CS 886: Multiagent Systems Introduction to Social Choice

Kate Larson

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Kate Larson Social Choice

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Outline



- Motivation
- Formal Model
- Two Alternatives: A Special Case
- Three or More Alternatives 3
 - Case 1: Agents Specify Top Preference
 - Case 2: Agents Specify Complete Preferences
- Properties for Voting Protocols
 - Properties
 - Arrow's Theorem



Summary

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Motivation Formal Model

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Motivation Formal Model

What Is Social Choice Theory

- Study of decision problems in which a group has to make the decision
- The decision affects all members of the group
 - Their opinions should count!
- Applications
 - Political elections
 - Other elections
 - Allocations problems (e.g. allocation of money among agents, alocation of goods, tasks, resources....)

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Motivation Formal Model

CS Applications of Social Choice

- Multiagent Planning
- Computerized Elections
- Accepting a joint project
- Rating Web articles
- Rating CD's, movies,...

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Motivation Formal Model

Formal Model

- Set of agents $N = \{1, 2, \cdots, n\}$
- Set of outcomes O
- Set of strict total orders on O, L
- Social choice function: $f: L^n \to O$
- Social welfare function: *f* : *Lⁿ* → *L⁻* where *L⁻* is the set of weak total orders on *O*

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Motivation Formal Model

Assumptions

Agents have preferences over alternatives

Agents can rank order outcomes

Voters are sincere

They truthfully tell the center their preferences

Outcome is enforced on all agents

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Assume that there are only two alternatives, *x* and *y*. We can represent the family of preferences by

 $(\alpha_1,\ldots,\alpha_n)\in\mathbb{R}^n$

where α_i is 1, 0, or -1 according to whether agent *i* preferes *x* to *y*, is ambivalent between them, or prefers *y* to *x*.

Definition (Paretian)

A social choice function is **paretian** if it respects unanimity of strict preferences on the part of the agents.

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Majority Voting

$$f(\alpha_1,\ldots,\alpha_n) = \operatorname{sign} \sum_i \alpha_i$$

 $f(\alpha) = 1$ if and only if more agents prefer x to y and -1 if and onyl if more agents prefer y to x. Clearly majority voting is paretian.

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Additional Properties

- Symmetric among agents
- Neutral between alternatives
- Positively responsive

Theorem (May's Theorem)

A social choice function f is a majority voting rule if and only if it is symmetric among agents, neutral between alternatives, and positively responsive.

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Plurality Voting

The rules of plurality voting are probably familiar to you (e.g. the Canadian election system)

- One name is ticked on a ballot
- One round of voting
- One candidate is chosen
 - Candidate with the most votes

Is this a "good" voting system?

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Plurality Example

- 3 candidates
 - Lib, NDP, C

21 voters with the following preferences

- 10 C>NDP>Lib
- 6 NDP>Lib>C
- 5 Lib>NDP>C
- Result: C 10, NDP 6, Lib 5

The Conservative candidate wins, but a majority of voters (11) prefer all other parties more than the Conservatives.

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What Can We Do?

Majority system works well when there are two alternatives, but has problems when there are more alternatives.

Proposal: Organize a series of votes between 2 alternatives at a time

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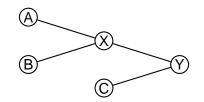
Case 1: Agents Specify Top Preference Case 2: Agents Specify Complete Preferences

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Agendas

- 3 alternatives {*A*, *B*, *C*}
- Agenda: (A, B, C)



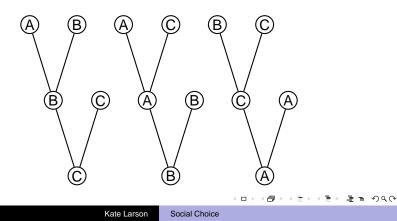
where X is the outcome of majority vote between A and B, and Y is the outcome of majority vote between X and C.

Case 1: Agents Specify Top Preference Case 2: Agents Specify Complete Preferences

Agenda Paradox: Power of the Agenda Setter

3 types of agents: A > C > B (35%), B > A > C (33%), C > B > A (32%).

3 different agendas:



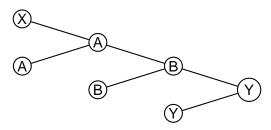
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Pareto Dominated Winner Paradox

4 alternatives and 3 agents

- X > Y > B > A
- A > X > Y > B
- B > A > X > Y



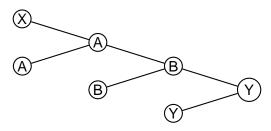
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Social Choice

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Maybe the problem is with the ballots

Now have agents reveal their entire preference ordering. Condorcet proposed the following

- Compare each pair of alternatives
- Declare "A" is socially preferred to "B" if more voters strictly prefer A to B

Condorcet Principle: If one alternative is preferred to *all other* candidates, then it should be selected.

