



Extending Alloy to Express and Analyze Optimization Constraints

CS846 Project Presentation
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Overview

- Motivation, Technology, and Context
- Methodology and Implementation
- Demonstration
- Concluding Remarks



Motivation, Technology, and Context



Motivation

- *Feature configuration problem:*
 - How do we obtain the optimal configuration of features for a software product?
- *Solution:* combine lightweight modelling with discrete multiobjective optimization



Motivation

- *My objective*: enable the ability to express MOOPs (multiobjective optimization problems) in Alloy

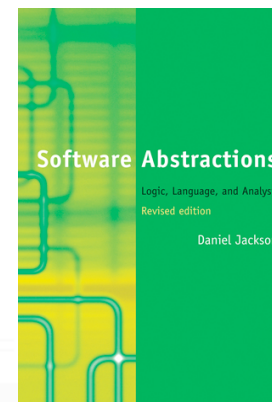


Technology

- Lightweight modelling
 - Alloy (<http://alloy.mit.edu/alloy/>)
- Multiobjective optimization using Moolloy (<http://sdg.csail.mit.edu/moolloy/>)
- Feature models & Design Space Modelling



Alloy



- A Language and Tool for Relational Models (<http://alloy.mit.edu/alloy/>)
- Logic and Language
 - First-order logic and transitive closure



Alloy

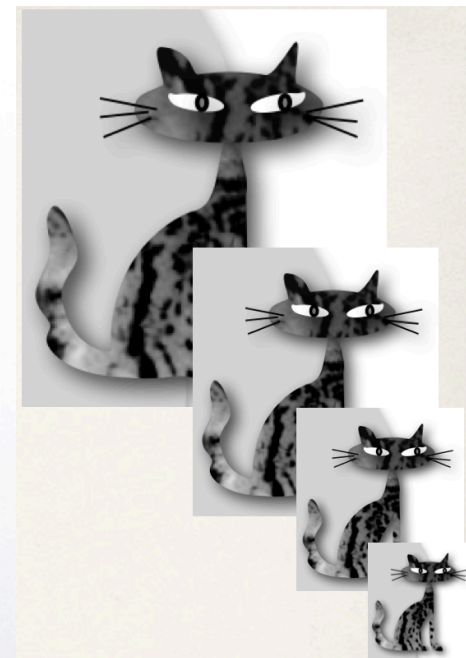


- Analysis
 - Model-finding / Simulation
 - Refutation: check assertions against a huge set (likely billions) of test cases to find a counter-example



Alloy+Kodkod

- The Alloy compiler translates a specification into a Kodkod formula
- Kodkod¹ (a relational constraint solver) translates its “bounded relational logic” to CNF using novel techniques
- Kodkod passes the formula to a backend SAT solver



¹E. Torlak and D. Jackson. “Kodkod: A Relational Model Finder,” *Proceedings of 13th International Conference on Tools and Algorithms for Construction and Analysis of Systems*, Braga, Portugal, April 2007. Lecture Notes in Computer Science, Vol. 4424, Berlin, Springer-Verlag, pp.632-647.



