Many conjectures in combinatorics concern the existence or nonexistence of combinatorial objects that are only feasibly constructed through a search.

Typically a lot of domain-specific knowledge is known about such objects, but it is necessary to use a computer with a clever search procedure to find large instances of these objects.
A SAT$+$CAS Method

Computer Algebra System

Programmatic SAT Solver

Assignment

Clause