Definition (Condorcet Winner)

An outcome $o \in O$ is a Condorcet Winner if $\forall o' \in O$, $\#(o > o') \ge \#(o' > o)$.

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Result: NDP win since 11/21 prefer them to the Conservatives and 16/21 prefer them to the Liberals.

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There Are Other Problems With Condorcet Winners

- 3 candidates: Liberal, NDP, Conservative
- 3 voters with preferences
 - Liberal > NDP>Conservative
 - NDP>Conservative>Liberal
 - Conservative>Liberal>NDP

Result: Condorcet winners do not always exist.

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There Are Other Problems With Condorcet Winners

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 - NDP>Conservative>Liberal
 - Conservative>Liberal>NDP

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Borda Count

- Each ballot is a list of ordered alternatives
- On each ballot, compute the rank of each alternative
- Rank order alternatives based on decreasing sum of their ranks

$$\begin{array}{rl} A > B > C & A : 4 \\ A > C > B & \Rightarrow & B : 8 \\ C > A > B & C : 6 \end{array}$$

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Borda Count

The Borda Count is simple

- There is always a Borda winner
- BUT the Borda winner is not always the Condorcet winner

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Other Borda Count Issues: Inverted-Order Paradox Agents

- X>C>B>A
- A>X>C>B
- B>A>X>C
- X>C>B>A
- A>X>C>B
- B>A>X>C
- X>C>B>A

Borda Scores

• X:13, A:18, B:19, C:20

Remove X

• C:13, B:14, A:15

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Vulnerability to Irrelevant Alternatives

3 types of agents

- X>Z>Y (35%)
- Y>X>Z (33%)
- Z>Y>X (32%)

The Borda winner is X.

Remove alternative Z. Then the Borda winner is Y.

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Other Scoring Rules

- Copeland
 - Do pairwise comparisons of outcomes.
 - Assign 1 point if an outcome wins, 0 if it loses, $\frac{1}{2}$ if it ties
 - Winner is the outcome with the highest summed score
- Kemeny
 - Given outcomes a and b, ranking r and vote v, define δ_{a,b}(r, v) = 1 if r and v agree on relative ranking of a and b
 - Kemeny ranking r' maximises $\sum_{v} \sum_{a,b} \delta_{a,b}(r, v)$

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Properties Arrow's Theorem

Properties for Voting Protocols

Property (Universality)

A voting protocol should work with any set of preferences.

Property (Transitivity)

A voting protocol should produce an ordered list of alternatives (social welfare function).

Property (Pareto efficiency)

If all agents prefer X to Y, then in the outcome X should be prefered to Y. That is, SWF f is pareto efficient if for any $o_1, o_2 \in O, \forall i \in N, o_1 >_i o_2$ then $o_1 >_f o_2$.

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Properties Arrow's Theorem

More Properties

Property (Independence of Irrelevant Alternatives (IIA))

Comparison of two alternatives depends only on their standings among agents' preferences, and not on the ranking of other alternatives. That is, SWF f is IIA if for any $o_1, o_2 \in O$

Property (No Dictators)

A SWF f has no dictator if $\neg \exists i \forall o_1, o_2 \in O, o_1 >_i o_2 \Rightarrow o_1 >_f o_2$

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Arrow's Theorem

Theorem (Arrow's Theorem)

If there are 3 or more alternatives and a finite number of agents, then there is no SWF which satisfies the 5 desired properties.

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Properties Arrow's Theorem

Is There Anything That Can Be Done?

Can we relax the properties?

- No dictator?
 - Fundamental for a voting protocol
- Paretian?
 - Also pretty fundamental
- Transitivity?
 - Maybe you only need to know the top ranked alternative?
 - Stronger form of Arrow's theorem says that you are still in trouble

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- IIA?
- Universality
 - Some hope here (1 dimensional preferences, spacial preferences...)

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Take-home Message

- Despair?
 - No ideal voting method
 - That would be boring!
- A group of more complex that an individual
- Weigh the pro's and cons of each system and understand the setting they will be used in
- Do not believe anyone who says they have the best voting system out there!

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For Further Reading I



A. Mas-Colell, M. Whinston, and J. Green. Microeconomic Theory. Oxford University Press, 1995.

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