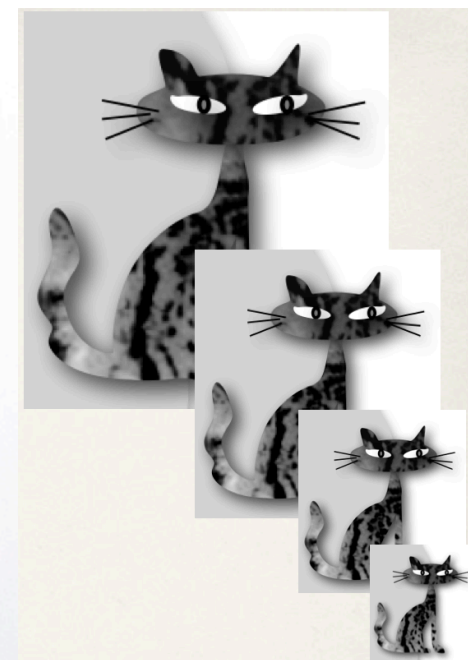
Alloy+Kodkod





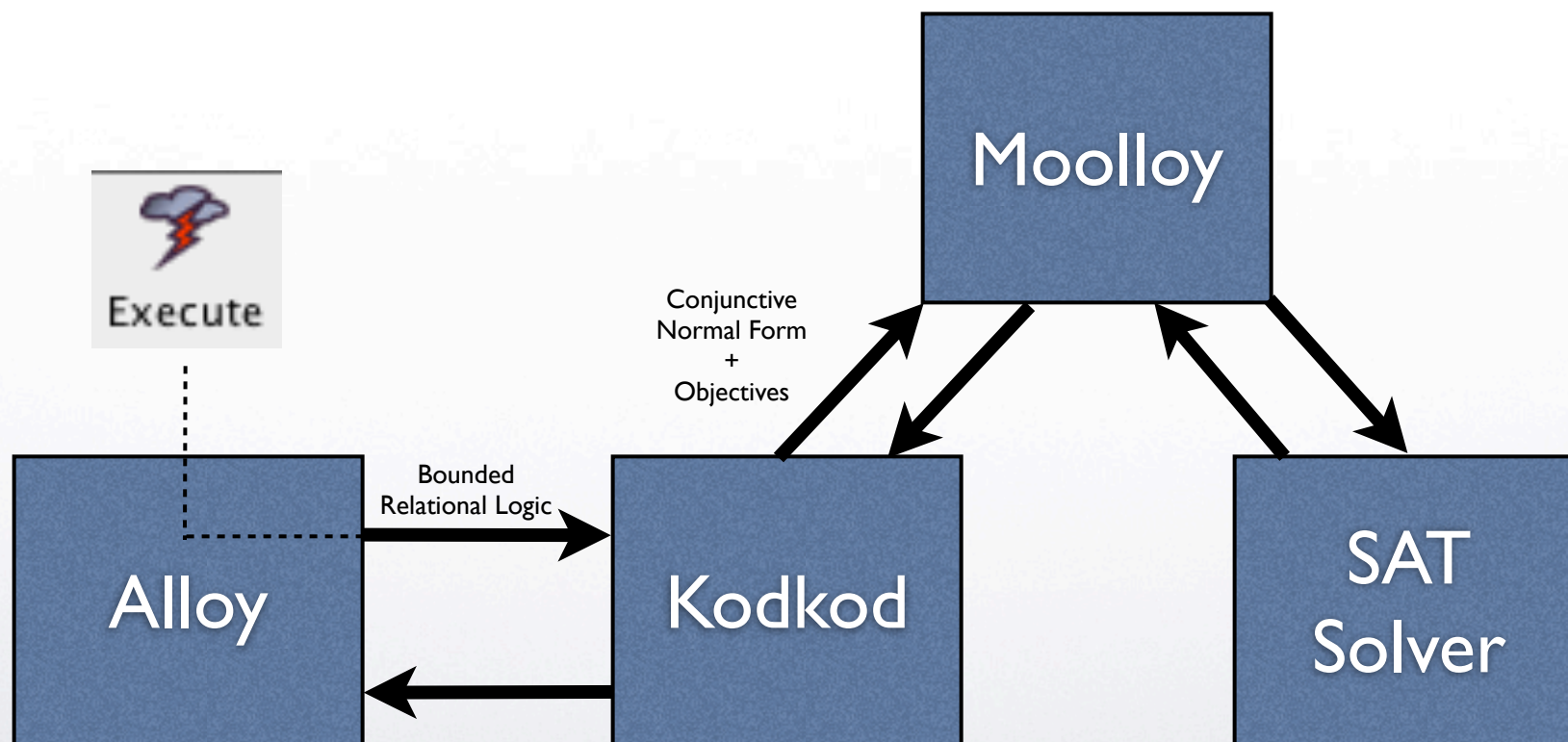
Alloy+MOOP

- Alloy calls Kodkod (as per usual)
- Kodkod, instead, passes control to Moolloy
- Moolloy uses the “Guided Improvement Algorithm” for solving discrete MOOPs





Alloy+MOOP





Optimization

- Single objective
 - 0-1 Knapsack: maximize the value of the contents of your knapsack subject to a weight restriction
 - one optimal solution



