The Quartic Formula

The quartic formula gives the solutions of $ax^4 + bx^3 + cx^2 + dx + e = 0$ for real numbers a, b, c, d, e with $a \neq 0$.

 $-3b \pm \left(\sqrt{3\left(3b^2 - 8ac + 2a\sqrt[3]{4(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace} + \sqrt{(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace} + \sqrt{(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace})^2 + 2a\sqrt[3]{4(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace} + \sqrt{(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace})^2 + 2a\sqrt[3]{4(2c^3 - 9bcd + 27ad^2 +$

Directions: Choose all possibilities for the three \pm signs with the last two equivalent. Use real cube roots if possible, and principal roots otherwise.