Abstract. The turning point problem

$$\begin{cases} -\varepsilon \Delta u + x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 0 & (x, y) \in [(-1, 1) \times (-1, 1)] \\ u(-1, y) = V_a, & u(1, y) = V_b, \\ u(x, -1) = V_c, & u(x, 1) = V_d, \end{cases}$$

is known to have some extremely small eigenvalues. No successful numerical solution to this problem has been reported. In this paper, a numerical procedure is proposed. All four boundary layers are well defined and the numerical singularity is successfully removed.

Key words. boundary layer, domain decomposition, overlap, Schwarz Alternating Method(*SAM*), turning point problem

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