Graph Drawing: From algorithms to tools to specific use case

Zhiying Jiang • 08.04.2021
Overview

Introduction
Graph and Graph Drawing
Graph Layout Algorithms
- Trees
- DAG
- General Graph

DAG Visualization Tools
- Software Based
- Web App Based

Use Case - Concept Map
- Requirement Analysis
- Implementation and Evaluation
Introduction
Introduction

History

- Noli turbare circulos meos! (Do not disturb my circles!)
- Mill or Morris games
- The Middle Ages Family Tree
Introduction

Nowadays

- Social Networks
- Knowledge Graph
- Protein Protein Interaction
- Citation Network
Graph and Graph Drawing
Graph and Graph Drawing

Graph

- graph $G = (V, E)$ is defined as the pair of vertices $V$ and edges $E$, and any edge in $E$ connects either two vertices in $V$

Graph Drawing

- it's defined as mapping $d$ that satisfies $d: G \rightarrow d(G)$, where $d(G)$ in $R^2$ (or even $R^3$). Specifically, this mapping $d$ assigns coordinates to the nodes and the bends of edges.
Graph and Graph Drawing

Types

- Tree
- DAG
- Planar Graph
- General Graph
Graph Layout Algorithms
Graph Layout Algorithms

Tree (Diagram Types)

- Indentation
- Node-Link diagrams
- Enclosure diagrams
- Layered Diagrams
Graph Layout Algorithms

**Tree (Knuth’s)**

- Do a top-down inorder traversal of a tree, with the depth as its y value and the global counter as its x value.

```python
def knuth_layout(tree, depth):
    i = 0
    if tree.left_child:
        knuth_layout(tree.left_child, depth+1)
    tree.x = i
    tree.y = depth
    i += 1
    if tree.right_child:
        knuth_layout(tree.right_child, depth+1)
```

**Principles:**

1. No crossed edges.
2. Nodes at the same level/depth should be placed on the same horizontal line (same y value).
Graph Layout Algorithms

Tree (Knuth’s)

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```

What’s missing?

- Might be:
Graph Layout Algorithms

Tree (Wetherell’s)

- Do a bottom-up algorithm that keeps track of next slot on each row and then traverse the tree in postorder

Principles:

1. No crossed edges.
2. Nodes at the same level/depth should be placed on the same horizontal line (same y value).
3. Place the whole graph into minimum width
Graph Layout Algorithms

Tree (Wetherell’s)

- Do a bottom-up algorithm that keeps track of next slot on each row and then traverse the tree in postorder

What’s missing?
Graph Layout Algorithms

Tree (Reingold-Tilford’s)

- Start with bottom-up pass of the tree. The initialization of x coordinate is arbitrary and y coordinate is by depth; then merge left and right subtrees by shifting right and finally do a top-down pass for assignment of final positions. global counter as its x value.

Additional Principles:

4. Parent should be centered above its children
5. Isomorphic subtrees should be drawn identically
Graph Layout Algorithms

Tree (Reingold-Tilford’s)

Algorithm 1: Reingold-Tilford Algorithms

Do post-order traversal of the tree

if node v is a leaf then
    v.x = 0;
else
    Place the right subtree of v as close to v as possible;
    Record how many Δx to move
end

Place the node halfway between its children.

A second top-down pass to accumulate Δx for the final assignment.

Additional Principles:

4. Parent should be centered above its children

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Graph Layout Algorithms

Tree (Reingold-Tilford’s)

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Finally: 👏
Graph Layout Algorithms

Directed Acyclic Graph (DAG)

- Directed graphs with no cycles
- If and only if can be ordered topologically, by arranging the vertices as a linear ordering that is consistent with all edge directions
- Comparing to trees, allow multiple parents
Graph Layout Algorithms

Directed Acyclic Graph (DAG)

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- Comparing to trees, allow multiple parents
Graph Layout Algorithms

**DAG (Sugiyama’s method) - Principles**

- Edges should point in a uniform direction
- Short edges are more readable
- Nodes should be distributed uniformly to avoid clutter
- Edge crossings should be minimized
- Straight edges are more readable
Graph Layout Algorithms

DAG (Sugiyama’s method) - High Level Algorithm

<table>
<thead>
<tr>
<th>Algorithm 2: Sugiyama methods in a high level</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cycles Removal;</td>
</tr>
<tr>
<td>Calculate layering;</td>
</tr>
<tr>
<td>Crossing Reduction;</td>
</tr>
<tr>
<td>Routing of the edges;</td>
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</tbody>
</table>
Graph Layout Algorithms

DAG (Sugiyama’s method) - High Level Algorithm

- Cycles Removal;
- Calculate layering;
- Crossing Reduction;
- Routing of the edges;
Graph Layout Algorithms

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Graph Layout Algorithms

General Graph

- No explicit hierarchy
- Often large scale

The Principle

- Minimizing crossing edges
Graph Layout Algorithms

General Graph (Force Directed Method)

- Also called “Spring Embedder”
- Assign “force” to pair of nodes
- Treat graph layout optimization as a “physical system” simulation problem
- General framework
Graph Layout Algorithms

General Graph (Force Directed Method)

Basic Version:

