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# Replace with your title

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**Yao-Liang Yu**

School of Computer Science  
University of Waterloo  
Waterloo, ON, N2L 3G1  
yaoliang.yu@uwaterloo.ca  
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## Abstract

1 Put here a brief summary of the project: what is it about and what are the main  
2 results. You also need to submit your code for reproducibility (a github link suf-  
3 fices). Be concise and to the point. Please limit the report to less than ( $\leq$ ) **4 pages**  
4 (references excluded).

## 5 1 Introduction

6 In this section you are going to present a brief background and motivation of your project. Consider  
7 summarizing the entire report in one overarching figure, such as Figure 1.

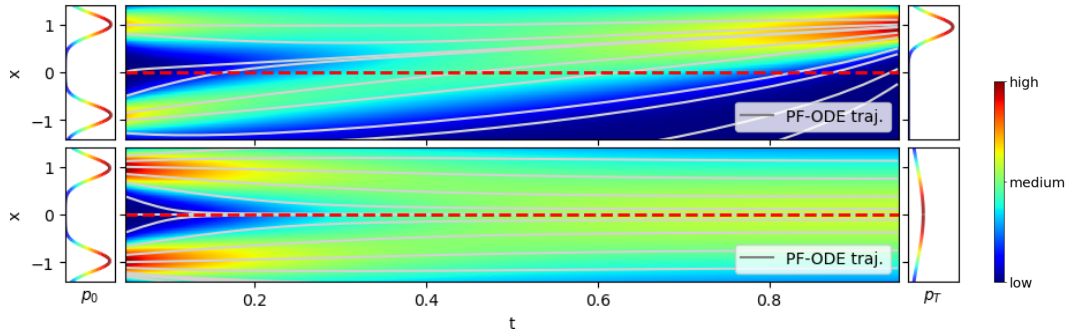


Figure 1: The evolution of  $p_t$  driven by diffusion processes where the data distribution  $p_0$  is invariant under flipping with respect to the origin. We also plot the PF-ODE trajectories to visualize the transition direction of  $p_t(x)$ . The upper plot has  $f(x, t) = \frac{1-x}{1-t}$  and  $g(t) = 1$ . The lower is VP-SDE with  $\alpha_t = 1 - t$ . For both processes,  $T = 0.95$ .

## 8 2 Related Works

9 Perform a reasonably thorough review of relevant literature. Has your approach, or one of similar  
10 nature, been considered before? By whom? What are the differences or limitations (if any)?

## 11 3 Main Results

12 Formulate your problem precisely (mathematically) and present the main methodology. Explain and  
13 justify each of your design choices, with some ablation studies to back them up.

Table 1: Model Comparison on 28x28x1 Rotated MNIST (Group C4). \* indicates author-reported values.

Model	FID↓				Inv-FID↓	$\Delta\hat{x}_0 \downarrow$
	1%	5%	10%	100%	100%	100%
SPDiff	5.97	<b>3.05</b>	3.47	2.81	2.21	0.2997
SPDiff+WT	5.80	3.34	3.57	3.50	2.20	0.0004
SPDiff+OC	6.10	3.09	3.45	2.82	2.12	0.0002
SPDiff+Reg	<b>5.42</b>	3.69	<b>2.83</b>	2.75	2.09	0.1806
SPDiff+Reg+OC	5.64	3.67	2.86	<b>2.64</b>	<b>2.07</b>	0.0002
SP-GAN	149*	99*	88*	81*	—	—
SP-GAN (Reprod.)	16.59	11.28	9.02	10.95	19.92	—

14 Please always give proper citations to prior work or results. Be precise and concise. Pay some  
 15 attention to the organization and layout of the entire paper. Add variety (table, curves, bar graph,  
 16 scatter plot, violin plot, pseudocode, etc.) and report statistical deviation (over at least 3~5 runs).

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**Algorithm 1:** Stochastic variance reduced proximal gradient

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**Input:**  $\mathbf{w}_0 \in \text{dom } f$

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1 for  $k = 0, 1, 2, \dots$  do
2    $\mathbf{g}_k \leftarrow \frac{1}{n} \sum_{i=1}^n \nabla \ell_i(\mathbf{w}_k)$            // compute full gradient at epoch  $k$ 
3    $\mathbf{w}_{k,0} \leftarrow \mathbf{w}_k$ 
17 4   for  $t = 0, \dots, m-1$  do
5     randomly draw  $i_t = i$  with probability  $p_i$ 
6      $\mathbf{g}_{k,t} \leftarrow \mathbf{g}_k - \frac{1}{np_{i_t}} \nabla \ell_{i_t}(\mathbf{w}_k) + \frac{1}{np_{i_t}} \nabla \ell_{i_t}(\mathbf{w}_{k,t})$            // amortized gradient
7      $\mathbf{w}_{k,t+1} \leftarrow P_r^{\eta_k}(\mathbf{w}_{k,t} - \eta_k \mathbf{g}_{k,t})$            // stochastic proximal gradient
8    $\mathbf{w}_{k+1} \leftarrow \frac{1}{m} \sum_{t=1}^m \mathbf{w}_{k,t}$            // in practice, can also do  $\mathbf{w}_{k+1} \leftarrow \mathbf{w}_{k,m}$ 

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## 18 4 Conclusion

19 What have we learned? What limitations or directions do you think are worth exploring in the  
 20 future?

21 **Acknowledgement**

22 Thank people who have helped or influenced you in this project. Figure 1 and Table 1 are from Lu  
23 et al. (2024).

24 **References**

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26 Based Generative Models”. In: *Advances in Neural Information Processing Systems 35*  
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- 28 Lu, H., S. Szabados, and Y. Yu (2024). “Structure Preserving Diffusion Models”.
- 29 Villani, C. (2003). “Topics in Optimal Transportation”. American Mathematical Society.
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31 *Computation*, vol. 23, no. 7, pp. 1661–1674.