

DATABASE DESIGN

Other Dependencies and SQL

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Other Dependencies

other anomalies/redundancies in relational schemas?

⇒ beyond FDs and BCNF??

Example: consider the following table (in BCNF):

Course	Teacher	Book
Math	Smith	Algebra
Math	Smith	Calculus
Math	Jones	Algebra
Math	Jones	Calculus
Physics	Black	Mechanics
Physics	Black	Optics

⇒ tuples (Course, Set-of-profs, Set-of-books) in 1NF.

Multivalued Dependencies (MVD)

- *CTB* table contains redundant information because:

whenever $(c, t_1, b_1) \in CTB$ and $(c, t_2, b_2) \in CTB$

then also $(c, t_1, b_2) \in CTB$

and, by symmetry, $(c, t_2, b_1) \in CTB$

- we say that a **multivalued dependency** (MVD)

$C \twoheadrightarrow B$ (and $C \twoheadrightarrow T$ as well)

holds on *CTB*.

given a course, the set of teachers and the set of books are uniquely determined and independent.

Another Example

Course	Teacher	Hour	Room	Student	Grade
CS101	Jones	M-9	2222	Smith	A
CS101	Jones	W-9	3333	Smith	A
CS101	Jones	F-9	2222	Smith	A
CS101	Jones	M-9	2222	Black	B
CS101	Jones	W-9	3333	Black	B
CS101	Jones	F-9	2222	Black	B

- FDs:

$C \rightarrow T$, $CS \rightarrow G$, $HR \rightarrow C$, $HT \rightarrow R$, and $HS \rightarrow R$

- MVDs:

$C \twoheadrightarrow HR$

Axioms for MVDs

1. $Y \subset X \Rightarrow X \twoheadrightarrow Y$ (reflexivity)
2. $X \twoheadrightarrow Y \Rightarrow X \twoheadrightarrow (R - Y)$ (complementation)
3. $X \twoheadrightarrow Y \Rightarrow XZ \twoheadrightarrow YZ$ (augmentation)
4. $X \twoheadrightarrow Y, Y \twoheadrightarrow Z \Rightarrow X \twoheadrightarrow (Z - Y)$ (transitivity)
5. $X \rightarrow Y \Rightarrow X \twoheadrightarrow Y$ (conversion)
6. $X \twoheadrightarrow Y, XY \rightarrow Z \Rightarrow X \rightarrow (Z - Y)$ (interaction)

Theorem: Axioms for FDs (1)-(6) are sound and complete for logical implication of FDs and MVDs.

Example

In the *CTHRSG* schema $C \twoheadrightarrow SG$:

1. $C \twoheadrightarrow HR$
2. $C \twoheadrightarrow T$ (from $C \rightarrow T$)
3. $C \twoheadrightarrow CTSG$ (complementation of (1))
4. $C \twoheadrightarrow CT$ (augmentation of (2) by C)
5. $CT \twoheadrightarrow CTSG$ (augmentation of (3) by T)
6. $C \twoheadrightarrow SG$ (transitivity on (4) and (5))

\Rightarrow the “rest” of the *CTHRSG* attributes (except C)
are **partitioned** to disjoint groups
each *multidetermined* by C .

Dependency Basis

Definition:

A **dependency basis** for X with respect to a set of FDs and MVDs F is a partition of $R - X$ to sets Y_1, \dots, Y_k such that $F \models X \twoheadrightarrow Z$ if and only if $Z - X$ is a union of some of the Y_i s.

- used as a quick test of $F \models X \twoheadrightarrow Y$ and $F \models X \rightarrow Y$
- unlike for FDs we can't split right-hand sides of MVDs to single attributes (cf. minimal cover).
- the dependency basis of X w.r.t. F can be computed in PTIME [Beeri80].