**Algorithm 3: Force Directed Method**

```
foreach node v do
    foreach pair of nodes (u, v) do
        compute repulsive force \( f_r(u, v) \)
    foreach edge \( e = (u, v) \) do
        compute attractive force \( f_a(u, v) \)
    sum over all force vectors on \( v \rightarrow F(v) \);
    move node \( v \) according to \( F(v) \)
```

|Attractive force|: c1*log(d/c2)

|Repulsive force|: c3/d^2
Graph Layout Algorithms

Aesthetics

- Visual complexity --- how easy it is to get an overview
- Regularity --- repetitions like if isomorphic graphs look the same
- Symmetry --- geometric symmetry by rotation, reflection and translation
- Consistence --- if showing similar patterns indicates similar meaning
- Form, size and proportionality --- size and `node density and sparsity``
- Algorithms' time complexity --- how long does algorithm take to run
DAG Visualization Tools
DAG Visualization Tools

GraphViz

- DOT language
  - Simple & Intuitive
  - Adopted by many other applications
  - Support any output format like GIF, PNG, SVG, PDF or PostScript

- Sugiyama’s method for directed graph

```
digraph G {
    main -> parse -> execute;
    main -> init;
    main -> cleanup;
    execute -> make_string;
    execute -> printf
    init -> make_string;
    main -> printf;
    execute -> compare
}
```
DAG Visualization Tools

GraphViz

- **CLI**
  - dot for directed graph
  - neato for undirected graph

- **Web**
  - webdot HTTP server

```
dot -Tsvg input.dot
```

<img src="/cgi-bin/webdot/input1.dot.neato.png">
DAG Visualization Tools

TikZ/PGF

- For TeX
- Basically can draw anything
- All graph layout algorithms require LuaTeX compiler
  - You can also implement your own algorithm in Lua
- Intuitive syntax
DAG Visualization Tools

d3dagre

- d3 + dagre
- dagre is a specific “flavor” of Sugiyama’s method
- Take full advantage of d3’s flexibility without writing layout algorithm
- Steep learning curve
- SVG
DAG Visualization Tools

Cytoscape.js

- Origin from software, aiming at analyzing large scale bio-medical data
- Specialized for graph, no other charts
- Number of graph analysis functions implemented, like minimum spanning tree, clustering, etc.
- Have the most graph layout algorithms
- Canvas
DAG Visualization Tools

GoJS

- Model-View architecture to separate data and style
- Limited pre-built layout algorithm
- Mature commercialized data visualization library
- Easy-to-use API
- Canvas
My Use Case - Concept Map
Concept Map

Intro

- Node? - Concept
- Concept? - Subject concepts like “bayes’ rule”, “gradient descent”
- Edge? - Prerequisite relation
- Scale? - About 500 concepts, 1000 relations
Concept Map

Requirement Analysis

- Cannot fit in one screen - Zoom in/out function required
- Too many nodes to see prerequisite nodes clearly - Highlight prerequisite nodes and relations required
- Nodes need to display text directly - text wrapper or auto-fitting to the shape or other style manipulation required
Concept Map

Implementation and Evaluation (Full Graph)

- Layout Complexity
- Styling Flexibility
- Function Flexibility
- How easy to implement
- Speed
Concept Map
Implementation and Evaluation (Full Graph)
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Concept Map

Implementation and Evaluation (Full Graph)

- Layout Complexity
  - Cytoscape: Clear hierarchy, messy direct lines but easier to trace back
  - GoJS: Clean layout, zigzag lines, impossible to trace
  - d3dagre: Too many parallel lines, impossible to trace; too spacious
Concept Map

Implementation and Evaluation (Full Graph)

- Styling Flexibility
  - Cytoscape: text wrapper available, but rigorous on padding, which makes text too small
  - GoJS: text wrapper available, easy to configure, nice result
  - d3dagre: text wrapper not available, but shape will adopt to the text automatically; basically full control
Concept Map

Implementation and Evaluation (Full Graph)

- Function Flexibility (especially for highlighting prerequisites)
  - Cytoscape: Extremely easy to find parents or ancestors as they have functions available to call directly
  - GoJS: Can find parents but ancestors need to hack through their API
  - d3dagre: No handy tools to calculate parents or ancestors at front-end, but flexible to read and manipulate any back-end data
Concept Map

Implementation and Evaluation (Full Graph)

● How easy to implement
  ○ Cytoscape: Detailed documentation, many examples, lots of available functions
  ○ GoJS: Detailed documentation, many examples, easy to configure
  ○ d3dagre: Limited documentation, steep learning curve because of d3
Concept Map

Implementation and Evaluation (Full Graph)

- Speed
  - Cytoscape: 10.26s because of this layout, much faster for layout like BF layout
  - GoJS: 3.56s, thanks to Canvas
  - d3dagre: 11.88s because of the layout and also the fact that SVG is not as fast as Canvas
Concept Map

Implementation and Evaluation (Full Graph)

● More discussion
  ○ SVG, although slow, can manipulate every single DOM element inside, which makes us able to search text directly inside browser. But Canvas can’t.
  ○ Full graph visualization still seem to be unrealistic
  ○ Maybe should try visualize a subgraph (clique) of the whole graph
Concept Map
Implementation and Evaluation (Sub Graph)
Concept Map
Implementation and Evaluation (Sub Graph)
Concept Map
Implementation and Evaluation (Sub Graph)
Concept Map
Implementation and Evaluation (Sub Graph)
Concept Map

Implementation and Evaluation (Sub Graph)

- More discussion
  - GoJS, although still has cleaner layout, becomes disadvantageous because of its zigzag edges.
  - They probably don’t do routing of the edges. Ironically, this might be desirable for really large graphs according to our previous experiments.
  - Sub graph seems to be a feasible solution for now
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Thanks!
References


Image References

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