

Midterm Practice Problems

Disclaimer: I in no way suggest that this is comprehensive. Students should review their notes, assignments and sample problems in conjunction with these practice problems. Sample midterms are on the wiki.

For reference, you may need some or all of the following formulas

$$\sum_{i=1}^n i = \frac{n(n+1)}{2} \quad \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6} \quad \sum_{i=1}^n i^3 = \frac{n^2(n+1)^2}{4}$$

1) Using the definition of an integral (with right endpoints in the Riemann sums), evaluate

i. $\int_0^4 3dx$

ii. $\int_0^1 (2x+3)dx$

2) Integrate $\int \sec^3(x)dx$ (Hint: Try by parts splitting up the secant terms)

3) Integrate all of the below.

(i) $\int_1^2 \frac{1+u^2}{u^3} du$

(ii) $\int (u^2 - 1)^2 du$

(iii) $\int \arctan(x) dx$

(iv) $\int \tan(x) dx$

(v) $\int_0^{\frac{\pi}{4}} \sec^2(t) dt$

(vi) $\int e^u \sin(u) du$

(vii) $\int \frac{\ln(x)}{x^2} dx$

(viii) $\int_1^2 \frac{e^{x-1}}{x^2} dx$

(ix) $\int \frac{1}{2x} dx$

(x) $\int \frac{1}{\sqrt{1-x^2}} dx$

(xi) $\int_0^{\pi} \sec(x) \tan(x) dx$

(xii) $\int 10^u du$

(xiii) $\int_{-1}^1 x^2 \sin(x) dx$

(xiv) $\int_0^1 \frac{4}{t^2+1} dt$

(xv) $\int \sec(t) dt$

(xvi) $\int_1^4 \frac{1}{x^3} dx$

(xvii) $\int \frac{t^9}{1+t^{20}} dt$

(xviii) $\int x \ln(x) dx$

(xix) $\int_{-1}^1 |x^3 - x| dx$

(xx) $\int \frac{x^2}{1+x^2} dx$

(xxi) $\int_0^{\pi} \sin(x) dx$

(xxii) $\int \frac{3}{t \ln(t)} dt$

(xxiii) $\int_0^{\pi} \cos(x) dx$

(xxiv) $\int x^2 e^x dx$

(xxv) $\int \frac{4x^3+1}{x^4+x} dx$

- (xxvi) $\int 4x^2\sqrt{x^3+2}dx$
 (xxvii) $\int \ln(t)dt$
 (xxviii) $\int_{-5}^3 |x^2-4|dx$
 (xxix) $\int 2t \log_3(t)dt$
 (xxx) $\int_{-10}^{10} (2x^3+5x^7+11x^{13}+17x^{19}+23x^{29})dx$
 (xxxii) $\int_0^{\ln(3)} \frac{e^t}{e^t+1} dt$
 (xxxiii) $\int x^3 \cos(4x^4+10)dx$
 (xxxiv) $\int_{-1}^3 (x^2+x+1)dx$
 (xxxv) $\int \frac{x}{1+x^4} dx$
 (xxxvi) $\int \sec^2(t)dt$
 (xxxvii) $\int x \sin(x)dx$
 (xxxviii) $\int_{e^2}^{e^3} (\ln(x))^2 dx$
 (xxxix) $\int u \arctan(u)du$
 (xl) $\int \frac{1+x}{1+x^2} dx$
 (xli) $\int x e^{-x} dx$
 (xlii) $\int \cos(x) e^{\sin(x)} dx$
 (xliii) $\int \cos(x) \sin(x) dx$
 (xliv) $\int x^2 \cos(x) dx$
 (xlv) $\int e^x \sin(x) dx$
 (xlvi) $\int \tan^5(x) dx$
 (xlvii) $\int \frac{x+27}{x^2-9} dx$
 (xlviii) $\int \frac{x+27}{x^2+9} dx$
 (xlix) $\int \sec^2(x) \sqrt{5+\tan(x)} dx$
 (l) $\int \cos^2(x) dx$
 (li) $\int x^2 \sqrt{4-x^2} dx$
 (lii) $\int x^2 \sqrt{4+x^2} dx$
 (liii) $\int x^2 \sqrt{x^2-4} dx$
 (liv) $\int \frac{2x+1}{x(1-x)} dx$
 (lv) $\int (\csc(x) + \cot(x))^2 dx$ **
 (lvi) $\int \sin^{10}(x) \cos^5(x) dx$
 (lvii) $\int \cos^2(x) dx$
 (lviii) $\int \sin^2(x) dx$
 (lix) $\int \ln^2(x) dx$
 (lx) $\int 5^x dx$
 (lxi) $\int \frac{7x-26}{x^2-6x-16} dx$
 (lxii) $\int \left(\frac{\tan(x)}{\cos(x)} \right)^3 dx$
 (lxiii) $\int_{-1}^1 \frac{1}{x} dx$
 (lxiv) $\int_{-1}^1 x dx$
 (lxv) $\int_{-1}^1 \frac{1}{x^{0.999}} dx$

- (lxvi) $\int e^{\sqrt{x}} \sqrt{x} dx$
 (lxvii) $\int \sqrt{x^2 + 6x} dx$
 (lxviii) $\int \tan^4(x) \sec^4(x) dx$
 (lxix) $\int_{1/2}^1 \frac{1}{\sqrt{2x-x^2}} dx$
 (lxx) $\int \frac{1}{e^x \sqrt{e^{2x}-9}} dx$
 (lxxi) $\int \frac{\sec^2(x)}{\tan^2(x)-\tan(x)} dx$
 (lxxii) $\int \frac{1}{x^4-16} dx$
 (lxxiii) $\int \frac{1}{x^4+4} dx$
 (lxxiv) $\int \frac{1}{x^2+4} dx$
 (lxxv) $\int \frac{1}{\sqrt{x}(\sqrt{x}+1)} dx$
 (lxxvi) $\int \sec^3(x) dx$ **
 (lxxvii) $\int \frac{1}{x\sqrt{1+x^2}} dx$
 (lxxviii) $\int_{-1}^2 |e^x - 1|$
 (lxxix) $\int_6^8 \frac{4}{(x-6)^3} dx$
 (lxxx) $\int_0^1 \arcsin(x) dx$
 (lxxxii) $\int_0^1 \frac{3}{x^5} dx$
 (lxxxiii) $\int \frac{4x^2-2x}{(x-1)(x^2+1)} dx$
 (lxxxiv) $\int \tan(x) \sec^3(x) dx$
 (lxxxv) $\int \frac{1}{\sqrt{x^2+2x+2}} dx$
 (lxxxvi) $\int \cos(\pi x) dx$
 (lxxxvii) $\int \sin(x) \cos^5(x) dx$
 (lxxxviii) $\int \frac{1}{x\sqrt{x}} dx$
 (lxxxix) $\int \sin^5 \cos^2(x) dx$
 (xc) $\int \frac{x^4+3x^2+1}{x^5+5x^3+5x} dx$

4) Find the centroid of the region bounded by

- (i) $x + y = 2$, $x = y^2$.
 (ii) $y = 1 + \sin(x)$ between $x = -\pi/2$ and $x = \pi/2$ and the x -axis.
 (iii) $y = 5x$ between $y = -1$ and $x = 2$.