Lossless-Join Decomposition

- similarly to the FD case we want to decompose the schema to avoid anomalies

⇒ a lossless-join decomposition (R_1, R_2) of R with respect to **MVDs** F :

$$F \models (R_1 \cap R_2) \twoheadrightarrow (R_1 - R_2)$$

or, by symmetry

$$F \models (R_1 \cap R_2) \twoheadrightarrow (R_2 - R_1)$$

- this condition implies the condition for FDs (in only FDs appear in F).

Fourth Normal Form (4NF)

Definition:

Let R be a relation schema and F a set of FDs and MVDs.

Schema R is in **4NF** if and only if

whenever $(X \twoheadrightarrow Y) \in F^+$ and $XY \subseteq R$, then either

- $(X \twoheadrightarrow Y)$ is trivial ($Y \subseteq X$ or $XY = R$), or
- X is a superkey of R

A database schema $\{R_1, \dots, R_n\}$ is in BCNF if each relation schema R_i is in 4NF.

\Rightarrow use BCNF-like decomposition procedure to obtain 4NF.

Example

The *CTB* schema can be decomposed to 4NF
(using $C \twoheadrightarrow P$) as follows:

Course	Teacher
Math	Smith
Math	Jones
Physics	Black

Course	Book
Math	Algebra
Math	Calculus
Physics	Mechanics
Physics	Optics

⇒ no FDs here!

Other Dependencies

- **Join Dependency** on R

$\Rightarrow \bowtie [R_1, \dots, R_k]$ holds if $I = \pi_{R_1}(I) \bowtie \dots \bowtie \pi_{R_k}(I)$

\Rightarrow generalization of an MVD

$X \twoheadrightarrow Y$ is the same as $\bowtie [XY, X(R - Y)]$

\Rightarrow **cannot** be simulated by MVDs

\Rightarrow no axiomatization

\Rightarrow Project-Join NF (5NF)

$\bowtie [R_1, \dots, R_k]$ implies R_i is a key.

- **Inclusion Dependency** on R and S

$\Rightarrow R[X] \subseteq S[Y]$ holds if $\pi_X(I_R) \subseteq \pi_Y(I_S)$

\Rightarrow relates **two** relations

foreign-key relationships

Integrity Constraints vs. Queries

Observation:

- Queries:
first-order formulas true in a database (instance) for a given valuation.
- Integrity constraints:
assertions about all valid database instances

Integrity Constraints as queries?

⇒ **YES**, we use *closed first-order formulas*

Dependencies as Formulas

Let $R(A, B, C)$ and $S(A, B)$ be two relational schemas.

- FD $A \rightarrow B$ on R :

$$\forall x, y_1, y_2, z_1, z_2. R(x, y_1, z_1) \wedge R(x, y_2, z_2) \Rightarrow y_1 = y_2$$

- MVD $A \twoheadrightarrow B$ on R :

$$\forall x, y_1, y_2, z_1, z_2. R(x, y_1, z_1) \wedge R(x, y_2, z_2) \Rightarrow R(x, y_1, z_2)$$

- IND $R[A] \subseteq S[A]$ on R and S :

$$\forall x, y, z. R(x, y, z) \Rightarrow \exists u. S(x, u)$$

- etc, etc.

Generalized Dependencies

Why don't we just use general first-order formulas for integrity constraints?

- notational convenience
- decidable theories
 - ... at least in many cases.
- axiomatizations
- normal forms induced by the constraints

Integrity Constraints in SQL

- connected with a table (definition)
 - ⇒ Primary Keys
 - ⇒ Foreign Keys
 - ⇒ **CHECK** constraints
- separate ECA rules (triggers)

Primary Key

- specifies a *primary key* in a table
- syntax:

```
CREATE TABLE <name>
  (
    ... <attributes>,
    PRIMARY KEY ( <list of attr> )
  )
```

- also creates an unique index on the key

Example

```
create table DEPT
( ID          integer not NULL,
  DeptName    char(20),
  MgrNO       char(3),
  PRIMARY KEY (ID)
)
```

