Logic and Computation: Introduction

Alice Gao
Lecture 1

Come and sit in the front. I won’t pick on you. :D
Outline

Let’s get acquainted

What is Logic and Computation?

Logistics and Resources
Let’s get acquainted

What is Logic and Computation?

Logistics and Resources
Who am I?

My name is Alice Gao. I grew up in Beijing, China, and have lived in Vancouver, Toronto, Cambridge (MA), Cambridge (UK), New York City, and Waterloo.

Research: artificial intelligence, game theory, education.

My work/education history:
- Lecturer, Computer Science, University of Waterloo.
- Postdoc, Computer Science, UBC.
- Ph.D., Computer Science, Harvard University.
- Undergraduate, Computer Science and Mathematics, UBC.

Hobbies: board games, escape room games, hiking, swimming, and traveling.
Meet your peers

- In the next 2 minutes, introduce yourself to someone you don’t know.
- Talk about courses, co-op, summer activities, dorms, extracurricular activities...
I’d like to learn your names

<table>
<thead>
<tr>
<th>On your index card, write</th>
<th>An example</th>
</tr>
</thead>
<tbody>
<tr>
<td>Your name</td>
<td>Xi Gao</td>
</tr>
<tr>
<td>Your preferred name and tips for pronunciation</td>
<td>Alice Gao</td>
</tr>
<tr>
<td>Student number</td>
<td>15270036</td>
</tr>
<tr>
<td>Something interesting about you</td>
<td>I once had a pet hedgehog named Ebbie.</td>
</tr>
</tbody>
</table>
Let’s get acquainted

What is Logic and Computation?

Logistics and Resources
CQ: Did you bring your clicker today?
Your expectations of this course

What have you heard about this course?

How do you feel about this course?

What do you expect the course to be like?
Some questions to answer

- Is logic useful especially for computer science?
- What is logic?
- Why do we need a formal language for logic?
Is logic useful for computer science?

Yes, of course.

Think of at least one application of logic in computer science.
Circuit Design

- Digital circuits are the basic building blocks of an electronic computer.

- CS 251: Computer Organization and Design
  CS 350: Operating Systems
Logic in Computer Science

Algorithms and Theory of Computing

- How much time and memory space do we need to solve a problem?
- Are there problems that cannot be solved by algorithms?
- CS 341: Algorithm Design and Analysis
- CS 360: Introduction to the Theory of Computing
Artificial Intelligence

- 19 billion FCC spectrum auction: Buy airwaves from television broadcasters and sell them to mobile phone carriers.
- IBM Watson won the Jeopardy Man vs. Machine Challenge
- CS 486: Artificial Intelligence
  CS 485: Machine Learning
Databases

- Structural Query Language (SQL) $\approx$ first-order logic
- Efficient query evaluation based on relational algebra
- Scale to large databases with parallel processors
- CS 348: Introduction to Database Management
  CS 448: Database Systems Implementation
Logic in Computer Science

Type Theory in Programming Language

- Propositions in logic $\leftrightarrow$ types in a programming language
- Proofs of a proposition $\leftrightarrow$ programs with the type
- Simplifications of proofs $\leftrightarrow$ evaluations of the programs

- CS 241: The compiler course
- CS 442: Principles of Programming Languages
- CS 444: Compiler Construction
Logic in Computer Science

Formal Verification

- Prove that a program is bug free. Bugs can be costly and dangerous in real life.
- Intel’s Pentium FDIV bug (1994) cost them half a billion dollars.
- Cancer patients died due to severe overdoses of radiation.
- CS 360: Theory of Computing (Finite Automata)
What is logic?

- Logic: Logykos (Greek) - pertaining to reasoning
- Logic = the science of reasoning, inference, and deduction.
- Logic = the analysis of arguments.
Being logical

I’ll be in your city tomorrow if you want to hang out.

But where will you be if I don’t want to hang out?!

You know, I just remembered I’m busy.

Why I try not to be pedantic about conditionals.
An example of logical deduction

Let’s look at two clips from the TV series Sherlock.

Series 1, Episode 1, 9:23
Series 1, Episode 1, 18:00
Logical Arguments

- Logic is the analysis of arguments.
- An argument is a set of statements, consisting of one or more premises and a conclusion.
- Logic studies the forms of the arguments. It does not study the content.
CQ: Is this argument valid?

The sun rises from the West. (premise)
If the sun rises from the West, then I will eat my hat. (premise)

I will eat my hat. (conclusion)

CQ: Is the above argument valid?

(A) Yes, it is valid.

(B) No, it is not valid.

(C) I don’t know...
Why do we need a formal language for logic?

- The English language is imprecise and ambiguous.
- Common sense is not always sufficient and reliable.
Claim: McDonald’s cheeseburger is better than eternal happiness.

Proof.
McDonald’s cheeseburger is better than nothing.
Nothing is better than eternal happiness.
Since $a > b$ and $b > c$, we can conclude $a > c$.
Then, McDonald’s cheeseburger is better than eternal happiness.
Russell’s paradox

Let $R$ be the set of all sets that are not members of themselves.

$$R = \{ x \mid x \notin x \}$$

Is $R$ a member of itself?
Let’s get acquainted

What is Logic and Computation?

Logistics and Resources
Grading

- Clicker questions (5%)
- Weekly assignments (20%)
- Midterm (25%)
  - Thursday, November 7, 4:30 pm to 6:20 pm
- Final exam (50%)
Resources

- **Course website**: things that do not change, e.g. office hours and lecture schedule.
- **Piazza**: things that do change, e.g. announcements, questions, and discussions.
- **Learn**: assignments, tutorial notes, assignment and exam solutions, and marks.
How do I succeed in this course?

- Engage during lectures and tutorials.
- Practice with the assignments and take advantage of office hours.
- Use learning goals as a study guide.
- Struggling is necessary for learning.