

one more paper on dynamic graphs (connectivity rather than shortest paths)

[Efficient edge splitting-off algorithms maintaining all-pairs edge-connectivities](#)

[LC Lau, CK Yung](#) - Integer Programming and Combinatorial Optimization, 2010 - Springer

Abstract In this paper we present new **edge splitting-off** results **maintaining all-pairs edge-connectivities** of a graph. We first give an alternate proof of Mader's theorem, and use it to obtain a deterministic $O(r_{\max}^2 \cdot n^2)$ -time complete **edge splitting-off algorithm** for ...

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From: http://scholar.google.ca/scholar?q=%22Efficient+Edge+Splitting-Off+Algorithms+in+Maintaining+All-Pairs+Edge-Connectivities&btnG=&hl=en&as_sdt=0%2C5

will start here in F 2015

spanners

Given an edge-weighted graph, make it sparse while approximately preserving shortest paths.

original graph G , new graph G'

$$\forall u, v \in V \quad d_{G'}(u, v) \leq t \cdot d_G(u, v)$$

constant t - spanning ratio
= stretch factor

criteria

min. # edges in G'

min $\sum_{e \in G'} w(e)$

make G' "nice" e.g. planar, bounded degree

spanners of general graphs

greedy : given factor t
heuristic

initialize $E(G') = \emptyset$

consider $e_{(u,v)} \in E(G)$ ordered from min w to max

if $d_{G'}(u,v) > t \cdot d_G(u,v)$

then add (u,v) to G' .

(*)

On sparse spanners of weighted graphs

Althöfer, G Das, D Dobkin, D Joseph... - Discrete & Computational ..., 1993 - Springer

Abstract Given a **graph** G , a subgraph G' is at-**spanner** of G if, for every $u, v \in V$, the distance from u to v in G' is at most t times longer than the distance in G . In this paper we give a simple algorithm for constructing **sparse spanners** for arbitrary **weighted graphs**. We then apply ...

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geometric graphs

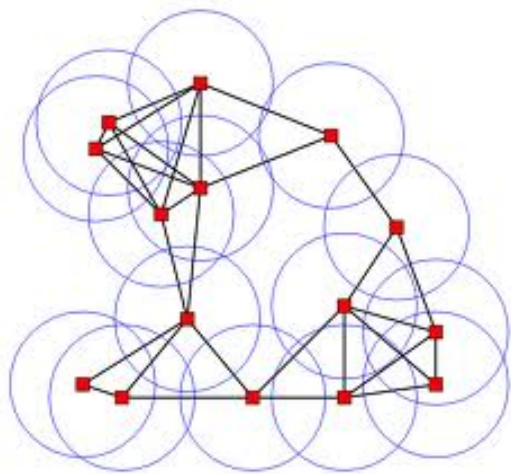
— complete Euclidean graph

Given n points in plane G — (implicit) complete graph
with Euclidean weights

Construct G'

$$d_{G'}(u, v) \leq t \cdot \underbrace{|uv|}_{\text{Euclidean distance}}$$

— unit disc graph



Given n points in plane
 G has edge (u, v) if $|uv| \leq 2$
Find good spanner $G' \subseteq G$

spanners

(not to present, just for reference)

Spanning trees and spanners[D Eppstein](#) - [Handbook of computational geometry, 1999](#) - [books.google.com](#)

This survey covers topics in geometric network design theory. The problem is easy to state: connect a collection of n sites by a "good" network. For instance, one may wish to connect components of a VLSI circuit by networks of wires, in a way that uses little surface area on ...

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From: http://scholar.google.ca/scholar?hl=en&q=Spanning+trees+and+spanners&btnG=&as_sdt=1%2C5&as_sdtp=

[BOOK] Geometric spanner networks[G Narasimhan](#), [M Smid](#) - 2007 - [langtoninfo.com](#)

11.1 Chapter overview 196 11.2 Dumbbells 197 11.3 A packing result for dumbbells 198
11.4 Establishing the length-grouping property 202 11.5 Establishing the empty-region
property 205 11.6 Dumbbell trees 207 11.7 Constructing the dumbbell trees 209 11.8 The ...

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From: http://scholar.google.ca/scholar?hl=en&q=geometric+spanner+networks&btnG=&as_sdt=1%2C5&as_sdtp=

**On plane geometric spanners: A survey and open problems**[P Bose](#), [M Smid](#) - [Computational Geometry, 2013](#) - Elsevier

Given a weighted graph $G=(V, E)$ and a real number $t \geq 1$, a t -spanner of G is a spanning subgraph G' with the property that for every edge xy in G , there exists a path between x and y in G' whose weight is no more than t times the weight of the edge xy . We review ...

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papers on geometric spanners — for complete Euclidean graph

planar spanners — $O(n)$ edges

P. Chew, There are planar graphs almost as good as the complete graph, Journal of Computer and System Sciences 39 (1989) 205–219.

— used type of Delaunay graph
— spanning ratio 2

Competitive routing in the half- θ 6-graph

P. Bose, R. Fagerberg, A. van Renssen... - Proceedings of the ..., 2012 - dl.acm.org

Page 1. **Competitive Routing** in the **Half- θ -Graph** * ... D 4 **Routing** in the **Half- θ -Graph**

In this section, we give matching upper and lower bounds for the **competitive routing** ratio on the **half- θ -graph**. We begin by defining our model. ...

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— easier pf. of above
— bounded degree

standard Delaunay as a spanner?

The stretch factor of the Delaunay triangulation is less than 1.998

G. Xia - SIAM Journal on Computing, 2013 - SIAM

Let S be a finite set of points in the Euclidean plane. Let D be a Delaunay triangulation of S .

The stretch factor (also known as dilation or spanning ratio) of D is the maximum ratio, among all points p and q in S , of the shortest path distance from p to q in D over the ...

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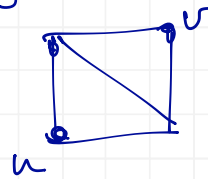
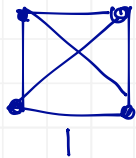
From: http://scholar.google.ca/scholar?cites=16099590622383505695&as_sdt=2005&sciodt=0.5&hl=en

standard Del. triangulation
breakthrough

lower bound 1.581

papers on geometric spanners

limit on spanning ratio for planar spanner



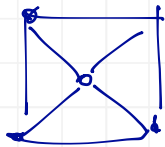
only planar spanner G'

$$d_{G'}(u, v) = 2$$

$$|uv| = \sqrt{2}$$

So we cannot beat $\sqrt{2}$ for spanning ratio

what about adding extra points - "Steiner" points



Planar spanners and approximate shortest path queries among obstacles in the plane

S Arikati, DZ Chen, LP Chew, G Das, M Smid... - Algorithms—ESA'96, 1996 - Springer

Abstract We consider the problem of finding an **obstacle-avoiding path between** two points s and t in the **plane**, amidst a set of disjoint polygonal **obstacles** with a total of n vertices. The length of this **path** should be within a small constant factor c of the length of the **shortest ...**

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