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1 Learning Goals

By the end of the exercise, you should be able to

- Construct a decision tree given an order of testing the features.
- Determine the prediction accuracy of a decision tree on a test set.
- Compute the entropy of a probability distribution.
- Compute the expected information gain for testing a feature.
- Trace the execution of and implement the ID3 algorithm. Construct a decision tree by selecting a feature for each node using the expected information gain metric.

2 Jeeves the valet - the data set

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 1 | Sunny | Hot | High | Weak | No |
| 2 | Sunny | Hot | High | Strong | No |
| 3 | Overcast | Hot | High | Weak | Yes |
| 4 | Rain | Mild | High | Weak | Yes |
| 5 | Rain | Cool | Normal | Weak | Yes |
| 6 | Rain | Cool | Normal | Strong | No |
| 7 | Overcast | Cool | Normal | Strong | Yes |
| 8 | Sunny | Mild | High | Weak | No |
| 9 | Sunny | Cool | Normal | Weak | Yes |
| 10 | Rain | Mild | Normal | Weak | Yes |
| 11 | Sunny | Mild | Normal | Strong | Yes |
| 12 | Overcast | Mild | High | Strong | Yes |
| 13 | Overcast | Hot | Normal | Weak | Yes |
| 14 | Rain | Mild | High | Strong | No |

Jeeves the valet – the training set

Jeeves the valet – the test set

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 1 | Sunny | Mild | High | Strong | No |
| 2 | Rain | Hot | Normal | Strong | No |
| 3 | Rain | Cool | High | Strong | No |
| 4 | Overcast | Hot | High | Strong | Yes |
| 5 | Overcast | Cool | Normal | Weak | Yes |
| 6 | Rain | Hot | High | Weak | Yes |
| 7 | Overcast | Mild | Normal | Weak | Yes |
| 8 | Overcast | Cool | High | Weak | Yes |
| 9 | Rain | Cool | High | Weak | Yes |
| 10 | Rain | Mild | Normal | Strong | No |
| 11 | Overcast | Mild | High | Weak | Yes |
| 12 | Sunny | Mild | Normal | Weak | Yes |
| 13 | Sunny | Cool | High | Strong | No |
| 14 | Sunny | Cool | High | Weak | No |

3 Practice Questions

3.1 Construct a decision tree given an order of testing the features

Question 1:

Considering the following partial decision tree generated using the training set. Assume that after we test Outlook = Sunny we are going to test Temp next. Also, assume that we always test Humidity before testing Wind. Generate the full decision tree using the training set.



3.2 The ID-3 Algorithm

Algorithm 1 ID3 Algorithm (Features, Examples)

1: If all examples are positive, return a leaf node with decision yes.

2: If all examples are negative, return a leaf node with decision no.

3: If no features left, return a leaf node with the most common decision of the examples.

4: If no examples left, return a leaf node with the most common decision of the examples in the parent. 5: else

- 6: choose the most important feature f
- 7: for each value v of feature f do
- 8: add arc with label v
- 9: add subtree $ID3(F f, s \in S | f(s) = v)$

```
10: end for
```

3.3 Trace the execution of ID-3 Algorithm

Question 2:

Suppose we add 3 extra data points into the training dataset. The training set becomes the following:

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 1 | Sunny | Hot | High | Weak | No |
| 2 | Sunny | Hot | High | Strong | No |
| 3 | Overcast | Hot | High | Weak | Yes |
| 4 | Rain | Mild | High | Weak | Yes |
| 5 | Rain | Cool | Normal | Weak | Yes |
| 6 | Rain | Cool | Normal | Strong | No |
| 7 | Overcast | Cool | Normal | Strong | Yes |
| 8 | Sunny | Mild | High | Weak | No |
| 9 | Sunny | Cool | Normal | Weak | Yes |
| 10 | Rain | Mild | Normal | Weak | Yes |
| 11 | Sunny | Mild | Normal | Strong | Yes |
| 12 | Overcast | Mild | High | Strong | Yes |
| 13 | Overcast | Hot | Normal | Weak | Yes |
| 14 | Rain | Mild | High | Strong | No |
| 15 | Sunny | Mild | High | Weak | No |
| 16 | Sunny | Mild | High | Weak | Yes |
| 17 | Sunny | Mild | High | Strong | Yes |

Jeeves the valet – the training set

Consider the partial decision tree generated from the above training set, generate the full decision tree using ID-3 Algorithm.