Optimization

- **Multiobjective**
 - maximize performance; minimize cost; maximize stability; minimize energy use...
 - one or more optimal solutions representing the trade-offs among the objectives



e/workspace/moolloy-ui-cason09/models/Bike.moolloy

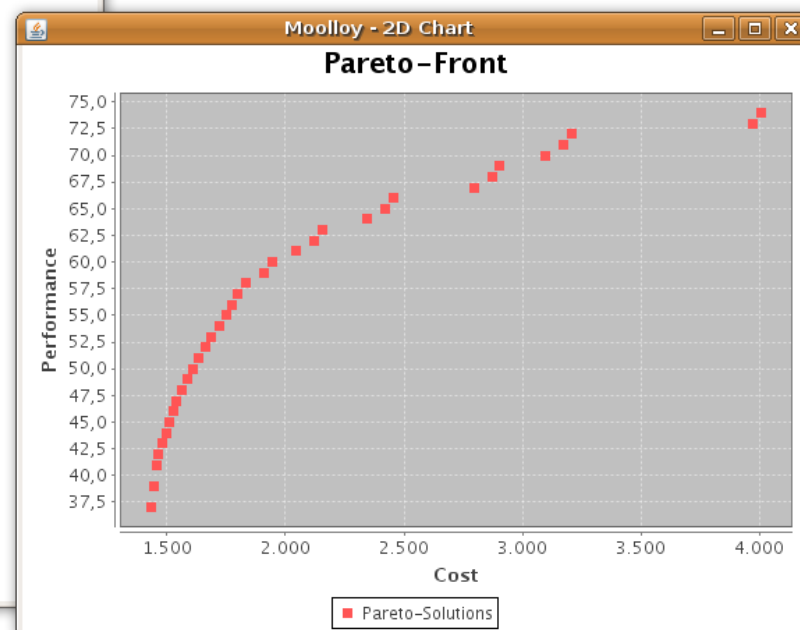
Metrics				
Name	Operator	Preference	Min	Max
Perform...	+	max		
Cost	+	min		

Frame		
Frame	Performance	Cost
Steel	5.0	800.0
Aluminum	8.0	1100.0
Carbon_fiber	10.0	1900.0

Fork		
Fork	Performance	Cost
RockShock_XL	9.0	800.0
Mountain_July	6.0	680.0
LST_AJR	9.0	750.0
none	3.0	0.0

Rear_mech		
Rear_mech	Performance	Cost
Shimano_XYZ	10.0	190.0
Shimano_XR	9.0	125.0
Shimano_Deo	7.0	75.0
Srum_10	10.0	160.0
Srum_9	8.0	130.0

Solutions to Bike.moolloy		
Solutions	Cost	Performance
soln0	2045.0	61.0
soln1	1720.0	54.0
soln2	1610.0	50.0
soln3	1610.0	50.0
soln4	1435.0	37.0
soln5	2345.0	64.0
soln6	1465.0	42.0
soln7	1775.0	56.0
soln8	1835.0	58.0
soln9	1635.0	51.0
soln10	1635.0	51.0
soln11	2455.0	66.0
soln12	1525.0	46.0
soln13	1525.0	46.0
soln14	1525.0	46.0





Moolloy+GIA

- The “guided improvement algorithm” (GIA¹) is used by Moolloy to solve MOOPs
- It repeatedly adjusts a Kodkod formula to ask for better and better solutions
- When no better solution exists, then an optimal solution has been identified on the Pareto Front
- Moolloy provides *exact* solutions

¹D. Rayside, H.-C. Estler and D. Jackson. “A Guided Improvement Algorithm for Exact, General Purpose, Many-Objective Combinatorial Optimization,” MIT-CSAIL-TR-2009-033.



