

CS745/ECE725 Fall 2013

Homework 2

(Predicate Logic)

1. Prove or disprove the following derivations:

- $\forall x \bullet \exists y \bullet P(x, y) \vdash \exists y \bullet \forall x \bullet P(x, y)$
- $(\forall x \bullet P(x) \wedge Q(x)) \vdash ((\forall x \bullet P(x)) \wedge (\forall x \bullet Q(x)))$

2. Show that

$$(\forall x \bullet P(x) \vee Q(x)) \Leftrightarrow ((\forall x \bullet P(x)) \vee (\forall x \bullet Q(x)))$$

is not a tautology.

3. Using sequent calculus, prove that

$$\forall x \bullet \forall y \bullet A \vdash \forall y \bullet \forall x \bullet A$$

Deliverable

Your solutions must be typed and submitted by 4:00pm on Tuesday October 8 in class.