Question 3:

Suppose we add 1 extra data point to the original training set. The training set becomes the following:

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 1 | Sunny | Hot | High | Weak | No |
| 2 | Sunny | Hot | High | Strong | No |
| 3 | Overcast | Hot | High | Weak | Yes |
| 4 | Rain | Mild | High | Weak | Yes |
| 5 | Rain | Cool | Normal | Weak | Yes |
| 6 | Rain | Cool | Normal | Strong | No |
| 7 | Overcast | Cool | Normal | Strong | Yes |
| 8 | Sunny | Mild | High | Weak | No |
| 9 | Sunny | Cool | Normal | Weak | Yes |
| 10 | Rain | Mild | Normal | Weak | Yes |
| 11 | Sunny | Mild | Normal | Strong | Yes |
| 12 | Overcast | Mild | High | Strong | Yes |
| 13 | Overcast | Hot | Normal | Weak | Yes |
| 14 | Rain | Mild | High | Strong | No |
| 15 | Sunny | Hot | High | Weak | No |

Jeeves the valet – the training set

Consider the following partial decision tree generated from the above training set. Complete the branch of Temp = Hot.



Question 4:

What is the entropy of the distribution (0.5, 0.5)?

What is the entropy of the distribution (0.01, 0.99)?

Which distribution has more uncertainty?

Question 5:

Consider the original training set.

Jeeves the valet – the training set

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 1 | Sunny | Hot | High | Weak | No |
| 2 | Sunny | Hot | High | Strong | No |
| 3 | Overcast | Hot | High | Weak | Yes |
| 4 | Rain | Mild | High | Weak | Yes |
| 5 | Rain | Cool | Normal | Weak | Yes |
| 6 | Rain | Cool | Normal | Strong | No |
| 7 | Overcast | Cool | Normal | Strong | Yes |
| 8 | Sunny | Mild | High | Weak | No |
| 9 | Sunny | Cool | Normal | Weak | Yes |
| 10 | Rain | Mild | Normal | Weak | Yes |
| 11 | Sunny | Mild | Normal | Strong | Yes |
| 12 | Overcast | Mild | High | Strong | Yes |
| 13 | Overcast | Hot | Normal | Weak | Yes |
| 14 | Rain | Mild | High | Strong | No |

To construct a decision tree, we need to determine which feature to test first by Information Gain metric.

The following are the Information Gain of testing Temp and Wind at the first step. Calculate the Information Gain for the remaining features and determine which feature we should test first.

- Gain(Temp) = 0.029
- Gain(Wind) = 0.048

3.4 Handling Continuous Values

Question 6:

The following dataset is sorted according to the values of Temp.

| Day | Outlook | Temp | Humidity | Wind | Tennis? |
|-----|----------|------|----------|--------|---------|
| 7 | Overcast | 17.7 | Normal | Strong | Yes |
| 6 | Rain | 18.3 | Normal | Strong | No |
| 5 | Rain | 20.0 | Normal | Weak | Yes |
| 9 | Sunny | 20.6 | Normal | Weak | Yes |
| 4 | Rain | 21.1 | High | Weak | Yes |
| 14 | Rain | 21.7 | High | Strong | No |
| 8 | Sunny | 22.2 | High | Weak | No |
| 12 | Overcast | 22.2 | High | Strong | Yes |
| 10 | Rain | 23.9 | Normal | Weak | Yes |
| 11 | Sunny | 23.9 | Normal | Strong | Yes |
| 2 | Sunny | 26.6 | High | Strong | No |
| 13 | Overcast | 27.2 | Normal | Weak | Yes |
| 3 | Overcast | 28.3 | High | Weak | Yes |
| 1 | Sunny | 29.4 | High | Weak | No |

Determine whether we would consider the following values as possible split points

- Temp = 18
- Temp = 20.3
- Temp = 23.05
- Temp = 26.6