Alloy + Partial Instances

- Alloy generates tuples for each relation bounded by a specified scope
- The ability to specify *partial instances* is a pre-requisite for Alloy+MOOP, because we need relations that map *specific* features to their metric values



```
inst inventory {  
  exactly 1 Product, --explore possible configs of one product  
  6 Int,             --large enough integers for our metrics  
  
  --inventory of options for each feature  
  F1 = F1O1 + F1O2 + F1O3,  
  F2 = F2O1 + F2O2 + F2O3,  
  
  --assignment of values to metrics for each option  
  m1 = F1O1->10 + F1O2->15 + F1O3->5 +  
        F2O1->4 + F2O2->16 + F2O3->8,  
  m2 = F1O1->5 + F1O2->7 + F1O3->3 +  
        F2O1->8 + F2O2->5 + F2O3->2  
}
```



Context

- Design Space Modelling and Analysis (Cai and Sullivan)
- MOOPs may arise when we consider possible decisions in software design
- Make optimal design decisions in terms of algorithm and data structure selection
- Minimize the impact of changes on other modules



Context

- Feature-oriented software development¹
 - A *feature* is a unit of functionality that satisfies some requirement
- Software systems are decomposed into their features
- Software Product Lines (SPLs) are generated from a set of features (i.e., configurations)

¹S. Apel and C. Kastner. An overview of feature-oriented software development. Journal of Object Technology, 8, 2009.



Context

- What if we have limited resources?
(i.e., CPU speed, memory, battery)
- Select features that satisfy stakeholder requirements within this constrained context
“optimal configurations”



Context

- The Alloy Analyzer can potentially allow us to step-through, and explore optimal configurations in an SPL
- We're essentially turning Alloy into a discrete MOOP solver



Methodology and Implementation



Methodology

- Update Alloy compiler
 - JFlex -- lexical analyzer
 - JavaCUP -- parser generator
 - Add new classes for AST



Methodology

- Translation of Alloy to Kodkod
 - Objectives must be translated and passed to Kodkod
- Update Kodkod to interact with Moolloy
- Alloy GUI is oblivious to backend changes



Implementation

- Updating JFlex (lex file)
 - Add new keywords:

objectives

maximize and **minimize**

optimize



Alloy+MOOP - Grammar

- Alloy 4 grammar

```
paragraph ::= sigDecl | factDecl | predDecl | funDecl  
| assertDecl | cmdDecl
```

- Alloy+MOOP

```
paragraph ::= sigDecl | factDecl | predDecl | funDecl  
| assertDecl | cmdDecl | instDecl | objDecl
```



```
objectives myGoals {  
    minimize energy,  
    maximize performance,  
    minimize memoryUse,  
    maximize stability  
}
```



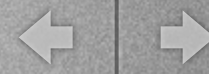
inst
block



run myPredicate **for** config
optimize myGoals



objectives
block



Demonstration



Demonstration

- Now we can use Alloy to solve problems such as 0-1 Knapsack
- Imagine: “executable declarative specifications”
- In fact, “Squander” uses an Alloy-like language for executing declarative syntax in Java (performs well on NP-complete problems)



Demonstration

- Product configuration
 - A product is specified as having a set of features
 - For each feature, we can specify a value for the metrics we are interested in
- Alloy+MOOP will solve for optimal configurations



Mandatory			Optional		
FeatureA	m1	m2	FeatureB	m1	m2
FAV1	5	4	FBV1	3	5
FAV2	4	2	FBV2	3	2

Configurations					
FeatureA	FeatureB	totalM1	totalM2	Optimal?	
FAV1	none	5	4	no	
FAV2	none	4	2	yes	
none	FBV1	3	5	no	
none	FBV2	3	2	no	
FAV1	FBV1	8	9	no	
FAV1	FBV2	8	6	yes	
FAV2	FBV1	7	7	no	
FAV2	FBV2	7	4	yes	



Concluding Remarks



Results

- The Alloy syntax has been extended to support the specification of optimization constraints
- The extension has enabled the ability to express and solve MOOPs via Alloy
- Rafael Olaechea will present his work (next) on translating Clafer to Alloy for MOOPs



Conclusions

- The new syntax enables the exploration of optimal configurations of software products
- This ability enables us to use Alloy as a MOOP solver, with the full-capabilities of Moolloy at our disposal



Lessons Learned

- Making changes to the Alloy compiler was *difficult*
 - Very little documentation
 - Some questionable design decisions
- Reminds us of the benefits of applying best-practices in our academic work



Future Work

- Additional work is currently underway to improve and better-define how the scope of relational variables are computed
- The problem of discontinuous integers leading to increased formula generation and solving time is still being addressed
- As part of their 4th-year design project, students are working on how to improve the visualization of Pareto-optimal solutions
- A group of nano students are writing Alloy models for discrete multiobjective optimization problems