

ASSIGNMENT 3

1. Given a set S of points in the plane, its “onion peeling” consists of a sequence H_1, \dots, H_k of convex polygons, where H_1 is the convex hull of S , H_2 is the convex hull of S with the points of H_1 removed, etc. Draw yourself a picture. The onion peeling of a set of points can easily be found in $O(n^2)$ time using some of the convex hull algorithms from class.

(i) Give an $O(n^2)$ time algorithm using the incremental method of adding points by x -order.

(ii) Give an $O(n^2)$ time algorithm using gift-wrapping (Jarvis’s algorithm).

(iii) Is it easy to use Graham’s algorithm to get an $O(n^2)$ time algorithm?

In all cases, your answers may be brief. [Extra information not needed for this assignment: There is an $O(n \log n)$ time algorithm due to Chazelle.]

2. Consider the following randomized algorithm to find the minimum of n distinct integers. Take a random order x_1, \dots, x_n of the input numbers. Set $m = \infty$. For $i = 1 \dots n$, if $x_i < m$ then update m to x_i .

Use backwards analysis to argue that the expected number of times you update m is $O(\log n)$.

(You may use without proof the fact that the Harmonic numbers grow as $O(\log n)$.)