Example (cont.)

```
sql => insert into DEPT values \  
sql (cont.) => ( 1 , 'Computer Science', 000100)  
DB20000I  The SQL command completed successfully.
```

```
sql => insert into DEPT values \  
sql (cont.) => ( 1 , 'Computer Science', 000100)  
SQL0803N  One or more values in the INSERT or UPDATE  
statement are not valid because they would produce  
duplicate rows for a table with a unique index.  
SQLSTATE=23505
```

Foreign Key

- specifies an *referential constraint*
- syntax:

```
CREATE TABLE <name>
(
    ... <attributes>,
    FOREIGN KEY ( <attrs> )
    REFERENCES <ref-table>( <attrs> )
    ON DELETE <delete-action>
    ON UPDATE <update action>
```

- the actions can be:
 - * **RESTRICT** – produce an error
 - * **CASCADE** – propagate the delete
 - * **SET NULL** – set to “unknown”

Example

```
create table EMP
( SSN      integer not NULL,
  Name     char(20),
  Dept     integer,
  Salary   dec(8,2),
  primary key (SSN),
  foreign key (Dept) references DEPT(ID)
                        on delete cascade
                        on update restrict)
```

Example (cont.)

```
db2 => insert into EMP \
sql (cont.) => values ( 999, 'DAVE', 2, 50000 )
SQL0530N  The insert or update value of FOREIGN KEY
"DAVID.EMP.SQL970916001756640" is not equal to any
value of the primary key of the parent table.
SQLSTATE=23503
```

```
db2 => insert into EMP \
sql (cont.) => values ( 999, 'DAVE', 1, 50000 )
DB20000I  The SQL command completed successfully.
db2 => select * from emp where SSN=999
```

SSN	NAME	DEPT	SALARY
999	DAVE	1	50000.00

```
db2 => delete from DEPT where id=1
DB20000I  The SQL command completed successfully.
db2 => select * from emp where SSN=999
```

SSN	NAME	DEPT	SALARY
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CHECK constraints

- allow checking for “correct” data:
- syntax:

```
CREATE TABLE <name>
    (    ... <attributes>,
      CHECK <condition>
    )
```

- condition is a *simple* search condition
⇒ no subqueries (in DB2)

Example

```
create table EMP
( SSN      integer not NULL,
  Name     char(20),
  Dept     integer,
  Salary   dec(8,2),
  primary key (SSN),
  foreign key (Dept) references DEPT(ID)
          on delete cascade
          on update restrict,
  check ( salary > 0 )
)
```

```
db2 => insert into emp values (998, 'DAVE', 1, 0 )
SQL0545N  The requested operation is not allowed
because a row does not satisfy the check constraint
"DAVID.EMP.SQL970916000939620".  SQLSTATE=23513
```


Active (ECA) Rules

- for more complex integrity constraints and other things
- general structure:

```
CREATE TRIGGER <name>
  <event> ON <table>
  REFERENCING <transition-tables>
  FOR EACH ROW | FOR EACH STATEMENT
  WHEN <condition> <sql-statement>
```

- events:

- * AFTER or NO CASCADE BEFORE, and
- * INSERT, DELETE, or UPDATE (col)

- transition tables:

- * OLD AS <id>, NEW AS <id>
(single row)
- * OLD_TABLE AS <id>, NEW_TABLE AS <id>
(transition tables)

Summary

Schema design summary:

1. Create an ER diagram
 - ⇒ visualization of the design goals
2. Translate ER-to-Relational
3. Determine FD, MVD, JD, . . .
 - ⇒ detect anomalies and decompose
 - ⇒ find **keys**
4. Determine inter-relational constraints
 - ⇒ INDs and foreign key constraints
5. Enforce rest of constraints
 - ⇒ **CHECK** declarations
 - ⇒ ECA rules (only as the last resort!)