Maple program, begin the line with `#`. To continue input to the next line (this is useful for assigning large integer values), use a backslash character (`\`) at the end of a line.